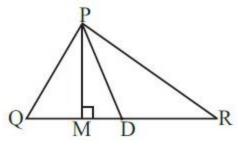


#### **EXERCISE 6.1**

PAGE: 116

1. In  $\Delta$  PQR, D is the mid-point of  $\overline{QR}$ 



(i)  $\overline{PM}$  is \_\_\_\_\_.

Solution:-

Altitude

An altitude has one end point at a vertex of the triangle and other on the line containing the opposite side.

(ii) PD is \_\_\_\_\_

Solution:-

Median

A median connects a vertex of a triangle to the mid-point of the opposite side.

(iii) Is QM = MR?

#### Solution:-

No, QM  $\neq$  MR because, D is the mid-point of QR.

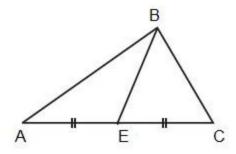
#### 2. Draw rough sketches for the following:

#### (a) In $\triangle ABC$ , BE is a median.

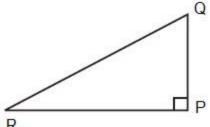
#### Solution:-

A median connects a vertex of a triangle to the mid-point of the opposite side.





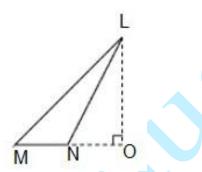
(b) In ΔPQR, PQ and PR are altitudes of the triangle. Solution:-



R

An altitude has one end point at a vertex of the triangle and other on the line containing the opposite side.

#### (c) In $\Delta XYZ$ , YL is an altitude in the exterior of the triangle. Solution:-

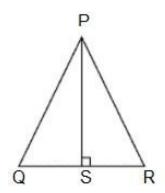


In the figure we may observe that for  $\Delta LMN$ , LO is an altitude drawn exteriorly to side LN which is extended up to point L.

3. Verify by drawing a diagram if the median and altitude of an isosceles triangle can be same.

Solution:-





Draw a Line segment  $PS \perp BC$ . It is an altitude for this triangle. Here we observe that length of QS and SR is also same. So PS is also a median of this triangle.

#### EXERCISE 6.2

### PAGE: 118

**1.** Find the value of the unknown exterior angle x in the following diagram:

(i)

70° х

#### Solution:-

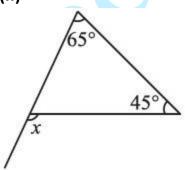
We Know That,

An exterior angle of a triangle is equal to the sum of its interior opposite angles.

 $= x = 50^{\circ} + 70^{\circ}$ 

= x = 120°

(ii)



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#### Solution:-

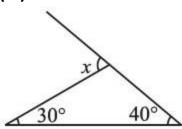
We Know That,

An exterior angle of a triangle is equal to the sum of its interior opposite angles.

 $= x = 65^{\circ} + 45^{\circ}$ 

= x = 110°

(iii)

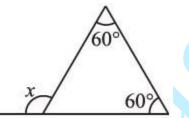


#### Solution:-

We Know That,

An exterior angle of a triangle is equal to the sum of its interior opposite angles.

(iv)



#### Solution:-

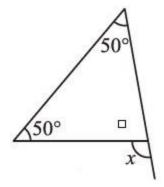
We Know That,

An exterior angle of a triangle is equal to the sum of its interior opposite angles.

$$= x = 60^{\circ} + 60^{\circ}$$
  
 $= x = 120^{\circ}$ 

(v)





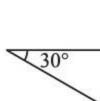
#### Solution:-

We Know That,

An exterior angle of a triangle is equal to the sum of its interior opposite angles.

 $= x = 50^{\circ} + 50^{\circ}$ = x = 100°





#### Solution:-

We Know That,

An exterior angle of a triangle is equal to the sum of its interior opposite angles.

