

EXERCISE 12.1

PAGE NO: 251

1. There are 20 girls and 15 boys in a class.

(a) What is the ratio of number of girls to the number boys?

(b) What is the ratio of number of girls to the total number of students in the class?

Solutions:

Given

Number of girls = 20 girls

Number of boys = 15 boys

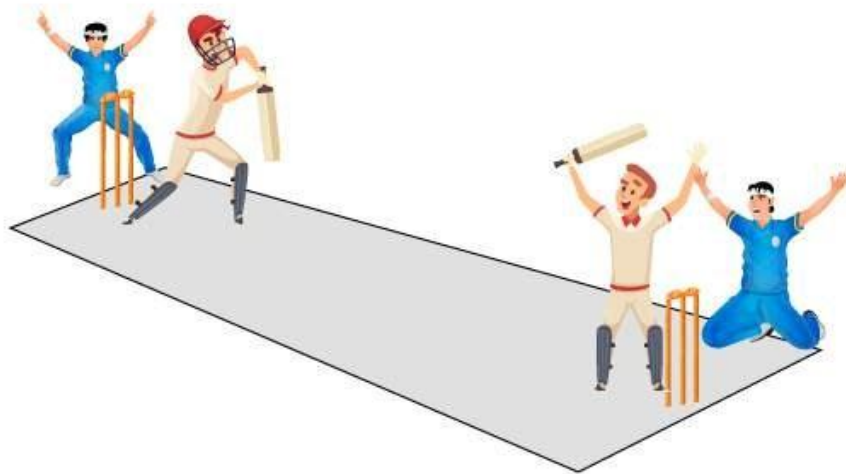
Total number of students = $20 + 15$

= 35

(a) Ratio of number of girls to number of boys = $20 / 15 = 4 / 3$

(b) Ratio of number of girls to total number of students = $20 / 35 = 4 / 7$

2. Out of 30 students in a class, 6 like football, 12 like cricket and remaining like tennis. Find the ratio of



(a) Number of students liking football to number of students liking tennis.

(b) Number of students liking cricket to total number of students.

Solutions:

Given

Number of students who like football = 6

Number of students who like cricket = 12

Number of students who like tennis = $30 - 6 - 12$

= 12

(a) Ratio of number of students liking football to the number of students liking tennis

