1. In $\triangle$ PQR, D is the mid-point of $\overline{Q R}$

(i) $\overline{P M}$ is $\qquad$ .
Solution:-
Altitude
An altitude has one end point at a vertex of the triangle and other on the line containing the opposite side.
(ii) PD is $\qquad$
Solution:-
Median
A median connects a vertex of a triangle to the mid-point of the opposite side.
(iii) Is QM = MR?

Solution:-
No, $Q M \neq M R$ because, $D$ is the mid-point of $Q R$.
2. Draw rough sketches for the following:
(a) In $\triangle A B C, B E$ is a median.

Solution:-
A median connects a vertex of a triangle to the mid-point of the opposite side.

(b) In $\triangle P Q R, P Q$ and PR are altitudes of the triangle. Solution:-


An altitude has one end point at a vertex of the triangle and other on the line containing the opposite side.
(c) In $\Delta X Y Z, Y L$ is an altitude in the exterior of the triangle.

Solution:-


In the figure we may observe that for $\triangle \mathrm{LMN}, \mathrm{LO}$ is an altitude drawn exteriorly to side LN which is extended up to point L .
3. Verify by drawing a diagram if the median and altitude of an isosceles triangle can be same.
Solution:-


Draw a Line segment $P S \perp B C$. It is an altitude for this triangle. Here we observe that length of QS and SR is also same. So PS is also a median of this triangle.

1. Find the value of the unknown exterior angle $x$ in the following diagram:
(i)


## Solution:-

We Know That,
An exterior angle of a triangle is equal to the sum of its interior opposite angles.

$$
\begin{aligned}
& =x=50^{\circ}+70^{\circ} \\
& =x=120^{\circ}
\end{aligned}
$$

(ii)


## Solution:-

We Know That,
An exterior angle of a triangle is equal to the sum of its interior opposite angles.

$$
\begin{aligned}
& =x=65^{\circ}+45^{\circ} \\
& =x=110^{\circ}
\end{aligned}
$$

(iii)


## Solution:-

## We Know That,

An exterior angle of a triangle is equal to the sum of its interior opposite angles.

$$
\begin{aligned}
& =x=30^{\circ}+40^{\circ} \\
& =x=70^{\circ}
\end{aligned}
$$

(iv)


## Solution:-

We Know That,
An exterior angle of a triangle is equal to the sum of its interior opposite angles.

$$
\begin{aligned}
& =x=60^{\circ}+60^{\circ} \\
& =x=120^{\circ}
\end{aligned}
$$



Solution:-
We Know That,
An exterior angle of a triangle is equal to the sum of its interior opposite angles.

$$
\begin{aligned}
& =x=50^{\circ}+50^{\circ} \\
& =x=100^{\circ}
\end{aligned}
$$

(vi)


## Solution:-

We Know That,
An exterior angle of a triangle is equal to the sum of its interior opposite angles.

$$
\begin{aligned}
& =x=30^{\circ}+60^{\circ} \\
& =x=90^{\circ}
\end{aligned}
$$

2. Find the value of the unknown interior angle $x$ in the following figures:
(i)


## Solution:-

We Know That,
An exterior angle of a triangle is equal to the sum of its interior opposite angles. =

$$
x+50^{\circ}=115^{\circ}
$$

By transposing $50^{\circ}$ from LHS to RHS it becomes $-50^{\circ}$

$$
\begin{aligned}
& =x=115^{\circ}-50^{\circ} \\
& =x=65^{\circ}
\end{aligned}
$$

(ii)


## Solution:-

## We Know That,

An exterior angle of a triangle is equal to the sum of its interior opposite angles. =

$$
70^{\circ}+x=100^{\circ}
$$

By transposing $70^{\circ}$ from LHS to RHS it becomes $-70^{\circ}$

$$
\begin{aligned}
& =x=100^{\circ}-70^{\circ} \\
& =x=30^{\circ}
\end{aligned}
$$

(iii)


## Solution:-

We Know That,
An exterior angle of a triangle is equal to the sum of its interior opposite angles.
The given triangle is a right angled triangle. So the angle opposite to the x is $90^{\circ}$. $=$

$$
x+90^{\circ}=125^{\circ}
$$

By transposing $90^{\circ}$ from LHS to RHS it becomes $-90^{\circ}$

$$
\begin{aligned}
& =x=125^{\circ}-90^{\circ} \\
& =x=35^{\circ}
\end{aligned}
$$

