

NCERT Solution For Class 10 Maths Chapter 2- Polynomials

Exercise 2.2

Page: 33

1. Find the zeroes of the following quadratic polynomials and verify the relationship between the zeroes and the coefficients.

Solutions:

(i) $x^2 - 2x - 8$

$$\Rightarrow x^2 - 4x + 2x - 8 = x(x - 4) + 2(x - 4) = (x - 4)(x + 2)$$

Therefore, zeroes of polynomial equation $x^2 - 2x - 8$ are $\{4, -2\}$

$$\text{Sum of zeroes} = 4 - 2 = 2 = -\frac{(-2)}{1} = \frac{(-\text{Coefficient of } x)}{\text{Coefficient of } x^2} \quad \text{Product of zeroes} = 4 \times (-2) = -8 = \frac{(-8)}{1} = \frac{\text{Constant term}}{\text{Coefficient of } x^2}$$

(ii) $4s^2 - 4s + 1$

$$\Rightarrow 4s^2 - 2s - 2s + 1 = 2s(2s - 1) - 1(2s - 1) = (2s - 1)(2s - 1)$$

Therefore, zeroes of polynomial equation $4s^2 - 4s + 1$ are $\left\{\frac{1}{2}, \frac{1}{2}\right\}$.

$$\text{Sum of zeroes} = \frac{1}{2} + \frac{1}{2} = 1 = \frac{-4}{4} = \frac{(-\text{Coefficient of } s)}{\text{Coefficient of } s^2} \quad \text{Product of zeroes} = \frac{1}{2} \times \frac{1}{2} = \frac{1}{4} = \frac{\text{Constant term}}{\text{Coefficient of } s^2}$$

(iii) $6x^2 - 3 - 7x$

$$\Rightarrow 6x^2 - 7x - 3 = (3x + 1)(2x - 3)$$

Therefore, zeroes of polynomial equation $6x^2 - 3 - 7x$ are $\left\{-\frac{1}{3}, \frac{3}{2}\right\}$

$$\text{Sum of zeroes} = -\frac{1}{3} + \frac{3}{2} = \frac{7}{6} = \frac{-(-7)}{6} = \frac{(-\text{Coefficient of } x)}{\text{Coefficient of } x^2} \quad \text{Product of zeroes} = -\frac{1}{3} \times \frac{3}{2} = -\frac{3}{6} = \frac{\text{Constant term}}{\text{Coefficient of } x^2}$$

(iv) $4u^2 + 8u$

NCERT Solution For Class 10 Maths Chapter 2- Polynomials

$\Rightarrow 4u(u + 2)$ Therefore zeroes of polynomial equation $4u^2 + 8u$ are $\{0, -2\}$.

$$\text{Sum of zeroes} = 0 + (-2) = -2 = \frac{(-8)}{4} = \frac{(-\text{Coefficient of } u)}{\text{Coefficient of } u^2} \quad \text{Product of zeroes} = 0 \times -2 = 0 = \frac{0}{4} = \frac{\text{Constant term}}{\text{Coefficient of } u^2}$$

(v) $t^2 - 15$

$$\Rightarrow t^2 = 15 \text{ or } t = \pm\sqrt{15}$$

Therefore zeroes of polynomial equation $t^2 - 15$ are $\{\sqrt{15}, -\sqrt{15}\}$.

$$\begin{aligned} \text{Sum of zeroes} &= \sqrt{15} + (-\sqrt{15}) = 0 = \frac{-0}{1} = \frac{(-\text{Coefficient of } t)}{\text{Coefficient of } t^2} \quad \text{Product of zeroes} \\ &= \sqrt{15} \times (-\sqrt{15}) = -15 = \frac{-15}{1} = \frac{\text{Constant term}}{\text{Coefficient of } t^2} \end{aligned}$$

(vi) $3x^2 - x - 4$

$$\Rightarrow 3x^2 - 4x + 3x - 4 = x(3x - 4) + 1(3x - 4) = (3x - 4)(x + 1)$$

Therefore zeroes of polynomial equation $3x^2 - x - 4$ are $\{\frac{4}{3}, -1\}$

$$\text{Sum of zeroes} = \frac{4}{3} + (-1) = \frac{1}{3} = \frac{-(-1)}{3} = \frac{(-\text{Coefficient of } x)}{\text{Coefficient of } x^2} \quad \text{Product of zeroes} = \frac{4}{3} \times (-1) = \frac{-4}{3} = \frac{\text{Constant term}}{\text{Coefficient of } x^2}$$