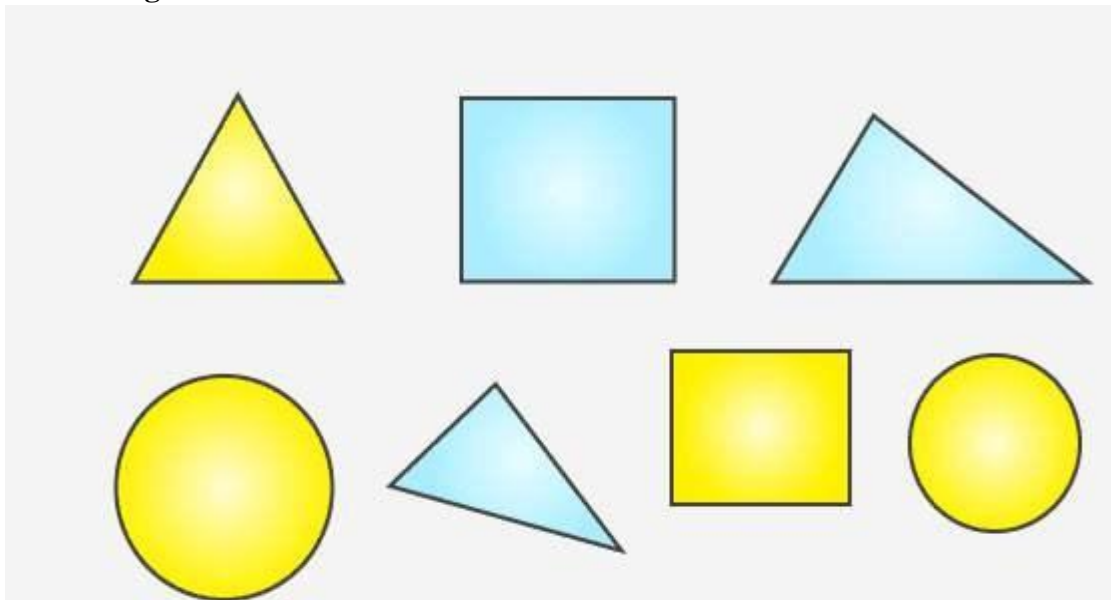
= $6 / 12 = 1 / 2$

(b) Ratio of number of students liking cricket to total number of

= $12 / 30$

= $2 / 5$

3. See the figure and find the ratio of



(a) Number of triangles to the number of circles inside the rectangle.

(b) Number of squares to all the figures inside the rectangle.

(c) Number of circles to all the figures inside the rectangle.

Solutions:

Given in the figure

Number of triangles = 3

Number of circles = 2

Number of squares = 2

Total number of figures = 7

(a) Ratio of number of triangles to the number of circles inside the rectangle

$$= 3 / 2$$

(b) Ratio of number of squares to all the figures inside the rectangle

$$= 2 / 7$$

(c) Ratio of number of circles to all the figures inside the rectangle

$$= 2 / 7$$

4. Distance travelled by Hamid and Akhtar in an hour are 9 km and 12 km. Find the ratio of speed of Hamid to the speed of Akhtar.

Solutions:

We know that the speed of a certain object is the distance travelled by that object in an hour

Distance travelled by Hamid in one hour = 9 km

Distance travelled by Akhtar in one hour = 12 km

Speed of Hamid = 9 km/hr

Speed of Akhtar = 12 km/hr

Ratio of speed of Hamid to the speed of Akhtar = $9 / 12 = 3 / 4$

5. Fill in the following blanks:

$$15 / 18 = \square / 6 = 10 / \square = \square / 30 \text{ [Are these equivalent ratios?]}$$

Solutions:

$$15 / 18 = (5 \times 3) / (6 \times 3) \\ = 5 / 6$$

$$5 / 6 = (5 \times 2) / (6 \times 2) \\ = 10 / 12$$

$$5 / 6 = (5 \times 5) / (6 \times 5) \\ = 25 / 30$$

Hence, 5, 12 and 25 are the numbers which come in the blanks respectively. Yes, all are equivalent ratios.

6. Find the ratio of the following:

(a) 81 to 108

(b) 98 to 63

(c) 33 km to 121 km

(d) 30 minutes to 45 minutes

Solutions:

$$(a) 81 / 108 = (3 \times 3 \times 3 \times 3) / (2 \times 2 \times 3 \times 3 \times 3) \\ = 3 / 4$$

$$(b) 98 / 63 = (14 \times 7) / (9 \times 7) \\ = 14 / 9$$

$$(c) 33 / 121 = (3 \times 11) / (11 \times 11) \\ = 3 / 11$$

$$(d) 30 / 45 = (2 \times 3 \times 5) / (3 \times 3 \times 5) \\ = 2 / 3$$

7. Find the ratio of the following:

(a) 30 minutes to 1.5 hours

(b) 40 cm to 1.5 m

(c) 55 paise to \square 1

(d) 500 ml to 2 litres

Solutions:

(a) 30 minutes to 1.5 hours

$$30 \text{ min} = 30 / 60$$

$$= 0.5 \text{ hours}$$

$$\text{Required ratio} = (0.5 \times 1) / (0.5 \times 3)$$

$$= 1 / 3$$

(b) 40 cm to 1.5 m

$$1.5 \text{ m} = 150 \text{ cm}$$

$$\text{Required ratio} = 40 / 150$$

$$= 4 / 15$$

(c) 55 paise to \square 1

$$\square 1 = 100 \text{ paise}$$

$$\begin{aligned} \text{Required ratio} &= 55 / 100 = (11 \times 5) / (20 \times 5) \\ &= 11 / 20 \end{aligned}$$

(d) 500 ml to 2 litres

$$1 \text{ litre} = 1000 \text{ ml}$$

$$2 \text{ litre} = 2000 \text{ ml}$$

$$\begin{aligned} \text{Required ratio} &= 500 / 2000 = 5 / 20 = 5 / (5 \times 4) \\ &= 1 / 4 \end{aligned}$$

8. In a year, Seema earns \square 1,50,000 and saves \square 50,000. Find the ratio of (a) Money that Seema earns to the money she saves (b) Money that she saves to the money she spends.