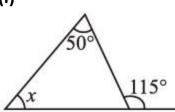
 $= x = 30^{\circ} + 60^{\circ}$  $= x = 90^{\circ}$ 

60

#### 2. Find the value of the unknown interior angle x in the following figures:



(i)



Solution:-

We Know That,

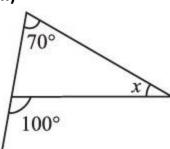
An exterior angle of a triangle is equal to the sum of its interior opposite angles. =

 $x + 50^{\circ} = 115^{\circ}$ 

By transposing  $50^{\circ}$  from LHS to RHS it becomes –  $50^{\circ}$ 

= x = 115° - 50° = x = 65°

(ii)



#### Solution:-

(iii)

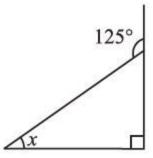
We Know That,

An exterior angle of a triangle is equal to the sum of its interior opposite angles. =

 $70^{\circ} + x = 100^{\circ}$ 

By transposing 70° from LHS to RHS it becomes – 70°

$$= x = 100^{\circ} - 70^{\circ}$$
  
= x = 30°



#### Solution:-

We Know That,

An exterior angle of a triangle is equal to the sum of its interior opposite angles.

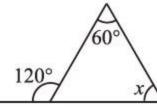
The given triangle is a right angled triangle. So the angle opposite to the x is 90°. =

 $x + 90^{\circ} = 125^{\circ}$ 

By transposing  $90^{\circ}$  from LHS to RHS it becomes –  $90^{\circ}$ 

 $= x = 125^{\circ} - 90^{\circ}$  $= x = 35^{\circ}$ 

(iv)



#### Solution:-

We Know That,

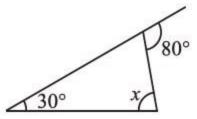
An exterior angle of a triangle is equal to the sum of its interior opposite angles.

The given triangle is a right angled triangle. So the angle opposite to the x is  $90^{\circ}$ . =  $x + 60^{\circ} = 120^{\circ}$ 

By transposing  $60^{\circ}$  from LHS to RHS it becomes –  $60^{\circ}$ 

 $= x = 120^{\circ} - 60^{\circ}$  $= x = 60^{\circ}$ 

(v)



#### Solution:-

We Know That,

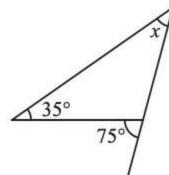
An exterior angle of a triangle is equal to the sum of its interior opposite angles. The given triangle is a right angled triangle. So the angle opposite to the x is 90°. =

$$x + 30^{\circ} = 80^{\circ}$$

By transposing  $30^{\circ}$  from LHS to RHS it becomes –  $30^{\circ}$ 

 $= x = 80^{\circ} - 30^{\circ}$ = x = 50°

(vi)



#### Solution:-

We Know That,

An exterior angle of a triangle is equal to the sum of its interior opposite angles. The given triangle is a right angled triangle. So the angle opposite to the v is  $00^\circ$ .

The given triangle is a right angled triangle. So the angle opposite to the x is  $90^{\circ}$ . =  $x + 35^{\circ} = 75^{\circ}$ 

By transposing  $35^{\circ}$  from LHS to RHS it becomes –  $35^{\circ}$ 

 $= x = 75^{\circ} - 35^{\circ}$ = x = 40°



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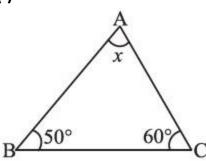
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#### **EXERCISE 6.3**

PAGE: 121

#### **1.** Find the value of the unknown x in the following diagrams:

(i)



#### Solution:-

We know that,

The sum of all the interior angles of a triangle is 180°.

#### Then,

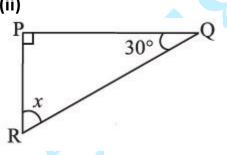
 $= \angle BAC + \angle ABC + \angle BCA = 180^{\circ}$ 

$$= x + 50^{\circ} + 60^{\circ} = 180^{\circ}$$

$$= x + 110^{\circ} = 180^{\circ}$$

By transposing 110° from LHS to RHS it becomes – 110°





#### Solution:-

We know that,

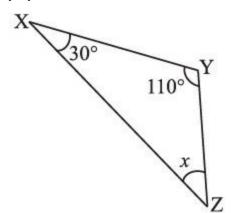
The sum of all the interior angles of a triangle is 180°.