(iv)


## Solution:-

We Know That,
An exterior angle of a triangle is equal to the sum of its interior opposite angles. The given triangle is a right angled triangle. So the angle opposite to the x is $90^{\circ}$. $=$

$$
x+60^{\circ}=120^{\circ}
$$

By transposing $60^{\circ}$ from LHS to RHS it becomes $-60^{\circ}$

$$
\begin{aligned}
& =x=120^{\circ}-60^{\circ} \\
& =x=60^{\circ}
\end{aligned}
$$



## Solution:-

We Know That,
An exterior angle of a triangle is equal to the sum of its interior opposite angles.
The given triangle is a right angled triangle. So the angle opposite to the x is $90^{\circ}$. $=$

$$
x+30^{\circ}=80^{\circ}
$$

By transposing $30^{\circ}$ from LHS to RHS it becomes $-30^{\circ}$

$$
\begin{aligned}
& =x=80^{\circ}-30^{\circ} \\
& =x=50^{\circ}
\end{aligned}
$$

(vi)


## Solution:-

We Know That,
An exterior angle of a triangle is equal to the sum of its interior opposite angles.
The given triangle is a right angled triangle. So the angle opposite to the x is $90^{\circ}$. $=$

$$
x+35^{\circ}=75^{\circ}
$$

By transposing $35^{\circ}$ from LHS to RHS it becomes $-35^{\circ}$

$$
\begin{aligned}
& =x=75^{\circ}-35^{\circ} \\
& =x=40^{\circ}
\end{aligned}
$$

1. Find the value of the unknown $x$ in the following diagrams:
(i)


## Solution:-

We know that,
The sum of all the interior angles of a triangle is $180^{\circ}$.
Then,

$$
\begin{aligned}
& =\angle \mathrm{BAC}+\angle \mathrm{ABC}+\angle \mathrm{BCA}=180^{\circ} \\
& =x+50^{\circ}+60^{\circ}=180^{\circ} \\
& =x+110^{\circ}=180^{\circ}
\end{aligned}
$$

By transposing $110^{\circ}$ from LHS to RHS it becomes $-110^{\circ}$

$$
\begin{aligned}
& =x=180^{\circ}-110^{\circ} \\
& =x=70^{\circ}
\end{aligned}
$$

(ii)


## Solution:-

We know that,
The sum of all the interior angles of a triangle is $180^{\circ}$.
The given triangle is a right angled triangle. So the $\angle \mathrm{QPR}$ is $90^{\circ}$.
Then,

$$
=\angle \mathrm{QPR}+\angle \mathrm{PQR}+\angle \mathrm{PRQ}=180^{\circ}
$$

$$
\begin{aligned}
& =90^{\circ}+30^{\circ}+x=180^{\circ} \\
& =120^{\circ}+x=180^{\circ}
\end{aligned}
$$

By transposing $110^{\circ}$ from LHS to RHS it becomes $-110^{\circ}$

$$
\begin{aligned}
& =x=180^{\circ}-120^{\circ} \\
& =x=60^{\circ}
\end{aligned}
$$

(iii)


Solution:-We
know that,
The sum of all the interior angles of a triangle is $180^{\circ}$.
Then,

$$
\begin{aligned}
& =\angle X Y Z+\angle Y X Z+\angle X Z Y=180^{\circ} \\
& =110^{\circ}+30^{\circ}+x=180^{\circ} \\
& =140^{\circ}+x=180^{\circ}
\end{aligned}
$$

By transposing $140^{\circ}$ from LHS to RHS it becomes $-140^{\circ}$

$$
\begin{aligned}
& =x=180^{\circ}-140^{\circ} \\
& =x=40^{\circ}
\end{aligned}
$$



Solution:- We
know that,
The sum of all the interior angles of a triangle is $180^{\circ}$.
Then,

$$
\begin{aligned}
& =50^{\circ}+x+x=180^{\circ} \\
& =50^{\circ}+2 x=180^{\circ}
\end{aligned}
$$

By transposing $50^{\circ}$ from LHS to RHS it becomes $-50^{\circ}$

$$
\begin{aligned}
& =2 x=180^{\circ}-50^{\circ} \\
& =2 x=130^{\circ} \\
& =x=130^{\circ} / 2 \\
& =x=65^{\circ}
\end{aligned}
$$

