

Exercise 5.2

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1. Fill in the blanks in the following table, given that  $a$  is the first term,  $d$  the common difference and  $a_n$  the  $n^{\text{th}}$  term of the A.P.

	$a$	$d$	$n$	$a_n$
(i)	7	3	8	.....
(ii)	-18	.....	10	0
(iii)	.....	-3	18	-5
(iv)	-18.9	2.5	.....	3.6
(v)	3.5	0	105	.....

**Solutions:**

(i) Given,

First term,  $a = 7$ Common difference,  $d = 3$ Number of terms,  $n = 8$ ,We have to find the  $n^{\text{th}}$  term,  $a_n = ?$ 

As we know, for an A.P.,

$$a_n = a + (n - 1) d$$

Putting the values,

$$\Rightarrow 7 + (8 - 1) 3$$

$$\Rightarrow 7 + (7) 3$$

$$\Rightarrow 7 + 21 = 28$$

Hence,  $a_n = 28$ 

(ii) Given,

First term,  $a = -18$ Common difference,  $d = ?$ Number of terms,  $n = 10$ Nth term,  $a_n = 0$ 

As we know, for an A.P.,

$$a_n = a + (n - 1) d \text{ Putting}$$

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the values,  $0 = -18 +$   
 $(10 - 1) d$   
 $18 = 9d$   
 $d = 18/9 = 2$  Hence, common  
difference,  $d = 2$

(iii) Given, First  
term,  $a = ?$   
Common difference,  $d = -3$   
Number of terms,  $n = 18$   
Nth term,  $a_n = -5$

As we know, for an A.P.,  
 $a_n = a + (n - 1) d$

Putting the values,  
 $-5 = a + (18 - 1) (-3)$   
 $-5 = a + (17) (-3) -5$   
 $= a - 51$   $a = 51 - 5 =$   
 $46$

Hence,  $a = 46$

(iv) Given,  
First term,  $a = -18.9$   
Common difference,  $d = 2.5$  Number  
of terms,  $n = ?$   
Nth term,  $a_n = 3.6$

As we know, for an A.P.,  
 $a_n = a + (n - 1) d$

Putting the values,  $3.6 =$   
 $-18.9 + (n - 1) 2.5$   
 $3.6 + 18.9 = (n - 1) 2.5$   
 $22.5 = (n - 1) 2.5$   
 $(n - 1) = 22.5/2.5$   $n$   
 $- 1 = 9$   
 $n = 10$

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Hence,  $n = 10$

(v) Given,

First term,  $a = 3.5$

Common difference,  $d = 0$

Number of terms,  $n = 105$  Nth

term,  $a_n = ?$

As we know, for an A.P.,

$$a_n = a + (n - 1) d$$

Putting the values,  $a_n$

$$= 3.5 + (105 - 1) 0 a_n$$

$$= 3.5 + 104 \times 0$$

$$a_n = 3.5$$

Hence,  $a_n = 3.5$

**2. Choose the correct choice in the following and justify:**

(i) 30<sup>th</sup> term of the A.P: 10, 7, 4, ..., is  
(A) 97 (B) 77 (C) -77 (D) -87

(ii) 11<sup>th</sup> term of the A.P. -3, -1/2, ,2 .... is  
(A) 28 (B) 22 (C) -38 (D)  $-48\frac{1}{2}$

**Solutions:**

(i) Given here,

A.P. = 10, 7, 4, ...