The given triangle is a right angled triangle. So the  $\angle$ QPR is 90°. Then,

 $= \angle QPR + \angle PQR + \angle PRQ = 180^{\circ}$ 

= 
$$90^{\circ} + 30^{\circ} + x = 180^{\circ}$$
  
=  $120^{\circ} + x = 180^{\circ}$   
By transposing  $110^{\circ}$  from LHS to RHS it becomes -  $110^{\circ}$   
=  $x = 180^{\circ} - 120^{\circ}$   
=  $x = 60^{\circ}$ 

(iii)



#### Solution:-We

know that,

The sum of all the interior angles of a triangle is 180°.

Then,

 $= \angle XYZ + \angle YXZ + \angle XZY = 180^{\circ}$ 

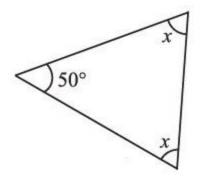
 $= 110^{\circ} + 30^{\circ} + x = 180^{\circ}$ 

$$= 140^{\circ} + x = 180^{\circ}$$

By transposing 140° from LHS to RHS it becomes – 140°

```
= x = 180^{\circ} - 140^{\circ}
= x = 40^{\circ}
```

(iv)



#### Solution:-We

know that,

The sum of all the interior angles of a triangle is 180°. Then,

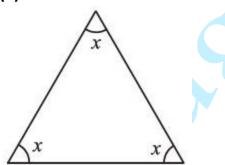
 $= 50^{\circ} + x + x = 180^{\circ}$ 

$$= 50^{\circ} + 2x = 180^{\circ}$$

By transposing 50° from LHS to RHS it becomes – 50°

$$= 2x = 180^{\circ} - 50^{\circ}$$
$$= 2x = 130^{\circ}$$
$$= x = 130^{\circ}/2$$
$$= x = 65^{\circ}$$

(v)



Solution:-We

know that,

The sum of all the interior angles of a triangle is 180°.

Then,

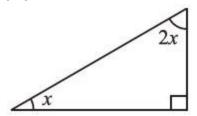
= x + x + x = 180° = 3x = 180° = x = 180°/3



= x = 60°

...The given triangle is an equiangular triangle.

(vi)



**Solution:-** We know that, The sum of all the interior angles of a triangle is 180°. Then,

 $= 90^{\circ} + 2x + x = 180^{\circ}$ 

$$= 90^{\circ} + 3x = 180^{\circ}$$

By transposing 90° from LHS to RHS it becomes – 90°

$$= 3x = 180^{\circ} - 90^{\circ}$$
  
=  $3x = 90^{\circ}$ 

$$= x = 90^{\circ}/3$$

Then,

 $= 2x = 2 \times 30^{\circ} = 60^{\circ}$ 

#### 2. Find the values of the unknowns x and y in the following diagrams:



120° 50°

#### Solution:-

#### We Know That,

An exterior angle of a triangle is equal to the sum of its interior opposite angles. Then,

 $= 50^{\circ} + x = 120^{\circ}$ 

By transposing  $50^{\circ}$  from LHS to RHS it becomes –  $50^{\circ}$ 

 $= x = 120^{\circ} - 50^{\circ}$ 

= x = 70°

We also know that,

The sum of all the interior angles of a triangle is 180°.

Then,

 $= 50^{\circ} + x + y = 180^{\circ}$ 

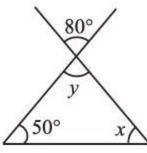
$$= 50^{\circ} + 70^{\circ} + y = 180^{\circ}$$

$$= 120^{\circ} + y = 180^{\circ}$$

By transposing  $120^{\circ}$  from LHS to RHS it becomes –  $120^{\circ}$ 

$$= y = 180^{\circ} - 120^{\circ}$$
  
 $= y = 60^{\circ}$ 

(ii)



Solution:-

From the rule of vertically opposite angles,

 $= y = 80^{\circ}$  Then,

We know that,

The sum of all the interior angles of a triangle is 180°.