Solutions:

$$\text{Money earned by Seema} = \square 150000$$

$$\text{Money saved by her} = \square 50000$$

$$\text{Money spent by her} = \square 150000 - \square 50000 = \square 100000$$

$$\begin{aligned} \text{(a) Ratio of money earned to money saved} &= 150000 / 50000 = 15 / 5 \\ &= 3 / 1 \end{aligned}$$

$$\begin{aligned} \text{(b) Ratio of money saved to money spent} &= 50000 / 100000 = 5 / 10 \\ &= 1 / 2 \end{aligned}$$

9. There are 102 teachers in a school of 3300 students. Find the ratio of the number of teachers to the number of students.

Solutions:

Given

$$\text{Number of teachers in a school} = 102$$

$$\text{Number of students in a school} = 3300$$

$$\begin{aligned} \text{Ratio of number of teachers to the number of students} &= 102 / 3300 \\ &= (2 \times 3 \times 17) / (2 \times 3 \times 550) \\ &= 17 / 550 \end{aligned}$$

10. In a college, out of 4320 students, 2300 are girls. Find the ratio of (a) Number of girls to the total number of students. (b) Number of boys to the number of girls.

(c) Number of boys to the total number of students.

Solutions:

Given

$$\text{Total number of students} = 4320$$

$$\text{Number of girls} = 2300$$

$$\begin{aligned} \text{Number of boys} &= 4320 - 2300 \\ &= 2020 \end{aligned}$$

- (a) Ratio of number of girls to the total number of students = $2300 / 4320$
 $= (2 \times 2 \times 5 \times 115) / (2 \times 2 \times 5 \times 216)$
 $= 115 / 216$
- (b) Ratio of number of boys to the number of girls = $2020 / 2300$
 $= (2 \times 2 \times 5 \times 101) / (2 \times 2 \times 5 \times 115)$
 $= 101 / 115$
- (c) Ratio of number of boys to the total number of students = $2020 / 4320$
 $= (2 \times 2 \times 5 \times 101) / (2 \times 2 \times 5 \times 216)$
 $= 101 / 216$

11. Out of 1800 students in a school, 750 opted basketball, 800 opted cricket and remaining opted table tennis. If a student can opt only one game, find the ratio of

(a) Number of students who opted basketball to the number of students who opted table tennis. (b) Number of students who opted cricket to the number of students opting basketball. (c) Number of students who opted basketball to the total number of students.

Solutions:

- (a) Ratio of number of students who opted basketball to the number of students who opted table tennis = $750 / 250 = 3 / 1$
- (b) Ratio of number of students who opted cricket to the number of students opting basketball = $800 / 750 = 16 / 15$
- (c) Ratio of number of students who opted basketball to the total number of students = $750 / 1800 = 25 / 60 = 5 / 12$

12. Cost of a dozen pens is ₹ 180 and cost of 8 ball pens is ₹ 56. Find the ratio of the cost of a pen to the cost of a ball pen.

Solutions:

$$\begin{aligned} \text{Cost of a dozen pens} &= ₹ 180 \\ \text{Cost of 1 pen} &= 180 / 12 \\ &= ₹ 15 \\ \text{Cost of 8 ball pens} &= ₹ 56 \\ \text{Cost of 1 ball pen} &= 56 / 8 \\ &= ₹ 7 \end{aligned}$$

Hence, required ratio is $15 / 7$

13. Consider the statement: Ratio of breadth and length of a hall is 2: 5. Complete the following table that shows some possible breadths and lengths of the hall.