Therefore, we can find,

First term,  $a = 10$

Common difference,  $d = a_2 - a_1 = 7 - 10 = -3$

As we know, for an A.P.,

$$a_n = a + (n - 1) d$$

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$$\begin{aligned} &\text{Putting the values; } a_{30} \\ &= 10 + (30 - 1)(-3) \\ &= 10 + (29)(-3) \\ &10 - 87 = -77 \end{aligned}$$

Hence, the correct answer is option C.

$$\begin{aligned} \text{(ii) Given here, A.P.} &= -3, -1/2, 2 \dots \\ \text{Therefore, we can find,} & \\ \text{First term } a &= -3 \\ \text{Common difference, } d &= a_2 - a_1 = (-1/2) - (-3) \\ \Rightarrow (-1/2) + 3 &= 5/2 \end{aligned}$$

As we know, for an A.P.,  
 $a_n = a + (n - 1)d$

$$\begin{aligned} &\text{Putting the values; } a_{11} \\ &= 3 + (11 - 1)(5/2) \\ &= 3 + (10)(5/2) \\ &3 + 25 \\ &a_{11} = 22 \end{aligned}$$

Hence, the answer is option B.

**3. In the following APs find the missing term in the boxes.**

$$\text{(i) } 2, \square, 26$$

$$\text{(ii) } \square, 13, \square, 3$$

$$\text{(iii) } 5, \square, \square, 9\frac{1}{2}$$

$$\text{(iv) } -4, \square, \square, \square, \square, 6$$

$$\text{(v) } \square, 38, \square, \square, \square, -22$$

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**Solutions:**

(i) For the given A.P., 2,  $\square$ , 26

The first and third term are;

$$a = 2 \quad a_3 = 26$$

As we know, for an A.P.,

$$a_n = a + (n - 1) d$$

Therefore, putting the values here,

$$a_3 = 2 + (3 - 1) d$$

$$26 = 2 + 2d$$

$$24 = 2d$$

$$d = 12$$

$$a_2 = 2 + (2 - 1) 12$$

$$= 14$$

Therefore, 14 is the missing term.

(ii) For the given A.P.,  $\square$ , 13,  $\square$ , 3

$$a_2 = 13 \text{ and } a_4$$

$$= 3$$

As we know, for an A.P.,

$$a_n = a + (n - 1) d$$

Therefore, putting the values here,

$$a_2 = a + (2 - 1) d$$

$$13 = a + d \dots\dots\dots \text{(i)}$$

$$a_4 = a + (4 - 1) d$$

$$3 = a + 3d \dots\dots\dots \text{(ii)}$$

On subtracting equation (i) from (ii), we get,

$$- 10 = 2d$$

$$d = - 5$$

From equation (i), putting the value of d, we get

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$$\begin{aligned}13 &= a + (-5) a = 18 a_3 = \\18 + (3 - 1)(-5) &= 18 + 2 \\(-5) &= 18 - 10 = 8\end{aligned}$$

Therefore, the missing terms are 18 and 8 respectively.

(iii) For the given A.P.,

$$\begin{aligned}a &= 5 \text{ and } a_4 \\&= 19/2\end{aligned}$$

As we know, for an A.P.,

$$a_n = a + (n - 1) d$$

Therefore, putting the values here,

$$\begin{aligned}a_4 &= a + (4 - 1) d \\19/2 &= 5 + 3d \\19/2 - 5 &= 3d \\3d &= 9/2 \\d &= 3/2\end{aligned}$$

$$\begin{aligned}a_2 &= a + (2 - 1) d \\a_2 &= 5 + 3/2 \\a_2 &= 13/2\end{aligned}$$

$$\begin{aligned}a_3 &= a + (3 - 1) d \\a_3 &= 5 + 2 \times 3/2 \\a_3 &= 8\end{aligned}$$

Therefore, the missing terms are  $13/2$  and 8 respectively.

(iv) For the given A.P.,

$$a = -4 \text{ and } a_6 = 6$$

As we know, for an A.P.,

$$a_n = a + (n - 1) d$$

Therefore, putting the values here,

$$\begin{aligned}a_6 &= a + (6 - 1) d \\6 &= -4 + 5d \\10 &= 5d \\d &= 2\end{aligned}$$

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$$\begin{aligned}
 a_2 &= a + d = -4 + 2 = -2 & a_3 \\
 &= a + 2d = -4 + 2(2) = 0 & a_4 \\
 &= a + 3d = -4 + 3(2) = 2 & a_5 \\
 &= a + 4d = -4 + 4(2) = 4
 \end{aligned}$$

Therefore, the missing terms are  $-2, 0, 2,$  and  $4$  respectively.