(v)


Solution:-We know that,
The sum of all the interior angles of a triangle is $180^{\circ}$.
Then,

$$
\begin{aligned}
& =x+x+x=180^{\circ} \\
& =3 x=180^{\circ} \\
& =x=180^{\circ} / 3
\end{aligned}
$$

$$
=x=60^{\circ}
$$

$\therefore$ :The given triangle is an equiangular triangle.
(vi)


Solution:-We
know that,
The sum of all the interior angles of a triangle is $180^{\circ}$. Then,

$$
\begin{aligned}
& =90^{\circ}+2 x+x=180^{\circ} \\
& =90^{\circ}+3 x=180^{\circ}
\end{aligned}
$$

By transposing $90^{\circ}$ from LHS to RHS it becomes $-90^{\circ}$

$$
\begin{aligned}
& =3 x=180^{\circ}-90^{\circ} \\
& =3 x=90^{\circ} \\
& =x=90^{\circ} / 3 \\
& =x=30^{\circ}
\end{aligned}
$$

Then,

$$
=2 x=2 \times 30^{\circ}=60^{\circ}
$$

## 2. Find the values of the unknowns $x$ and $y$ in the following diagrams:

(i)


## Solution:-

We Know That,
An exterior angle of a triangle is equal to the sum of its interior opposite angles.
Then,

$$
=50^{\circ}+x=120^{\circ}
$$

By transposing $50^{\circ}$ from LHS to RHS it becomes $-50^{\circ}$

$$
\begin{aligned}
& =x=120^{\circ}-50^{\circ} \\
& =x=70^{\circ}
\end{aligned}
$$

We also know that,
The sum of all the interior angles of a triangle is $180^{\circ}$.
Then,

$$
\begin{aligned}
& =50^{\circ}+x+y=180^{\circ} \\
& =50^{\circ}+70^{\circ}+y=180^{\circ} \\
& =120^{\circ}+y=180^{\circ}
\end{aligned}
$$

By transposing $120^{\circ}$ from LHS to RHS it becomes $-120^{\circ}$

$$
\begin{aligned}
& =y=180^{\circ}-120^{\circ} \\
& =y=60^{\circ}
\end{aligned}
$$

(ii)


Solution:-
From the rule of vertically opposite angles,

$$
=y=80^{\circ} \text { Then, }
$$

We know that,
The sum of all the interior angles of a triangle is $180^{\circ}$.
Then,

$$
\begin{aligned}
& =50^{\circ}+80^{\circ}+x=180^{\circ} \\
& =130^{\circ}+x=180^{\circ}
\end{aligned}
$$

By transposing $130^{\circ}$ from LHS to RHS it becomes $-130^{\circ}$

$$
\begin{aligned}
& =x=180^{\circ}-130^{\circ} \\
& =x=50^{\circ}
\end{aligned}
$$

(iii)


## Solution:-We

know that,
The sum of all the interior angles of a triangle is $180^{\circ}$.
Then,

$$
\begin{aligned}
& =50^{\circ}+60^{\circ}+y=180^{\circ} \\
& =110^{\circ}+y=180^{\circ}
\end{aligned}
$$

By transposing $110^{\circ}$ from LHS to RHS it becomes $-110^{\circ}$

$$
\begin{aligned}
& =y=180^{\circ}-110^{\circ} \\
& =y=70^{\circ}
\end{aligned}
$$

Now,
From the rule of linear pair,

$$
\begin{aligned}
& =x+y=180^{\circ} \\
& =x+70^{\circ}=180^{\circ}
\end{aligned}
$$

By transposing $70^{\circ}$ from LHS to RHS it becomes $-70^{\circ}$

$$
\begin{aligned}
& =x=180^{\circ}-70 \\
& =x=110^{\circ}
\end{aligned}
$$

(iv)


## Solution:-

From the rule of vertically opposite angles,

$$
=x=60^{\circ} \text { Then, }
$$

We know that,
The sum of all the interior angles of a triangle is $180^{\circ}$.