Then,

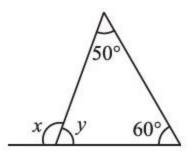
 $= 50^{\circ} + 80^{\circ} + x = 180^{\circ}$ 

$$= 130^{\circ} + x = 180^{\circ}$$

By transposing 130° from LHS to RHS it becomes – 130°

 $= x = 180^{\circ} - 130^{\circ}$ = x = 50°

(iii)



Solution:- We know that, The sum of all the interior angles of a triangle is 180°. Then,

```
= 50^{\circ} + 60^{\circ} + y = 180^{\circ}
```

$$= 110^{\circ} + y = 180^{\circ}$$

By transposing 110° from LHS to RHS it becomes – 110°

$$= y = 180^{\circ} - 110^{\circ}$$
  
= y = 70°

Now,

From the rule of linear pair,

```
= x + y = 180°
```

$$= x + 70^{\circ} = 180^{\circ}$$

By transposing 70° from LHS to RHS it becomes – 70°

```
= x = 180° - 70
= x = 110°
```

(iv)

#### Solution:-

From the rule of vertically opposite angles,

= x = 60° Then,

We know that,

The sum of all the interior angles of a triangle is 180°.

#### Then,

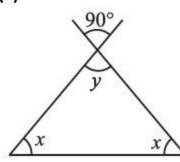
$$= 30^{\circ} + x + y = 180^{\circ}$$

$$= 30^{\circ} + 60^{\circ} + x = 180^{\circ}$$

$$= 90^{\circ} + x = 180^{\circ}$$

By transposing  $90^{\circ}$  from LHS to RHS it becomes –  $90^{\circ}$ 

$$= x = 180^{\circ} - 90^{\circ}$$
  
 $= x = 90^{\circ}$ 



#### Solution:-

From the rule of vertically opposite angles,

= y = 90° Then,

We know that,

The sum of all the interior angles of a triangle is 180°. Then,

 $= x + x + y = 180^{\circ}$ 

 $= 2x + 90^{\circ} = 180^{\circ}$ 

By transposing 90° from LHS to RHS it becomes – 90°

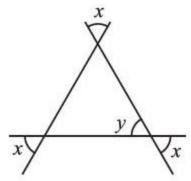
=  $2x = 180^{\circ} - 90^{\circ}$ =  $2x = 90^{\circ}$ =  $x = 90^{\circ}/2$ =  $x = 45^{\circ}$ 

(vi)



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#### Solution:-

From the rule of vertically opposite angles,

= x = y Then,

We know that,

The sum of all the interior angles of a triangle is 180°. Then,

= 
$$x + x + x = 180^{\circ}$$
  
=  $3x = 180^{\circ}$   
=  $x = 180^{\circ}/3$   
=  $x = 60^{\circ}$ 

#### **EXERCISE 6.4**

PAGE: 126

```
    Is it possible to have a triangle with the following sides?
    (i) 2 cm, 3 cm, 5 cm
```

**Solution:-** Clearly, we have: (2 + 3) = 5 5

, = 5

Thus, the sum of any two of these numbers is not greater than the third. Hence, it is not possible to draw a triangle whose sides are 2 cm, 3 cm and 5 cm.

(ii) 3 cm, 6 cm, 7 cm Solution:- Clearly, we have: (3 + 6) = 9 > 7 (6 + 7) = 13 > 3 (7 + 3) = 10 > 6

Thus, the sum of any two of these numbers is greater than the third. Hence, it is possible to draw a triangle whose sides are 3 cm, 6 cm and 7 cm.

(iii) 6 cm, 3 cm, 2 cm Solution:- Clearly, we have: (3 + 2) = 5 < 6

Thus, the sum of any two of these numbers is less than the third. Hence, it is not possible to draw a triangle whose sides are 6 cm, 3 cm and 2 cm.

2. Take any point O in the interior of a triangle PQR. Is (i)

```
OP + OQ > PQ?
(ii) OQ + OR > QR? (iii)

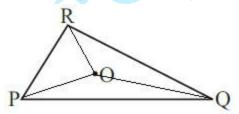
OR + OP > RP?

R

0
```

Solution:-

If we take any point O in the interior of a triangle PQR and join OR, OP, OQ. Then, we get three triangles  $\triangle OPQ$ ,  $\triangle OQR$  and  $\triangle ORP$  is shown in the figure below.



We know that, The sum of the length of any two sides is always greater than the third side.

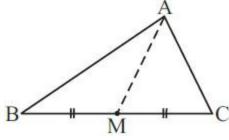
(i) Yes,  $\triangle OPQ$  has sides OP, OQ and PQ. So, OP + OQ > PQ

(ii) Yes,  $\triangle OQR$  has sides OR, OQ and QR. So, OQ + OR > QR

(iii) Yes,  $\triangle$ ORP has sides OR, OP and PR. So, OR + OP > RP

#### 3. AM is a median of a triangle ABC. Is AB + BC + CA > 2 AM?

(Consider the sides of triangles  $\triangle ABM$  and  $\triangle AMC$ .)