Solutions:

- (i) Length = 50 m
 Breadth / 50 = $2 / 5$
 By cross multiplication
 $5 \times \text{breadth} = 50 \times 2$
 Breadth = $(50 \times 2) / 5$
 $= 100 / 5$

$$= 20 \text{ m}$$

(ii) Breadth = 40 m

$$40 / \text{Length} = 2 / 5$$

By cross multiplication

$$2 \times \text{Length} = 40 \times 5$$

$$\text{Length} = (40 \times 5) / 2$$

$$\text{Length} = 200 / 2$$

$$\text{Length} = 100 \text{ m}$$

14. Divide 20 pens between Sheela and Sangeeta in the ratio of 3: 2.

Breadth of the hall (in metres)	10		40
Length of the hall (in metres)	25	50	

Solutions:

Terms of 3: 2 = 3 and 2

Sum of these terms = 3 + 2

$$= 5$$

Now Sheela will get $3 / 5$ of total pens and Sangeeta will get $2 / 5$ total pens

Number of pens having with Sheela = $3 / 5 \times 20$

$$= 3 \times 4$$

$$= 12$$

Number of pens having with Sangeeta = $2 / 5 \times 20$

$$= 2 \times 4$$

$$= 8$$

15. Mother wants to divide ₹ 36 between her daughters Shreya and Bhoomika in the ratio of their ages. If age of Shreya is 15 years and age of Bhoomika is 12 years, find how much Shreya and Bhoomika will get.



Solutions:

$$\begin{aligned}\text{Ratio of ages} &= 15 / 12 \\ &= 5 / 4\end{aligned}$$

Hence, mother wants to divide ₹ 36 in the ratio of 5: 4

Terms of 5: 4 are 5 and 4

$$\begin{aligned}\text{Sum of these terms} &= 5 + 4 \\ &= 9\end{aligned}$$

Here Shreya will get $5 / 9$ of total money and Sangeeta will get $4 / 9$ of total money

$$\begin{aligned}\text{The amount Shreya get} &= 5 / 9 \times 36 \\ &= 20\end{aligned}$$

$$\begin{aligned}\text{The amount Sangeeta get} &= 4 / 9 \times 36 \\ &= 16\end{aligned}$$

Therefore Shreya will get ₹ 20 and Sangeeta will get ₹ 16

16. Present age of father is 42 years and that of his son is 14 years. Find the ratio of

- (a) Present age of father to the present age of son
 (b) Age of the father to the age of son, when son was 12 years old.
 (c) Age of father after 10 years to the age of son after 10 years.
 (d) Age of father to the age of son when father was 30 years old. Solutions:

- (a) Present age of father = 42 years

Present age of son = 14 years

$$\begin{aligned}\text{Required ratio} &= 42 / 14 \\ &= 3 / 1\end{aligned}$$

- (b) The son was 12 years old 2 years ago. So the age father 2 years ago will be

$$= 42 - 2 = 40 \text{ years}$$

$$\text{Required ratio} = 40 / 12 = (4 \times 10) / (4 \times 3) = 10 / 3$$

- (c) After ten years age of father = $42 + 10 = 52$ years

After 10 years age of son = $14 + 10 = 22$ years

$$\begin{aligned}\text{Required ratio} &= 52 / 24 = (4 \times 13) / (4 \times 6) \\ &= 13 / 6\end{aligned}$$

- (d) 12 years ago, age of father was 30

At that time age of son = $14 - 12$

$$= 2 \text{ years}$$

$$\begin{aligned}\text{Required ratio} &= 30 / 2 = (2 \times 15) / 2 \\ &= 15 / 1\end{aligned}$$

EXERCISE 12.2

PAGE NO: 255

1. Determine if the following are in proportion.

- (a) 15, 45, 40, 120
(b) 33, 121, 9, 96
(c) 24, 28, 36, 48
(d) 32, 48, 70, 210
(e) 4, 6, 8, 12
(f) 33, 44, 75, 100

Solutions:

- (a) 15, 45, 40, 120
 $15 / 45 = 1 / 3$
 $40 / 120 = 1 / 3$
Hence, 15: 45 = 40:120
 \therefore These are in a proportion
- (b) 33, 121, 9, 96
 $33 / 121 = 3 / 11$
 $9 / 96 = 3 / 32$
Hence 33:121 \neq 9: 96
 \therefore These are not in a proportion
- (c) 24, 28, 36, 48
 $24 / 28 = 6 / 7$
 $36 / 48 = 3 / 4$
Hence, 24: 28 \neq 36:48
 \therefore These are not in a proportion
- (d) 32, 48, 70, 210
 $32 / 48 = 2 / 3$
 $70 / 210 = 1 / 3$
Hence, 32: 48 \neq 70: 210
 \therefore These are not in a proportion
- (e) 4, 6, 8, 12
 $4 / 6 = 2 / 3$
 $8 / 12 = 2 / 3$
Hence 4: 6 = 8: 12
 \therefore These are in a proportion
- (f) 33, 44, 75, 100
 $33 / 44 = 3 / 4$
 $75 / 100 = 3 / 4$
Hence, 33:44 = 75: 100
 \therefore These are in a proportion

2. Write True (T) or False (F) against each of the following statements :

- (a) $16 : 24 :: 20 : 30$
(b) $21 : 6 :: 35 : 10$
(c) $12 : 18 :: 28 : 12$
(d) $8 : 9 :: 24 : 27$
(e) $5.2 : 3.9 :: 3 : 4$
(f) $0.9 : 0.36 :: 10 : 4$

Solutions:

- (a) $16 : 24 :: 20 : 30$
 $16 / 24 = 2 / 3$
 $20 / 30 = 2 / 3$
Hence, $16 : 24 = 20 : 30$
Therefore True
- (b) $21 : 6 :: 35 : 10$
 $21 / 6 = 7 / 2$
 $35 / 10 = 7 / 2$
Hence, $21 : 6 = 35 : 10$
Therefore True
- (c) $12 : 18 :: 28 : 12$
 $12 / 18 = 2 / 3$
 $28 / 12 = 7 / 3$
Hence, $12 : 18 \neq 28 : 12$
Therefore False
- (d) $8 : 9 :: 24 : 27$
We know that $= 24 / 27 = (3 \times 8) / (3 \times 9)$
 $= 8 / 9$
Hence, $8 : 9 = 24 : 27$
Therefore True
- (e) $5.2 : 3.9 :: 3 : 4$
As $5.2 / 3.9 = 4 / 3$
Hence, $5.2 : 3.9 \neq 3 : 4$
Therefore False
- (f) $0.9 : 0.36 :: 10 : 4$
 $0.9 / 0.36 = 90 / 36$
 $= 10 / 4$
Hence, $0.9 : 0.36 = 10 : 4$
Therefore True

3. Are the following statements true?

- (a) $40 \text{ persons} : 200 \text{ persons} = \square 15 : \square 75$
(b) $7.5 \text{ litres} : 15 \text{ litres} = 5 \text{ kg} : 10 \text{ kg}$
(c) $99 \text{ kg} : 45 \text{ kg} = \square 44 : \square 20$

(d) $32 \text{ m} : 64 \text{ m} = 6 \text{ sec} : 12 \text{ sec}$

(e) $45 \text{ km} : 60 \text{ km} = 12 \text{ hours} : 15 \text{ hours}$

Solutions:

(a) $40 \text{ persons} : 200 \text{ persons} = \square 15 : \square 75$

$$40 / 200 = 1 / 5$$

$$15 / 75 = 1 / 5$$

Hence, True

(b) $7.5 \text{ litres} : 15 \text{ litres} = 5 \text{ kg} : 10 \text{ kg}$

$$7.5 / 15 = 1 / 2$$

$$5 / 10 = 1 / 2$$

Hence, True

(c) $99 \text{ kg} : 45 \text{ kg} = \square 44 : \square 20$

$$99 / 45 = 11 / 5$$

$$44 / 20 = 11 / 5$$

Hence, True

(d) $32 \text{ m} : 64 \text{ m} = 6 \text{ sec} : 12 \text{ sec}$

$$32 / 64 = 1 / 2$$

$$6 / 12 = 1 / 2$$

Hence, True

(e) $45 \text{ km} : 60 \text{ km} = 12 \text{ hours} : 15 \text{ hours}$

$$45 / 60 = 3 / 4$$

$$12 / 15 = 4 / 5$$

Hence, False

4. Determine if the following ratios form a proportion. Also, write the middle terms and extreme terms where the ratios form a proportion.