(v) For the given A.P.,

$$\begin{aligned}
 a_2 &= 38 & a_6 \\
 &= -22
 \end{aligned}$$

As we know, for an A.P.,

$$a_n = a + (n - 1) d$$

Therefore, putting the values here,

$$\begin{aligned}
 a_2 &= a + (2 - 1) d \\
 38 &= a + d \dots\dots\dots \text{(i)} \\
 a_6 &= a + (6 - 1) d \\
 -22 &= a + 5d \dots\dots\dots \text{(ii)}
 \end{aligned}$$

On subtracting equation (i) from (ii), we get

$$\begin{aligned}
 -22 - 38 &= 4d \\
 -60 &= 4d & d = \\
 -15 &
 \end{aligned}$$

$$\begin{aligned}
 a &= a_2 - d = 38 - (-15) = 53 & a_3 \\
 &= a + 2d = 53 + 2(-15) = 23 & a_4 \\
 &= a + 3d = 53 + 3(-15) = 8 \\
 &= a + 4d = 53 + 4(-15) = -7
 \end{aligned}$$

Therefore, the missing terms are  $53, 23, 8,$  and  $-7$  respectively.

**4. Which term of the A.P. 3, 8, 13, 18, ... is 78?**

**Solutions:**

Given the A.P. series as  $3, 8, 13, 18, \dots$

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Thus,

First term,  $a = 3$

Common difference,  $d = a_2 - a_1 = 8 - 3 = 5$

Let the  $n^{\text{th}}$  term of given A.P. be 78. Now as we know,

$$a_n = a + (n - 1) d$$

Therefore,

$$78 = 3 + (n - 1) 5$$

$$75 = (n - 1) 5$$

$$(n - 1) = 15$$

$$n = 16$$

Hence, 16<sup>th</sup> term of this A.P. is 78.

**5. Find the number of terms in each of the following A.P.**

(i) 7, 13, 19, ..., 205

(ii) 18,  $15\frac{1}{2}$ , 13, ..., -47

**Solutions:**

(i) Given, 7, 13, 19, ..., 205 is the A.P

Therefore,

First term,  $a = 7$

Common difference,  $d = a_2 - a_1 = 13 - 7 = 6$

Let there are  $n$  terms in this A.P.

$$a_n = 205$$

As we know, for an A.P.,

$$a_n = a + (n - 1) d$$

$$\text{Therefore, } 205 = 7 + (n - 1) 6$$

$$198 = (n - 1) 6$$

$$33 = (n - 1) n$$

$$= 34$$

Therefore, this given series has 34 terms in it.

(ii) Given, 18,  $15\frac{1}{2}$ , 13, ..., -47 is the A.P.



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First term,  $a = 18$

Common difference,  $d = a_2 - a_1 = 15\frac{1}{2} - 18$

$$d = \frac{31-36}{2} = -\frac{5}{2}$$

Let there are  $n$  terms in this A.P.

$$a_n = 205$$

As we know, for an A.P.,

$$a_n = a + (n - 1) d$$

$$-47 = 18 + (n - 1) (-5/2)$$

$$-47 - 18 = (n - 1) (-5/2)$$

$$-65 = (n - 1)(-5/2)$$

$$(n - 1) = -130/-5$$

$$(n - 1) = 26$$

$$n = 27$$

Therefore, this given A.P. has 27 terms in it.

### 6. Check whether -150 is a term of the A.P. 11, 8, 5, 2, ...

**Solution:**

For the given series, A.P. 11, 8, 5, 2, ...