Then,

$$
\begin{aligned}
& =30^{\circ}+x+y=180^{\circ} \\
& =30^{\circ}+60^{\circ}+x=180^{\circ} \\
& =90^{\circ}+x=180^{\circ}
\end{aligned}
$$

By transposing $90^{\circ}$ from LHS to RHS it becomes $-90^{\circ}$

$$
\begin{aligned}
& =x=180^{\circ}-90^{\circ} \\
& =x=90^{\circ}
\end{aligned}
$$

(v)


## Solution:-

From the rule of vertically opposite angles,

$$
=y=90^{\circ} \text { Then, }
$$

We know that,
The sum of all the interior angles of a triangle is $180^{\circ}$.
Then,

$$
=x+x+y=180^{\circ}
$$

$=2 x+90^{\circ}=180^{\circ}$
By transposing $90^{\circ}$ from LHS to RHS it becomes $-90^{\circ}$

$$
\begin{aligned}
& =2 x=180^{\circ}-90^{\circ} \\
& =2 x=90^{\circ} \\
& =x=90^{\circ} / 2 \\
& =x=45^{\circ}
\end{aligned}
$$

(vi)


## Solution:-

From the rule of vertically opposite angles,
= x = y Then,

We know that,
The sum of all the interior angles of a triangle is $180^{\circ}$.
Then,

$$
\begin{aligned}
& =x+x+x=180^{\circ} \\
& =3 x=180^{\circ} \\
& =x=180^{\circ} / 3 \\
& =x=60^{\circ}
\end{aligned}
$$

## EXERCISE 6.4

1. Is it possible to have a triangle with the following sides?
(i) $\mathbf{2 c m}, \mathbf{3 c m}, 5 \mathrm{~cm}$

Solution:- Clearly,
we have:
$(2+3)=55$
$=5$
Thus, the sum of any two of these numbers is not greater than the third.
Hence, it is not possible to draw a triangle whose sides are $2 \mathrm{~cm}, 3 \mathrm{~cm}$ and 5 cm .
(ii) $\mathbf{3 c m}, 6 \mathrm{~cm}, 7 \mathrm{~cm}$

Solution:- Clearly,
we have:
$(3+6)=9>7$
$(6+7)=13>3$
$(7+3)=10>6$
Thus, the sum of any two of these numbers is greater than the third.
Hence, it is possible to draw a triangle whose sides are $3 \mathrm{~cm}, 6 \mathrm{~cm}$ and 7 cm .
(iii) $\mathbf{6 c m}, \mathbf{3 c m}, 2 \mathrm{~cm}$

Solution:- Clearly,
we have:
$(3+2)=5<6$
Thus, the sum of any two of these numbers is less than the third.
Hence, it is not possible to draw a triangle whose sides are $6 \mathrm{~cm}, 3 \mathrm{~cm}$ and 2 cm .
2. Take any point $O$ in the interior of a triangle PQR. Is (i)
$O P+O Q>P Q$ ?
(ii) $O Q+O R>Q R$ ? (iii)
$O R+O P>R P$ ?


## Solution:-

If we take any point $O$ in the interior of a triangle $P Q R$ and join OR, OP, OQ.
Then, we get three triangles $\triangle O P Q, \triangle O Q R$ and $\triangle O R P$ is shown in the figure below.


We know that,
The sum of the length of any two sides is always greater than the third side.
(i) $Y e s, \triangle O P Q$ has sides $O P, O Q$ and $P Q$.

So, OP + OQ > PQ
(ii) $\mathrm{Yes}, \triangle O Q R$ has sides $O R, O Q$ and $Q R$.

So, $\mathrm{OQ}+\mathrm{OR}>\mathrm{QR}$
(iii) Yes, $\triangle$ ORP has sides OR, OP and PR.

So, OR + OP > RP
3. $A M$ is a median of a triangle $A B C$. Is
$A B+B C+C A>2 A M$ ?
(Consider the sides of triangles $\triangle A B M$ and $\triangle A M C$.)


## Solution:-

We know that,
The sum of the length of any two sides is always greater than the third side.
Now consider the $\triangle A B M$,

$$
\begin{equation*}
\text { Here, } \mathrm{AB}+\mathrm{BM}>\mathrm{AM} \tag{equationi}
\end{equation*}
$$

Then, consider the $\triangle A C M$
Here, AC + CM > AM
... [equation ii]
By adding equation [i] and [ii] we get,

$$
A B+B M+A C+C M>A M+A M
$$

From the figure we have, $B C=B M+C M A B$

$$
\text { + BC + AC > } 2 \text { AM }
$$

Hence, the given expression is true.
4. $A B C D$ is a quadrilateral.

Is $A B+B C+C D+D A>A C+B D$ ?