2. Find a quadratic polynomial each with the given numbers as the sum and product of its zeroes respectively.

(i) $\frac{1}{4}, -1$

Solution:

From the formulas of sum and product of zeroes, we know,

$$\text{Sum of zeroes} = \alpha + \beta$$

$$\text{Product of zeroes} = \alpha \beta$$

$$\text{Sum of zeroes} = \alpha + \beta = \frac{1}{4}$$

$$\text{Product of zeroes} = \alpha \beta = -1$$

NCERT Solution For Class 10 Maths Chapter 2- Polynomials

∴ If α and β are zeroes of any quadratic polynomial, then the quadratic polynomial equation can be written directly as:-

$$x^2 - (\alpha + \beta)x + \alpha\beta = 0$$

$$x^2 - (1/4)x + (-1) = 0$$

$$4x^2 - x - 4 = 0$$

Thus, $4x^2 - x - 4$ is the quadratic polynomial.

(ii) $\sqrt{2}, \frac{1}{3}$

Solution:

$$\text{Sum of zeroes} = \alpha + \beta = \sqrt{2}$$

$$\text{Product of zeroes} = \alpha\beta = \frac{1}{3}$$

∴ If α and β are zeroes of any quadratic polynomial, then the quadratic polynomial equation can be written directly as:-

$$x^2 - (\alpha + \beta)x + \alpha\beta = 0$$

$$x^2 - (\sqrt{2})x + \frac{1}{3} = 0$$

$$3x^2 - 3\sqrt{2}x + 1 = 0$$

Thus, $3x^2 - 3\sqrt{2}x + 1$ is the quadratic polynomial.

(iii) $0, \sqrt{5}$

Solution:

Given,

$$\text{Sum of zeroes} = \alpha + \beta = 0$$

$$\text{Product of zeroes} = \alpha\beta = \sqrt{5}$$

∴ If α and β are zeroes of any quadratic polynomial, then the quadratic polynomial equation can be written directly as:-

NCERT Solution For Class 10 Maths Chapter 2- Polynomials

$$x^2 - (\alpha + \beta)x + \alpha\beta = 0$$

2

$$x - (0)x + \sqrt{5} = 0$$

Thus, $x^2 + \sqrt{5}$ is the quadratic polynomial.

(iv) 1, 1

Solution:

Given,

$$\text{Sum of zeroes} = \alpha + \beta = 1$$

$$\text{Product of zeroes} = \alpha\beta = 1$$

∴ If α and β are zeroes of any quadratic polynomial, then the quadratic polynomial equation can be written directly as:-

$$x^2 - (\alpha + \beta)x + \alpha\beta = 0$$

$$x^2 - x + 1 = 0$$

Thus, $x^2 - x + 1$ is the quadratic polynomial.

(v) $-\frac{1}{4}, \frac{1}{4}$

Solution:

Given, Sum of zeroes = $\alpha +$

$$\beta = -\frac{1}{4}$$

$$\text{Product of zeroes} = \alpha\beta = \frac{1}{4}$$

∴ If α and β are zeroes of any quadratic polynomial, then the quadratic polynomial equation can be written directly as:-

$$x^2 - (\alpha + \beta)x + \alpha\beta = 0$$

$$x^2 - \left(-\frac{1}{4}\right)x + \frac{1}{4} = 0$$

NCERT Solution For Class 10 Maths Chapter 2- Polynomials

$$4x^2 + x + 1 = 0$$

Thus, $4x^2 + x + 1$ is the quadratic polynomial.

(vi) 4, 1

Solution:

Given,

$$\text{Sum of zeroes} = \alpha + \beta = 4$$

$$\text{Product of zeroes} = \alpha \beta = 1$$

\therefore If α and β are zeroes of any quadratic polynomial, then the quadratic polynomial equation can be written directly as:-

$$x^2 - (\alpha + \beta)x + \alpha\beta = 0$$

$$x^2 - 4x + 1 = 0$$

Thus, $x^2 - 4x + 1$ is the quadratic polynomial.

NCERT Solution For Class 10 Maths Chapter 2- Polynomials

edugrooss.com