(a) $25 \text{ cm} : 1 \text{ m}$ and $\square 40 : \square 160$

(b) $39 \text{ litres} : 65 \text{ litres}$ and $6 \text{ bottles} : 10 \text{ bottles}$

(c) $2 \text{ kg} : 80 \text{ kg}$ and $25 \text{ g} : 625 \text{ g}$ (d) $200 \text{ mL} : 2.5 \text{ litre}$ and $\square 4 : \square 50$ **Solutions:**

(a) $25 \text{ cm} : 1 \text{ m}$ and $\square 40 : \square 160$

$$25 \text{ cm} = 25 / 100 \text{ m}$$

$$= 0.25 \text{ m}$$

$$0.25 / 1 = 1 / 4$$

$$40 / 160 = 1 / 4$$

Yes, these are in a proportion

Middle terms are 1 m, $\square 40$ and Extreme terms are 25 cm, $\square 160$

(b) $39 \text{ litres} : 65 \text{ litres}$ and $6 \text{ bottles} : 10 \text{ bottles}$

$$39 / 65 = 3 / 5$$

$$6 / 10 = 3 / 5$$

Yes, these are in a proportion

Middle terms are 65 litres, 6 bottles and Extreme terms are 39 litres, 10 bottles

(c) 2 kg : 80 kg and 25 g : 625 g

$$2 / 80 = 1 / 40$$

$$25 / 625 = 1 / 25$$

No, these are not in a proportion

(d) 200 mL : 2.5 litre and \square 4 : \square 50

$$1 \text{ litre} = 1000 \text{ ml}$$

$$2.5 \text{ litre} = 2500 \text{ ml}$$

$$200 / 2500 = 2 / 5$$

$$4 / 50 = 2 / 25$$

Yes, these are in a proportion

Middle terms are 2.5 litres, \square 4 and Extreme terms are 200 ml, \square 50

EXERCISE 12.3

PAGE NO: 259

1. If the cost of 7 m of cloth is ₹ 1470, find the cost of 5 m of cloth.**Solutions:**

Given

$$\text{Cost of 7 m cloth} = ₹ 1470$$

$$\text{Cost of 1 m cloth} = 1470 / 7$$

$$= ₹ 210$$

$$\text{So, cost of 5 cloth} = 210 \times 5 = 1050$$

∴ Cost of 5 m cloth is ₹ 1050

2. Ekta earns ₹ 3000 in 10 days. How much will she earn in 30 days?**Solutions:**

$$\text{Money earned by Ekta in 10 days} = ₹ 3000$$

$$\text{Money earned in one day by her} = 3000 / 10$$

$$= ₹ 300$$

$$\text{So, money earned by her in 30 days} = 300 \times 30$$

$$= ₹ 9000$$

3. If it has rained 276 mm in the last 3 days, how many cm of rain will fall in one full week (7 days)? Assume that the rain continues to fall at the same rate.**Solutions:**

$$\text{Measure of rain in 3 days} = 276 \text{ mm}$$

$$\text{Measure of rain in one day} = 276 / 3$$

$$= 92 \text{ mm}$$

$$\text{So, measure of rain in one week i.e 7 days} = 92 \times 7$$

$$= 644 \text{ mm}$$

$$= 644 / 10$$

$$= 64.4 \text{ cm}$$

4. Cost of 5 kg of wheat is ₹ 91.50.**(a) What will be the cost of 8 kg of wheat?****(b) What quantity of wheat can be purchased in ₹ 183?****Solutions:**