First term,  $a = 11$

Common difference,  $d = a_2 - a_1 = 8 - 11 = -3$

Let -150 be the  $n^{\text{th}}$  term of this A.P.

As we know, for an A.P.,

$$a_n = a + (n - 1) d$$

$$-150 = 11 + (n - 1)(-3)$$

$$-150 = 11 - 3n + 3 - 164$$

$$= -3n$$

$$n = 164/3$$

Clearly,  $n$  is not an integer but a fraction.

Therefore, -150 is not a term of this A.P.

### 7. Find the 31<sup>st</sup> term of an A.P. whose 11<sup>th</sup> term is 38 and the 16<sup>th</sup> term is 73.

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**Solution:**

Given that,  $11^{\text{th}}$   
term,  $a_{11} = 38$   
and  $16^{\text{th}}$  term,  $a_{16} = 73$

We know that,  $a_n$   
 $= a + (n - 1) d$   
 $a_{11} = a + (11 - 1) d$   
 $38 = a + 10d$  ..... (i)

In the same way,  
 $a_{16} = a + (16 - 1) d$   
 $73 = a + 15d$  ..... (ii)

On subtracting equation (i) from (ii), we get  
 $35 = 5d$   
 $d = 7$

From equation (i), we can write,

$$38 = a + 10 \times (7)$$

$$38 - 70 = a$$

$$-32 = a$$

$$a = -32$$

$$a_{31} = a + (31 -$$

$$1) d$$

$$= -32 + 30(7)$$

$$= -32 + 210 =$$

$$178$$

Hence,  $31^{\text{st}}$  term is 178.

**8. An A.P. consists of 50 terms of which  $3^{\text{rd}}$  term is 12 and the last term is 106. Find the  $29^{\text{th}}$  term.**

**Solution:** Given that,  
 $3^{\text{rd}}$  term,  $a_3 = 12$   
 $50^{\text{th}}$  term,  $a_{50} = 106$

We know that,  $a_n$   
 $= a + (n - 1) d$

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$$a_3 = a + (3 - 1) d$$

$$12 = a + 2d \dots\dots\dots (i)$$

In the same way,

$$a_{50} = a + (50 - 1) d$$

$$106 = a + 49d \dots\dots\dots (ii)$$

On subtracting equation (i) from (ii), we get

$$94 = 47d$$

$$d = 2 = \text{common difference}$$

From equation (i), we can write now,

$$12 = a + 2(2) \quad a =$$

$$12 - 4 = 8 \quad a_{29} = a$$

$$+ (29 - 1) d \quad a_{29} = 8$$

$$+ (28)2$$

$$a_{29} = 8 + 56 = 64$$

Therefore, 29<sup>th</sup> term is 64.

**9. If the 3<sup>rd</sup> and the 9<sup>th</sup> terms of an A.P. are 4 and - 8 respectively. Which term of this A.P. is zero.**

**Solution:**

Given that, 3<sup>rd</sup> term,  $a_3 = 4$   
and 9<sup>th</sup> term,  $a_9 = -8$

We know that,

$a_n = a + (n - 1) d$	1
Therefore,	8
$a_3 = a + (3 - 1) d$	11
$4 = a + 2d \dots\dots\dots (i)$	11
$a_9 = a + (9 - 1) d - 8 = a + 8d$	
$\dots\dots\dots (ii)$	11

On subtracting equation (i) from (ii), we will get here,

$$-12 = 6d$$

$$d = -2$$

From equation

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(i), we can

write,

$$4 = a + 2(-2)$$

$$4 = a - 4 \quad a =$$

$$8$$

Let  $n^{\text{th}}$  term of this A.P. be zero.

$$a_n = a + (n - 1)d \quad 0 = 8 + (n -$$

$$1)(-2)$$

$$0 = 8 - 2n + 2 \quad 2n$$

$$= 10$$

$$n = 5$$

Hence, 5<sup>th</sup> term of this A.P. is 0.