## Solution:-

We know that,
The sum of the length of any two sides is always greater than the third side.
Now consider the $\triangle A B C$,
Here, $A B+B C>C A$ Then,
... [equation i]
consider the $\triangle B C D$
Here, $B C+C D>D B$
... [equation ii]
Consider the $\triangle$ CDA
Here, $C D+D A>A C$
... [equation iii]
Consider the $\triangle \mathrm{DAB}$
Here, DA + AB > DB
... [equation iv]
By adding equation [i], [ii], [iii] and [iv] we get,

$$
\begin{aligned}
& A B+B C+B C+C D+C D+D A+D A+A B>C A+D B+A C+D B \\
& 2 A B+2 B C+2 C D+2 D A>2 C A+2 D B
\end{aligned}
$$

Take out 2 on both the side,

$$
2(A B+B C+C A+D A)>2(C A+D B)
$$

$A B+B C+C A+D A>C A+D B$
Hence, the given expression is true.

## 5. $A B C D$ is quadrilateral. Is $A B+B C+C D+D A<2(A C+B D)$

## Solution:-

Let us consider $A B C D$ is quadrilateral and $P$ is the point where the diagonals are intersect. As shown in the figure below.


We know that,

The sum of the length of any two sides is always greater than the third side.
Now consider the $\triangle P A B$,
Here, $\mathrm{PA}+\mathrm{PB}<\mathrm{AB}$
... [equation i]
Then, consider the $\triangle P B C$
Here, $P B+P C<B C$
... [equation ii]
Consider the $\triangle P C D$
Here, $\mathrm{PC}+\mathrm{PD}<\mathrm{CD}$... [equation iii]
Consider the $\triangle$ PDA

> Here, PD + PA < DA ... [equation iv]

By adding equation [i], [ii], [iii] and [iv] we get,
$P A+P B+P B+P C+P C+P D+P D+P A<A B+B C+C D+D A$
$2 P A+2 P B+2 P C+2 P D<A B+B C+C D+D A$
$2 P A+2 P C+2 P B+2 P D<A B+B C+C D+D A$
$2(P A+P C)+2(P B+P D)<A B+B C+C D+D A$
From the figure we have, $A C=P A+P C$ and $B D=P B+P D$
Then,
$2 A C+2 B D<A B+B C+C D+D A 2(A C$
$+B D)<A B+B C+C D+D A$ Hence, the given expression is true.

## 6. The lengths of two sides of a triangle are 12 cm and 15 cm . Between what two measures should the length of the third side fall?

## Solution:-

We know that,
The sum of the length of any two sides is always greater than the third side.
From the question, it is given that two sides of triangle are 12 cm and 15 cm .
So, the third side length should be less than the sum of other two sides,
$12+15=27 \mathrm{~cm}$.
Then, it is given that the third side is cannot not be less than the difference of the two sides, $15-12=3 \mathrm{~cm}$
So, the length of the third side falls between 3 cm and 27 cm .

1. $P Q R$ is a triangle, right-angled at $P$. If $P Q=10 \mathrm{~cm}$ and $P R=24 \mathrm{~cm}$, find $Q R$. Solution:-
Let us draw a rough sketch of right-angled triangle


By the rule of Pythagoras Theorem,
Pythagoras theorem states that for any right angled triangle, the area of the square on the hypotenuse is equal to the sum of the areas of square on the legs.
In the above figure $R Q$ is the hypotenuse,

$$
\begin{aligned}
& Q R^{2}=P Q^{2}+P R^{2} \\
& Q R^{2}=10^{2}+24^{2} \\
& Q R^{2}=100+576 \\
& Q R^{2}=676 \\
& Q R=V 676 \\
& Q R=26 \mathrm{~cm}
\end{aligned}
$$

Hence, the length of the hypotenuse $Q R=26 \mathrm{~cm}$.
2. $A B C$ is a triangle, right-angled at $C$. If $A B=25 \mathrm{~cm}$ and $A C=7 \mathrm{~cm}$, find $B C$. Solution:-
Let us draw a rough sketch of right-angled triangle


By the rule of Pythagoras Theorem,
Pythagoras theorem states that for any right angled triangle, the area of the square on the hypotenuse is equal to the sum of the areas of square on the legs.
In the above figure $R Q$ is the hypotenuse,

$$
\begin{aligned}
& A B^{2}=A C^{2}+B C^{2} \\
& 25^{2}=7^{2}+B C^{2} \\
& 625=49+B C^{2}
\end{aligned}
$$

By transposing 49 from RHS to LHS it becomes - 49

$$
\begin{aligned}
& \mathrm{BC}^{2}=625-49 \\
& \mathrm{BC}^{2}=576 \\
& B C=\sqrt{ } 576 \\
& B C=24 \mathrm{~cm}
\end{aligned}
$$

Hence, the length of the $B C=24 \mathrm{~cm}$.