$$\text{(a) Cost of 5 kg wheat} = ₹ 91.50.$$

$$\text{Cost of 1 kg wheat} = 91.50 / 5$$

$$= ₹ 18.3$$

$$\text{So, cost of 8 kg wheat} = 18.3 \times 8$$

$$= ₹ 146.40$$

$$\text{(b) Wheat purchased in ₹ 91.50} = 5 \text{ kg}$$

$$\text{Wheat purchased in ₹ 1} = 5 / 91.50 \text{ kg}$$

$$\text{So, wheat purchased in ₹ 183} = (5 / 91.50) \times 183$$

$$= 10 \text{ kg}$$

5. The temperature dropped 15 degree celsius in the last 30 days. If the rate of temperature drop remains the same, how many degrees will the temperature drop in the next ten days?

Solutions:

$$\text{Temperature drop in 30 days} = 15^{\circ} \text{ C}$$

$$\text{Temperature drop in 1 day} = 15 / 30$$

$$= (1 / 2)^{\circ} \text{ C}$$

$$\text{So, temperature drop in next 10 days} = (1 / 2) \times 10$$

$$= 5^{\circ} \text{ C}$$

$$\therefore \text{The temperature drop in the next 10 days will be } 5^{\circ} \text{ C}$$

6. Shaina pays ₹ 15000 as rent for 3 months. How much does she has to pay for a whole year, if the rent per month remains same?

Solutions:

$$\text{Rent paid by Shaina in 3 months} = ₹ 15000$$

$$\text{Rent for 1 month} = 15000 / 3$$

$$= ₹ 5000$$

$$\text{So, rent for 12 months i.e 1 year} = 5000 \times 12$$

$$= ₹ 60,000$$

$$\therefore \text{Rent paid by Shaina in 1 year is } ₹ 60,000$$

7. Cost of 4 dozen bananas is ₹ 180. How many bananas can be purchased for ₹ 90?

Solutions:

$$\text{Number of bananas bought in } ₹ 180 = 4 \text{ dozens}$$

$$= 4 \times 12$$

$$= 48 \text{ bananas}$$

$$\text{Number of bananas bought in } ₹ 1 = 48 / 180$$

$$\text{So, number of bananas bought in } ₹ 90 = (48 / 180) \times 90$$

$$= 24 \text{ bananas}$$

$$\therefore 24 \text{ bananas can be purchased in } ₹ 90$$

8. The weight of 72 books is 9 kg. What is the weight of 40 such books?

Solutions:

$$\text{Weight of 72 books} = 9 \text{ kg}$$

$$\text{Weight of 1 book} = 9 / 72$$

$$= 1 / 8 \text{ kg}$$

$$\text{So, weight of 40 books} = (1 / 8) \times 40$$

$$= 5 \text{ kg}$$

$$\therefore \text{Weight of 40 books is } 5 \text{ kg}$$

9. A truck requires 108 litres of diesel for covering a distance of 594 km. How much diesel will be required by the truck to cover a distance of 1650 km?

Solutions:

Diesel required for 594 km = 108 litres

Diesel required for 1 km = $108 / 594$

= $2 / 11$ litre

So, diesel required for 1650 km = $(2 / 11) \times 1650$

= 300 litres

- ∴ Diesel required by the truck to cover a distance of 1650 km is 300 litres

10. Raju purchases 10 pens for ₹ 150 and Manish buys 7 pens for ₹ 84. Can you say who got the pens cheaper?

Solutions:

Pens purchased by Raju in ₹ 150 = 10 pens

Cost of 1 pen = $150 / 10$

= ₹ 15

Pens purchased by Manish in ₹ 84 = 7 pens

Cost of 1 pen = $84 / 7$

= ₹ 12

∴ Pens purchased by Manish are cheaper than Raju

11. Anish made 42 runs in 6 overs and Anup made 63 runs in 7 overs. Who made more runs per over?

Solutions:

Runs made by Anish in 6 overs = 42

Runs made by Anish in 1 over = $42 / 6$

= 7

Runs made by Anup in 7 overs = 63

Runs made by Anup in 1 over = $63 / 7$

= 9

∴ Anup scored more runs than Anish.