**10. If 17<sup>th</sup> term of an A.P. exceeds its 10<sup>th</sup> term by 7. Find the common difference.**

**Solution:** We know that, for an A.P series;

$$a_n = a + (n - 1)d \quad a_{17}$$

$$= a + (17 - 1)d \quad a_{17}$$

$$= a + 16d$$

In the same way,

$$a_{10} = a + 9d$$

As it is given in the question,

$$a_{17} - a_{10} = 7$$

Therefore,

$$(a + 16d) - (a + 9d) = 7$$

$$7d = 7 \quad d$$

$$= 1$$

Therefore, the common difference is 1.

**11. Which term of the A.P. 3, 15, 27, 39, ... will be 132 more than its 54<sup>th</sup> term?**

**Solution:** Given A.P. is 3, 15, 27, 39, ... *first term, a = 3*

*common difference, d = a<sub>2</sub> - a<sub>1</sub> = 15 - 3 = 12*

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We know that,  $a_n =$   
 $a + (n - 1) d$   
 Therefore,  $a_{54} = a$   
 $+ (54 - 1) d \Rightarrow 3 +$   
 $(53) (12)$   
 $\Rightarrow 3 + 636 = 639$   $a_{54}$   
 $= 639$

We have to find the term of this A.P. which is 132 more than  $a_{54}$ , i.e. 771.  
 Let  $n^{\text{th}}$  term be 771.  $a_n = a + (n - 1) d$   $771 = 3 + (n - 1) 12$   
 $768 = (n - 1) 12$   
 $(n - 1) = 64$   $n$   
 $= 65$

Therefore,  $65^{\text{th}}$  term was 132 more than  $54^{\text{th}}$  term.

**Or another method is;**

Let  $n^{\text{th}}$  term be 132 more than  $54^{\text{th}}$  term.  
 $n = 54 + 132/2 = 54 + 11 = 65^{\text{th}}$  term

**12. Two APs have the same common difference. The difference between their  $100^{\text{th}}$  term is 100, what is the difference between their  $1000^{\text{th}}$  terms?**

**Solution:** Let,

The first term of two APs be  $a_1$  and  $a_2$  respectively And the common difference of these APs be  $d$ .

For the first A.P., we know,  
 $a_n = a + (n - 1) d$  Therefore,  
 $a_{100} = a_1 + (100 - 1) d$   
 $= a_1 + 99d$   
 $a_{1000} = a_1 + (1000 - 1) d$   
 $a_{1000} = a_1 + 999d$

For second A.P., we know,  
 $a_n = a + (n - 1) d$  Therefore,  
 $a_{100} = a_2 + (100 - 1) d$   
 $= a_2 + 99d$   
 $a_{1000} = a_2 + (1000 - 1) d$   
 $= a_2 + 999d$

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Given that, difference between 100<sup>th</sup> term of the two APs = 100

Therefore,  $(a_1 + 99d) - (a_2 + 99d) = 100$

$$a_1 - a_2 = 100 \dots\dots\dots \text{(i)}$$

Difference between 1000<sup>th</sup> terms of the two APs

$$(a_1 + 999d) - (a_2 + 999d) = a_1 - a_2$$

From equation (i),

This difference,  $a_1 - a_2 = 100$

Hence, the difference between 1000<sup>th</sup> terms of the two A.P. will be 100.

### 13. How many three digit numbers are divisible by 7?

**Solution:** First three-digit number that is divisible by 7 are;

First number = 105

Second number =  $105 + 7 = 112$

Third number =  $112 + 7 = 119$

Therefore, 105, 112, 119, ...

All are three digit numbers are divisible by 7 and thus, all these are terms of an A.P. having first term as 105 and common difference as 7.

As we know, the largest possible three-digit number is 999. When we divide 999 by 7, the remainder will be 5.

Therefore,  $999 - 5 = 994$  is the maximum possible three-digit number that is divisible by 7.

Now the series is as follows.