#### Solution:-

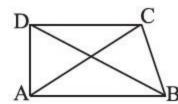
We know that,

The sum of the length of any two sides is always greater than the third side. Now consider the  $\Delta ABM$ ,

Here, AB + BM > AM ... [equation i] Then, consider the  $\Delta ACM$ Here, AC + CM > AM ... [equation ii] By adding equation [i] and [ii] we get, AB + BM + AC + CM > AM + AMFrom the figure we have, BC = BM + CM AB + BC + AC > 2 AMHence, the given expression is true.

#### 4. ABCD is a quadrilateral. Is AB + BC + CD + DA > AC + BD?

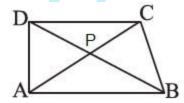




Solution:-We know that, The sum of the length of any two sides is always greater than the third side. Now consider the  $\triangle ABC$ , ... [equation i] Here, AB + BC > CA Then, consider the  $\triangle BCD$ Here, BC + CD > DB ... [equation ii] Consider the  $\Delta$ CDA ... [equation iii] Here, CD + DA > ACConsider the ΔDAB ... [equation iv] Here, DA + AB > DBBy adding equation [i], [ii], [iii] and [iv] we get, AB + BC + BC + CD + CD + DA + DA + AB > CA + DB + AC + DB2AB + 2BC + 2CD + 2DA > 2CA + 2DBTake out 2 on both the side, 2(AB + BC + CA + DA) > 2(CA + DB)AB + BC + CA + DA > CA + DBHence, the given expression is true.

#### 5. ABCD is quadrilateral. Is AB + BC + CD + DA < 2 (AC + BD) Solution:-

Let us consider ABCD is quadrilateral and P is the point where the diagonals are intersect. As shown in the figure below.



We know that,

The sum of the length of any two sides is always greater than the third side. Now consider the  $\Delta$ PAB,

Here, PA + PB < AB... [equation i] Then, consider the  $\triangle PBC$ Here, PB + PC < BC... [equation ii] Consider the  $\triangle PCD$ ... [equation iii] Here, PC + PD < CDConsider the ΔPDA Here, PD + PA < DA... [equation iv] By adding equation [i], [ii], [iii] and [iv] we get, PA + PB + PB + PC + PC + PD + PD + PA < AB + BC + CD + DA2PA + 2PB + 2PC + 2PD < AB + BC + CD + DA2PA + 2PC + 2PB + 2PD < AB + BC + CD + DA 2(PA + PC) + 2(PB + PD) < AB + BC + CD + DAFrom the figure we have, AC = PA + PC and BD = PB + PDThen, 2AC + 2BD < AB + BC + CD + DA 2(AC)+ BD) < AB + BC + CD + DA Hence, the given expression is true.

# 6. The lengths of two sides of a triangle are 12 cm and 15 cm. Between what two measures should the length of the third side fall? Solution:-

We know that,

The sum of the length of any two sides is always greater than the third side. From the question, it is given that two sides of triangle are 12 cm and 15 cm. So, the third side length should be less than the sum of other two sides,

12 + 15 = 27 cm.

Then, it is given that the third side is cannot not be less than the difference of the two sides, 15 - 12 = 3 cm

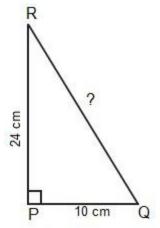
So, the length of the third side falls between 3 cm and 27 cm.

EXERCISE 6.5

PAGE: 130

# 1. PQR is a triangle, right-angled at P. If PQ = 10 cm and PR = 24 cm, find QR. Solution:-

Let us draw a rough sketch of right-angled triangle



By the rule of Pythagoras Theorem,

Pythagoras theorem states that for any right angled triangle, the area of the square on the hypotenuse is equal to the sum of the areas of square on the legs.

In the above figure RQ is the hypotenuse,

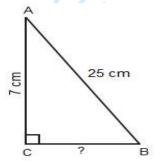
 $QR^{2} = PQ^{2} + PR^{2}$   $QR^{2} = 10^{2} + 24^{2}$   $QR^{2} = 100 + 576$   $QR^{2} = 676$   $QR = \sqrt{676}$ QR = 26 cm

Hence, the length of the hypotenuse QR = 26 cm.

