

NCERT Solutions For Class 10 Maths Chapter 4 Quadratic Equations

Exercise 4.4

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1. Find the nature of the roots of the following quadratic equations. If the real roots exist, find them;

(i) $2x^2 - 3x + 5 = 0$

(ii) $3x^2 - 4\sqrt{3}x + 4 = 0$

(iii) $2x^2 - 6x + 3 = 0$

Solutions:

(i) Given,

$2x^2 - 3x + 5 = 0$

Comparing the equation with $ax^2 + bx + c = 0$, we get $a = 2$, $b = -3$ and $c = 5$

We know, Discriminant $= b^2 - 4ac$

$= (-3)^2 - 4(2)(5) = 9 - 40$

$= -31$

As you can see, $b^2 - 4ac < 0$

Therefore, no real root is possible for the given equation, $2x^2 - 3x + 5 = 0$.

(ii) $3x^2 - 4\sqrt{3}x + 4 = 0$

Comparing the equation with $ax^2 + bx + c = 0$, we get

$a = 3$, $b = -4\sqrt{3}$ and $c = 4$ We know, Discriminant $=$

$b^2 - 4ac$

$= (-4\sqrt{3})^2 - 4(3)(4)$

$= 48 - 48 = 0$

As $b^2 - 4ac = 0$,

Real roots exist for the given equation and they are equal to each other. Hence the roots will be $-b/2a$ and $-b/2a$.

$-b/2a = -(-4\sqrt{3})/2 \times 3 = 4\sqrt{3}/6 = 2\sqrt{3}/3 = 2/\sqrt{3}$ Therefore, the roots are $2/\sqrt{3}$ and $2/\sqrt{3}$.

(iii) $2x^2 - 6x + 3 = 0$

Comparing the equation with $ax^2 + bx + c = 0$, we get a

$= 2$, $b = -6$, $c = 3$

As we know, Discriminant $= b^2 - 4ac$

$= (-6)^2 - 4(2)(3)$

$= 36 - 24 = 12$

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As $b^2 - 4ac > 0$,

Therefore, there are distinct real roots exist for this equation, $2x^2 - 6x + 3 = 0$.

$$\begin{aligned} x &= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \\ &= \frac{-(-6) \pm \sqrt{-6^2 - 4(2)(3)}}{2(2)} \\ &= \frac{6 \pm 2\sqrt{3}}{4} \\ &= \frac{3 \pm \sqrt{3}}{2} \end{aligned}$$

Therefore the roots for the given equation are $\frac{3+\sqrt{3}}{2}$ and $\frac{3-\sqrt{3}}{2}$.

2. Find the values of k for each of the following quadratic equations, so that they have two equal roots.

(i) $2x^2 + kx + 3 = 0$

(ii) $kx(x - 2) + 6 = 0$

Solutions:

(i) $2x^2 + kx + 3 = 0$

Comparing the given equation with $ax^2 + bx + c = 0$, we get, $a = 2$, $b = k$ and $c = 3$

As we know, Discriminant = $b^2 - 4ac$

$$= (k)^2 - 4(2)(3)$$

$$= k^2 - 24$$

For equal roots, we know,

$$\text{Discriminant} = 0 \quad k^2 - 24 = 0$$

$$k^2 = 24 \quad k = \pm\sqrt{24} =$$

$$\pm 2\sqrt{6}$$

(ii) $kx(x - 2) + 6 = 0$ or $kx^2 - 2kx + 6 = 0$

Comparing the given equation with $ax^2 + bx + c = 0$, we get $a = k$, $b = -2k$ and $c = 6$

We know, Discriminant = $b^2 - 4ac$

$$= (-2k)^2 - 4(k)(6)$$

$$= 4k^2 - 24k$$

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For equal roots, we know,

$$b^2 - 4ac = 0 \quad 4k^2 - 24k = 0$$

$$4k(k - 6) = 0$$

Either $4k = 0$ or $k = 6 = 0$

$$k = 0 \text{ or } k = 6$$

However, if $k = 0$, then the equation will not have the terms ' x^2 ' and ' x '.

Therefore, if this equation has two equal roots, k should be 6 only.

3. Is it possible to design a rectangular mango grove whose length is twice its breadth, and the area is 800 m^2 ? If so, find its length and breadth.

Solutions: Let the breadth of mango grove be l . Length of mango grove will be $2l$.

$$\text{Area of mango grove} = (2l)(l) = 2l^2$$

$$2l^2 = 800 \quad l^2 =$$

$$800/2 = 400 \quad l^2 =$$

$$400 = 0$$

Comparing the given equation with $ax^2 + bx + c = 0$, we get $a = 1$, $b = 0$, $c = 400$

As we know, Discriminant $= b^2 - 4ac$

$$\Rightarrow (0)^2 - 4 \times (1) \times (-400) = 1600$$

Here, $b^2 - 4ac > 0$

Thus, the equation will have real roots. And hence, the desired rectangular mango grove can be designed. $l = \pm 20$

As we know, the value of length cannot be negative.

Therefore, breadth of mango grove = 20 m

Length of mango grove = $2 \times 20 = 40$ m

4. Is the following situation possible? If so, determine their present ages. The sum of the ages of two friends is 20 years. Four years ago, the product of their ages in years was 48.

Solution: Let's say, the age of one friend be x years.

Then, the age of the other friend will be $(20 - x)$ years.

Four years ago,

Age of First friend = $(x - 4)$ years

Age of Second friend = $(20 - x - 4) = (16 - x)$ years

As per the given question, we can write,

$$(x - 4)(16 - x) = 48$$

$$16x - x^2 - 64 + 4x = 48$$

$$-x^2 + 20x - 112 = 0$$

$$x^2 - 20x + 112 = 0$$

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Comparing the equation with $ax^2 + bx + c = 0$, we get $a = 1$, $b = -20$ and $c = 112$

$$\text{Discriminant} = b^2 - 4ac$$

$$\Rightarrow (-20)^2 - 4 \times 112$$

$$\Rightarrow 400 - 448 = -48$$

$$b^2 - 4ac < 0$$

Therefore, there will be no real solution possible for the equations. Hence, condition doesn't exist.

5. Is it possible to design a rectangular park of perimeter 80 and area 400 m²? If so find its length and breadth.

Solution: Let the length and breadth of the park be l and b .

$$\text{Perimeter of the rectangular park} = 2(l + b) = 80$$

$$\text{So, } l + b = 40$$

$$\text{Or, } b = 40 - l$$

$$\text{Area of the rectangular park} = l \times b = l(40 - l) = 40l - l^2$$

$$40l - l^2 = 400 \Rightarrow l^2 - 40l + 400 = 0, \text{ which is a quadratic equation.}$$

Comparing the equation with $ax^2 + bx + c = 0$, we get $a = 1$, $b = -40$, $c = 400$

$$\text{Since, Discriminant} = b^2 - 4ac$$

$$\Rightarrow (-40)^2 - 4 \times 400$$

$$\Rightarrow 1600 - 1600 = 0$$

$$\text{Thus, } b^2 - 4ac = 0$$

Therefore, this equation has equal real roots. Hence, the situation is possible.

Root of the equation, l

$$= -b/2a$$

$$l = (40)/2(1) = 40/2 = 20$$

Therefore, length of rectangular park, $l = 20$ m And

breadth of the park, $b = 40 - l = 40 - 20 = 20$ m.