105, 112, 119, ..., 994

Let 994 be the  $n$ th term of this A.P.

first term,  $a = 105$

common difference,  $d = 7$

$a_n = 994$   $n = ?$  As we

know,  $a_n = a + (n - 1) d$

$$994 = 105 + (n - 1) 7$$

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$$889 = (n - 1) 7$$

$$(n - 1) = 127$$

$$n = 128$$

Therefore, 128 three-digit numbers are divisible by 7.

#### 14. How many multiples of 4 lie between 10 and 250?

**Solution:** The first multiple of 4 that is greater than 10 is 12.

Next multiple will be 16.

Therefore, the series formed as;

12, 16, 20, 24, ...

All these are divisible by 4 and thus, all these are terms of an A.P. with first term as 12 and common difference as 4.

When we divide 250 by 4, the remainder will be 2. Therefore,  $250 - 2 = 248$  is divisible by 4.

The series is as follows, now; 12,

16, 20, 24, ..., 248

Let 248 be the  $n^{\text{th}}$  term of this A.P.

first term,  $a = 12$  common

difference,  $d = 4$

$a_n = 248$  As

we know,

$$a_n = a + (n - 1) d$$

$$= 12 + (n - 1) \times 4$$

$$236/4 = n - 1$$

$$= n - 1$$

$$n = 60$$

Therefore, there are 60 multiples of 4 between 10 and 250.

#### 15. For what value of $n$ , are the $n^{\text{th}}$ terms of two APs 63, 65, 67, ... and 3, 10, 17, ... equal?

**Solution:** Given two APs as; 63, 65, 67, ... and 3, 10, 17, ...

Taking first AP, 63,

65, 67, ...

First term,  $a = 63$

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Common difference,  $d = a_2 - a_1 = 65 - 63 = 2$

We know,  $n^{\text{th}}$  term of this A.P. =  $a_n = a + (n - 1) d$   
 $a_n = 63 + (n - 1) 2 = 63 + 2n - 2$

$$a_n = 61 + 2n \dots\dots\dots \text{(i)}$$

**Taking second AP, 3,**

10, 17, ...

First term,  $a = 3$

Common difference,  $d = a_2 - a_1 = 10 - 3 = 7$

We know that,

$n^{\text{th}}$  term of this A.P. =  $3 + (n - 1) 7$   
 $a_n = 3 + 7n - 7$

$$a_n = 7n - 4 \dots\dots\dots \text{(ii)}$$

Given,  $n^{\text{th}}$  term of these A.P.s are equal to each other.

Equating both these equations, we get,

$$61 + 2n = 7n - 4$$

$$61 + 4 = 7n - 2n$$

$$= 65$$

$$n = 13$$

Therefore, 13<sup>th</sup> terms of both these A.P.s are equal to each other.

**16. Determine the A.P. whose third term is 16 and the 7<sup>th</sup> term exceeds the 5<sup>th</sup> term by 12.**

**Solutions:** Given,

Third term,  $a_3 = 16$  As

we know,

$$a + (3 - 1) d = 16$$

$$a + 2d = 16 \dots\dots\dots \text{(i)}$$

It is given that, 7<sup>th</sup> term exceeds the 5<sup>th</sup> term by 12.  $a_7$

$$- a_5 = 12$$

$$[a + (7 - 1) d] - [a + (5 - 1) d] = 12$$

$$(a + 6d) - (a + 4d) = 12$$

$$2d = 12$$

$$d = 6$$



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From equation (i), we get,

$$a + 2(6) = 16 \quad a + 12 = 16$$

$$a = 4$$

Therefore, A.P. will be 4, 10, 16, 22, ...