## 3. A 15 m long ladder reached a window 12 m high from the ground on placing it

 against a wall at a distance $a$. Find the distance of the foot of the ladder from the wall.

## Solution:-

By the rule of Pythagoras Theorem, Pythagoras theorem states that for any right angled triangle, the area of the square on the hypotenuse is equal to the sum of the areas of square on the legs.
In the above figure RQ is the hypotenuse,

$$
15^{2}=12^{2}+a^{2}
$$

$$
225=144+a^{2}
$$

By transposing 144 from RHS to LHS it becomes - 144

$$
\begin{aligned}
& a^{2}=225-144 a^{2}=81 \\
& a=\sqrt{ } 81 \\
& a=9 m
\end{aligned}
$$

Hence, the length of $\mathrm{a}=9 \mathrm{~m}$.
4. Which of the following can be the sides of a right triangle?
(i) $2.5 \mathrm{~cm}, 6.5 \mathrm{~cm}, 6 \mathrm{~cm}$.
(ii) $\mathbf{2 c m}, \mathbf{2 c m}, 5 \mathrm{~cm}$.
(iii) $1.5 \mathrm{~cm}, 2 \mathrm{~cm}, 2.5 \mathrm{~cm}$.

In the case of right-angled triangles, identify the right angles.

## Solution:-

(i) Let $\mathrm{a}=2.5 \mathrm{~cm}, \mathrm{~b}=6.5 \mathrm{~cm}, \mathrm{c}=6 \mathrm{~cm}$

Let us assume the largest value is the hypotenuse side i.e. $b=6.5 \mathrm{~cm}$.
Then, by Pythagoras theorem,
$b^{2}=a^{2}+c^{2}$
$6.5^{2}=2.5^{2}+6^{2}$
$42.25=6.25+36$
$42.25=42.25$
The sum of square of two side of triangle is equal to the square of third side, $:$ : The given triangle is right-angled triangle.
Right angle lies on the opposite of the greater side 6.5 cm .
(ii) Let $\mathrm{a}=2 \mathrm{~cm}, \mathrm{~b}=2 \mathrm{~cm}, \mathrm{c}=5 \mathrm{~cm}$

Let us assume the largest value is the hypotenuse side i.e. $c=5 \mathrm{~cm}$.
Then, by Pythagoras theorem,

$$
\begin{aligned}
& c^{2}=a^{2}+b^{2} \\
& 5^{2}=2^{2}+2^{2} \\
& 25=4+425 \\
& \neq 8
\end{aligned}
$$

The sum of square of two side of triangle is not equal to the square of third side, $\therefore$ The given triangle is not right-angled triangle.
(iii) Let $\mathrm{a}=1.5 \mathrm{~cm}, \mathrm{~b}=2 \mathrm{~cm}, \mathrm{c}=2.5 \mathrm{~cm}$

Let us assume the largest value is the hypotenuse side i.e. $b=2.5 \mathrm{~cm}$.
Then, by Pythagoras theorem,

$$
b^{2}=a^{2}+c^{2}
$$

$2.5^{2}=1.5^{2}+2^{2}$
$6.25=2.25+4$
$6.25=6.25$
The sum of square of two side of triangle is equal to the square of third side, $\therefore$ The given triangle is right-angled triangle.
Right angle lies on the opposite of the greater side 2.5 cm .

## 5. A tree is broken at a height of 5 m from the ground and its top touches the ground at a distance of 12 m from the base of the tree. Find the original height of the tree.