## 2. ABC is a triangle, right-angled at C. If AB = 25 cm and AC = 7 cm, find BC.

#### Solution:-

Let us draw a rough sketch of right-angled triangle



By the rule of Pythagoras Theorem,

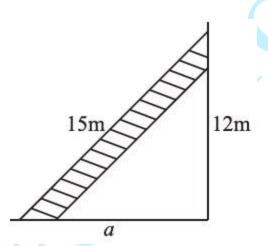
Pythagoras theorem states that for any right angled triangle, the area of the square on the hypotenuse is equal to the sum of the areas of square on the legs.

In the above figure RQ is the hypotenuse,

 $AB^{2} = AC^{2} + BC^{2}$   $25^{2} = 7^{2} + BC^{2}$   $625 = 49 + BC^{2}$ By transposing 49 from RHS to LHS it becomes - 49  $BC^{2} = 625 - 49$   $BC^{2} = 576$   $BC = \sqrt{576}$  BC = 24 cmHence, the length of the BC = 24 cm.

nes - 49

3. A 15 m long ladder reached a window 12 m high from the ground on placing it against a wall at a distance a. Find the distance of the foot of the ladder from the wall.



#### Solution:-

By the rule of Pythagoras Theorem,

Pythagoras theorem states that for any right angled triangle, the area of the square on the hypotenuse is equal to the sum of the areas of square on the legs.

In the above figure RQ is the hypotenuse,

$$15^2 = 12^2 + a^2$$

 $225 = 144 + a^{2}$ By transposing 144 from RHS to LHS it becomes - 144  $a^{2} = 225 - 144 a^{2} = 81$  $a = \sqrt{81}$ a = 9 mHence, the length of a = 9 m.

4. Which of the following can be the sides of a right triangle?

(i) 2.5 cm, 6.5 cm, 6 cm.

(ii) 2 cm, 2 cm, 5 cm.

(iii) 1.5 cm, 2cm, 2.5 cm.

#### In the case of right-angled triangles, identify the right angles.

#### Solution:-

(i) Let a = 2.5 cm, b = 6.5 cm, c = 6 cm

Let us assume the largest value is the hypotenuse side i.e. b = 6.5 cm.

Then, by Pythagoras theorem,

 $b^{2} = a^{2} + c^{2}$   $6.5^{2} = 2.5^{2} + 6^{2}$  42.25 = 6.25 + 3642.25 = 42.25

The sum of square of two side of triangle is equal to the square of third side, ... The given triangle is right-angled triangle.

Right angle lies on the opposite of the greater side 6.5 cm.

(ii) Let a = 2 cm, b = 2 cm, c = 5 cm

Let us assume the largest value is the hypotenuse side i.e. c = 5 cm. Then, by Pythagoras theorem,

$$c^{2} = a^{2} + b^{2}$$
  
 $5^{2} = 2^{2} + 2^{2}$   
 $25 = 4 + 4$  25  
≠ 8

The sum of square of two side of triangle is not equal to the square of third side, ∴ The given triangle is not right-angled triangle.



(iii) Let a = 1.5 cm, b = 2 cm, c = 2.5 cm

Let us assume the largest value is the hypotenuse side i.e. b = 2.5 cm. Then, by Pythagoras theorem,

 $b^{2} = a^{2} + c^{2}$ 2.5<sup>2</sup> = 1.5<sup>2</sup> + 2<sup>2</sup> 6.25 = 2.25 + 4 6.25 = 6.25

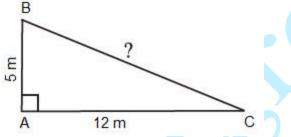
The sum of square of two side of triangle is equal to the square of third side, ... The given triangle is right-angled triangle.

Right angle lies on the opposite of the greater side 2.5 cm.

# 5. A tree is broken at a height of 5 m from the ground and its top touches the ground at a distance of 12 m from the base of the tree. Find the original height of the tree. Solution:-

Let ABC is the triangle and B is the point where tree is broken at the height 5 m from the ground.