**17. Find the 20<sup>th</sup> term from the last term of the A.P. 3, 8, 13, ..., 253.**

**Solutions:** Given A.P. is 3, 8, 13, ..., 253 Common difference,  $d = 5$ .

Therefore, we can write the given AP in reverse order as;  
253, 248, 243, ..., 13, 8, 5

Now for the new AP,

$$\text{first term, } a = 253$$

$$\text{and common difference, } d = 248 - 253 = -5 \quad n = 20$$

Therefore, using  $n$ th term formula, we get,

$$a_{20} = a + (20 - 1)d \quad a_{20} = 253 + (19)(-5)$$

$$a_{20} = 253 - 95 \quad a = 158$$

Therefore, 20<sup>th</sup> term from the last term of the AP 3, 8, 13, ..., 253. is 158.

**18. The sum of 4<sup>th</sup> and 8<sup>th</sup> terms of an A.P. is 24 and the sum of the 6<sup>th</sup> and 10<sup>th</sup> terms is 44. Find the first three terms of the A.P.**

**Solutions:** We know that, the  $n$ th term of the AP is;

$$a_n = a + (n - 1)d \quad a_4 = a + (4 - 1)d$$

$$a_4 = a + 3d$$

In the same way, we can write,

$$a_8 = a + 7d \quad a_6 = a + 5d$$

$$a_{10} = a + 9d$$

Given that,  $a_4 + a_8$

$$= 24 \quad a + 3d + a + 7d$$

$$= 24$$

$$2a + 10d = 24$$

$$a + 5d = 12 \dots\dots\dots \text{(i)}$$

$$a_6 + a_{10} = 44 \quad a + 5d + a + 9d = 44$$

$$2a + 14d = 44$$

$$a + 7d = 22 \dots\dots\dots \text{(ii)}$$

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On subtracting equation (i) from (ii), we get,

$$2d = 22 - 12$$

$$= 10$$

$$d = 5$$

From equation (i), we get,

$$a + 5d = 12$$

$$+ 5(5) = 12$$

$$+ 25 = 12$$

$$-13$$

$$a_2 = a + d = -13 + 5 = -8$$

$$a_3 = a_2 + d = -8 + 5 = -3$$

Therefore, the first three terms of this A.P. are  $-13$ ,  $-8$ , and  $-3$ .

**19. Subba Rao started work in 1995 at an annual salary of Rs 5000 and received an increment of Rs 200 each year. In which year did his income reach Rs 7000?**

**Solution:** It can be seen from the given question, that the incomes of Subba Rao increases every year by Rs.200 and hence, forms an AP.

Therefore, after 1995, the salaries of each year are;

5000, 5200, 5400, ...

Here, first term,  $a = 5000$

and common difference,  $d = 200$

Let after  $n^{\text{th}}$  year, his salary be Rs 7000. Therefore,

by the  $n^{\text{th}}$  term formula of AP,

$$a_n = a + (n - 1)d \quad 7000 =$$

$$5000 + (n - 1)200$$

$$200(n - 1) = 2000$$

$$(n - 1) = 10$$

$$n = 11$$

Therefore, in 11th year, his salary will be Rs 7000.

**20. Ramkali saved Rs 5 in the first week of a year and then increased her weekly saving by Rs 1.75. If in the  $n^{\text{th}}$  week, her weekly savings become Rs 20.75, find  $n$ .**

## NCERT Solutions Class 10 Maths Chapter 5 Arithmetic Progressions

**Solution:** Given that, Ramkali saved Rs.5 in first week and then started saving each week by Rs.1.75.

Hence,

First term,  $a = 5$

and common difference,  $d = 1.75$

Also given,  $a_n$

$= 20.75$  Find,

$n = ?$

As we know, by the nth term formula,  $a_n$

$= a + (n - 1) d$

Therefore,

$$20.75 = 5 + (n - 1) \times 1.75$$

$$15.75 = (n - 1) \times 1.75$$

$$(n - 1) = 15.75/1.75 = 1575/175$$

$$= 63/7 = 9$$

$$n - 1 = 9$$

$$n = 10$$

Hence,  $n$  is 10.