## Solution:-

Let $A B C$ is the triangle and $B$ is the point where tree is broken at the height 5 m from the ground.
Tree top touches the ground at a distance of $A C=12 \mathrm{~m}$ from the base of the tree,


By observing the figure we came to conclude that right angle triangle is formed at A .
From the rule of Pythagoras theorem,

$$
\begin{aligned}
& \mathrm{BC}^{2}=\mathrm{AB}^{2}+\mathrm{AC}^{2} \\
& \mathrm{BC}^{2}=5^{2}+12^{2} \\
& \mathrm{BC}^{2}=25+144 \\
& \mathrm{BC}^{2}=169 \\
& \mathrm{BC}=\mathrm{V} 169 \\
& \mathrm{BC}=13 \mathrm{~m}
\end{aligned}
$$

Then, the original height of the tree $=A B+B C$

$$
\begin{aligned}
& =5+13 \\
& =18 \mathrm{~m}
\end{aligned}
$$

## 6. Angles $Q$ and $R$ of a $\triangle P Q R$ are $25^{\circ}$ and $65^{\circ}$.

Write which of the following is true:
(i) $P Q^{2}+\mathrm{QR}^{2}=\mathrm{RP}^{2}$
(ii) $P Q^{2}+R P^{2}=Q R^{2}$
(iii) $\mathbf{R P 2}^{\mathbf{2}}+\mathbf{Q R}^{\mathbf{2}}=\mathbf{P Q}^{\mathbf{2}}$


## Solution:-

Given that $\angle B=35^{\circ}, \angle C=55^{\circ}$ Then,
$\angle A=$ ?
We know that sum of the three interior angles of triangle is equal to $180^{\circ}$.

$$
\begin{aligned}
& =\angle P Q R+\angle Q R P+\angle R P Q=180^{\circ} \\
& =25^{\circ}+65^{\circ}+\angle R P Q=180^{\circ} \\
& =90^{\circ}+\angle R P Q=180^{\circ} \\
& =\angle R P Q=180-90 \\
& =\angle R P Q=90^{\circ}
\end{aligned}
$$

Also, we know that side opposite to the right angle is the hypotenuse.
$\therefore \mathrm{QR}^{2}=\mathrm{PQ}^{2}+\mathrm{PR}^{2}$
Hence, (ii) is true
7. Find the perimeter of the rectangle whose length is 40 cm and a diagonal is 41 cm . Solution:-


Let $A B C D$ be the rectangular plot.
Then, $A B=40 \mathrm{~cm}$ and $A C=41 \mathrm{~cm}$
$\mathrm{BC}=$ ?
According to Pythagoras theorem,
From right angle triangle $A B C$, we have:

$$
\begin{aligned}
& =A C^{2}=A B^{2}+B C^{2} \\
& =41^{2}=40^{2}+B C^{2} \\
& =B C^{2}=41^{2}-40^{2} \\
& =B C^{2}=1681-1600 \\
& =B C^{2}=81 \\
& =B C=V 81 \\
& =B C=9 \mathrm{~cm}
\end{aligned}
$$

Hence, the perimeter of the rectangle plot $=2$ (length + breadth)
Where, length $=40 \mathrm{~cm}$, breadth $=9 \mathrm{~cm}$
Then,

$$
\begin{aligned}
& =2(40+9) \\
& =2 \times 49 \\
& =98 \mathrm{~cm}
\end{aligned}
$$

8. The diagonals of a rhombus measure 16 cm and 30 cm . Find its perimeter. Solution:-


Let PQRS be a rhombus, all sides of rhombus has equal length and its diagonal PR and $S Q$ are intersecting each other at a point $O$. Diagonals in rhombus bisect each other at $90^{\circ}$.
So, $\mathrm{PO}=(\mathrm{PR} / 2)$

$$
\begin{aligned}
& =16 / 2 \\
& =8 \mathrm{~cm}
\end{aligned}
$$

And, $\mathrm{SO}=(\mathrm{SO} / 2)$
= 30/2

$$
=15 \mathrm{~cm}
$$

Then, consider the triangle POS and apply the Pythagoras theorem,
$\mathrm{PS}^{2}=\mathrm{PO}^{2}+\mathrm{SO}^{2}$
$\mathrm{PS}^{2}=8^{2}+15^{2}$
PS $^{2}=64+225$
$\mathrm{PS}^{2}=289$
PS $=$ V289
PS $=17 \mathrm{~cm}$
Hence, the length of side of rhombus is 17 cm
Now,
Perimeter of rhombus $=4 \times$ side of the rhombus

$$
\begin{aligned}
& =4 \times 17 \\
& =68 \mathrm{~cm}
\end{aligned}
$$

$\therefore$ Perimeter of rhombus is 68 cm .