Tree top touches the ground at a distance of AC = 12 m from the base of the tree,



By observing the figure we came to conclude that right angle triangle is formed at A. From the rule of Pythagoras theorem,

$$BC^{2} = AB^{2} + AC^{2}$$
$$BC^{2} = 5^{2} + 12^{2}$$
$$BC^{2} = 25 + 144$$
$$BC^{2} = 169$$
$$BC = \sqrt{169}$$
$$BC = 13 \text{ m}$$

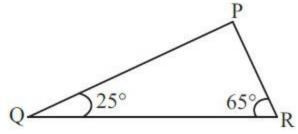
Then, the original height of the tree = AB + BC



6. Angles Q and R of a  $\Delta$ PQR are 25° and 65°.

Write which of the following is true:

- (i)  $PQ^2 + QR^2 = RP^2$
- (ii)  $PQ^2 + RP^2 = QR^2$
- (iii)  $RP2^2 + QR^2 = PQ^2$



Solution:-

Given that  $\angle B = 35^\circ$ ,  $\angle C = 55^\circ$  Then,  $\angle A = ?$ 

We know that sum of the three interior angles of triangle is equal to 180°.

- $= \angle PQR + \angle QRP + \angle RPQ = 180^{\circ}$
- $= 25^{\circ} + 65^{\circ} + \angle RPQ = 180^{\circ}$
- $= 90^{\circ} + \angle RPQ = 180^{\circ}$
- =∠RPQ = 180 90

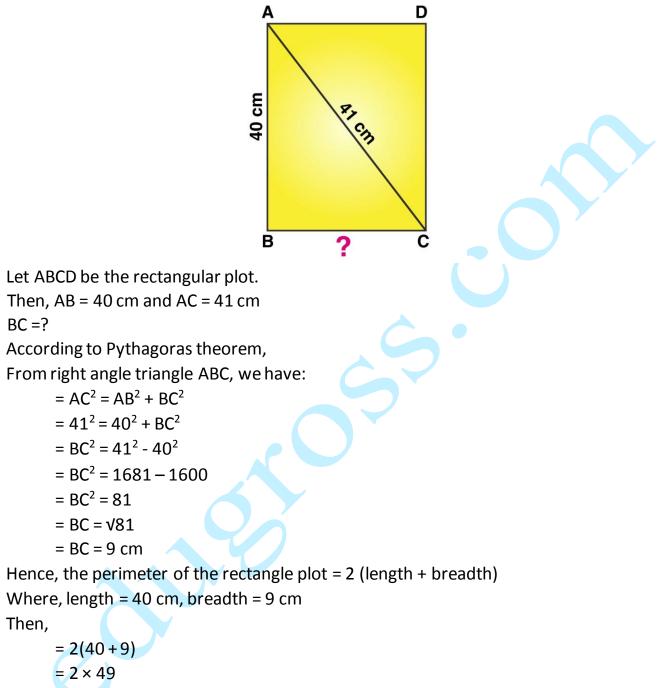
$$= \angle RPQ = 90^{\circ}$$

Also, we know that side opposite to the right angle is the hypotenuse.

 $\therefore QR^2 = PQ^2 + PR^2$ 

Hence, (ii) is true

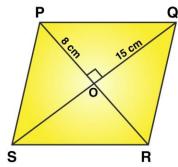
7. Find the perimeter of the rectangle whose length is 40 cm and a diagonal is 41 cm. Solution:-



= 98 cm

8. The diagonals of a rhombus measure 16 cm and 30 cm. Find its perimeter. Solution:-





Let PQRS be a rhombus, all sides of rhombus has equal length and its diagonal PR and SQ are intersecting each other at a point O. Diagonals in rhombus bisect each other at 90°.

So, PO = (PR/2) = 16/2 = 8 cm And, SO = (SQ/2) = 30/2

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= 15 cm
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Then, consider the triangle POS and apply the Pythagoras theorem,

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PS^{2} = PO^{2} + SO^{2}

PS^{2} = 8^{2} + 15^{2}

PS^{2} = 64 + 225

PS^{2} = 289

PS = \sqrt{289}

PS = 17 \text{ cm}
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Hence, the length of side of rhombus is 17 cm

Now,

Perimeter of rhombus = 4 × side of the rhombus

= 4 × 17 = 68 cm

... Perimeter of rhombus is 68 cm.