

## NCERT Solutions for Class 11 Maths Chapter 10 Straight Lines

### EXERCISE 10.1

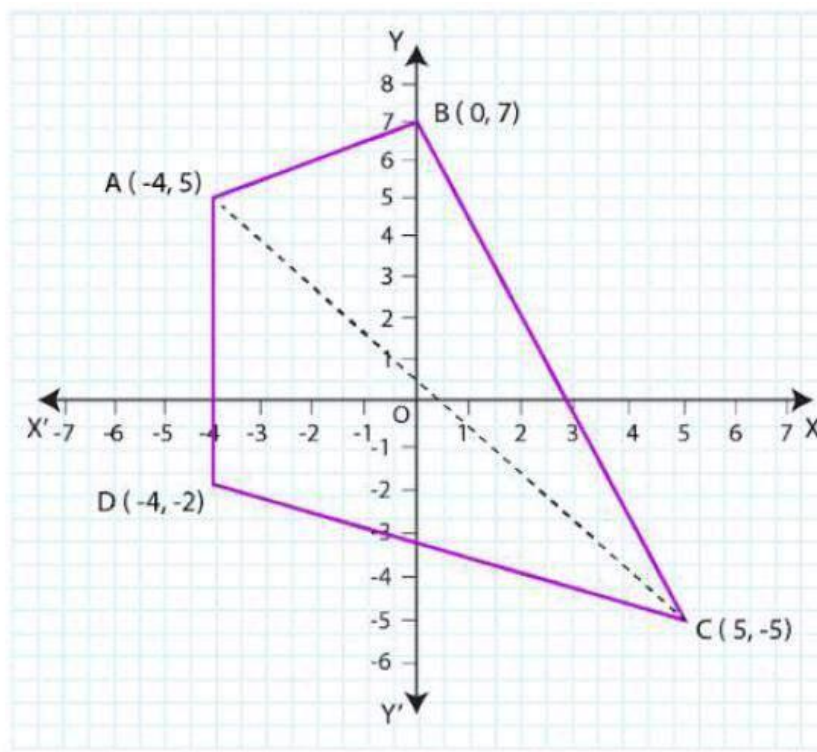
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1. Draw a quadrilateral in the Cartesian plane, whose vertices are  $(-4, 5)$ ,  $(0, 7)$ ,  $(5, -5)$  and  $(-4, -2)$ . Also, find its area.

**Solution:**

Let ABCD be the given quadrilateral with vertices A  $(-4, 5)$ , B  $(0, 7)$ , C  $(5, -5)$  and D  $(-4, -2)$ .

Now let us plot the points on the Cartesian plane by joining the points AB, BC, CD, AD which gives us the required quadrilateral.



To find the area, draw diagonal AC

So, area (ABCD) = area ( $\triangle ABC$ ) + area ( $\triangle ADC$ )

Then, area of triangle with vertices  $(x_1, y_1)$ ,  $(x_2, y_2)$  and  $(x_3, y_3)$  is

$$\begin{aligned}
 \text{Area of } \triangle ABC &= \frac{1}{2} [x_1 (y_2 - y_3) + x_2 (y_3 - y_1) + x_3 (y_1 - y_2)] \\
 &= \frac{1}{2} [-4 (7 - (-5)) + 0 (-5 - 5) + 5 (5 - 7)] \text{ unit}^2 \\
 &= \frac{1}{2} [-4 (12) + 5 (-2)] \text{ unit}^2 \\
 &= \frac{1}{2} (58) \text{ unit}^2 \\
 &= 29 \text{ unit}^2
 \end{aligned}$$

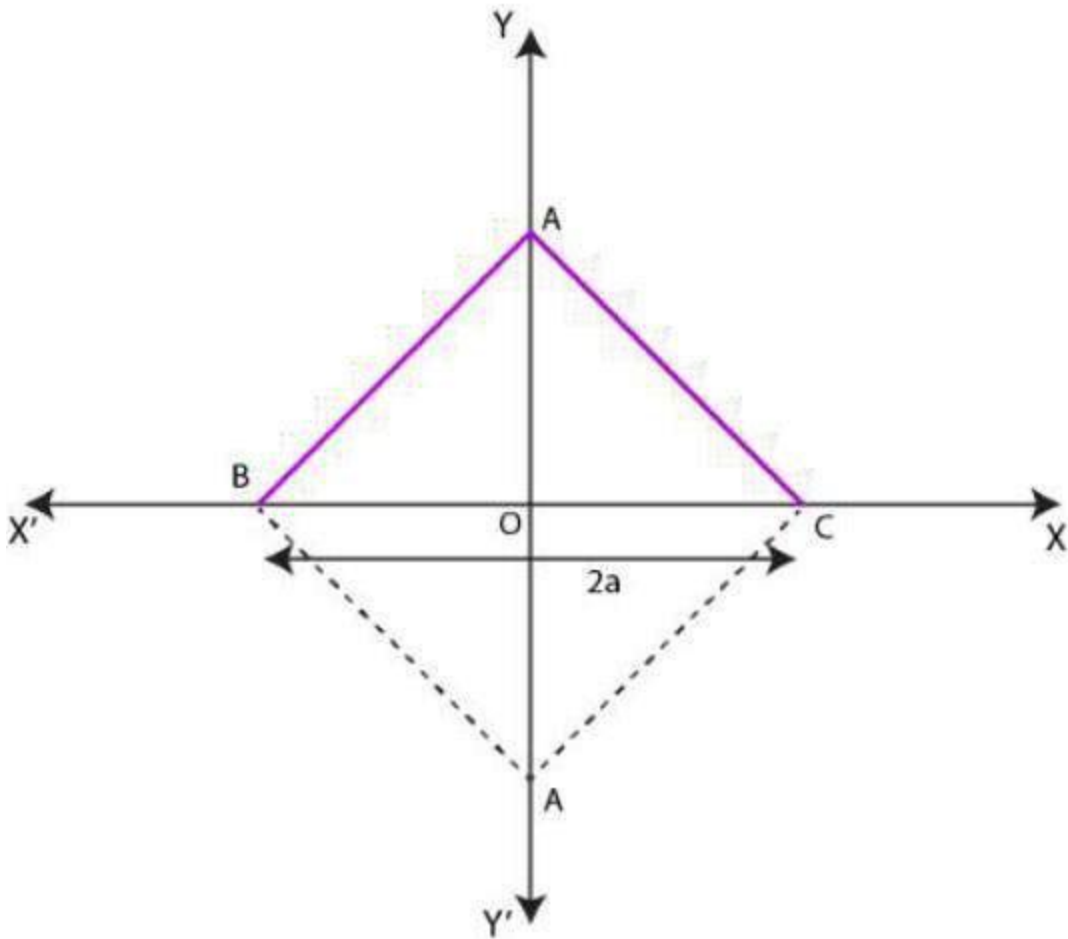
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$$\begin{aligned}
 \text{Area of } \triangle ACD &= \frac{1}{2} [x_1 (y_2 - y_3) + x_2 (y_3 - y_1) + x_3 (y_1 - y_2)] \\
 &= \frac{1}{2} [-4 (-5 + 2) + 5 (-2 - 5) + (-4) (5 - (-5))] \text{ unit}^2 \\
 &= \frac{1}{2} [-4 (-3) + 5 (-7) - 4 (10)] \text{ unit}^2 \\
 &= \frac{1}{2} (-63) \text{ unit}^2 \\
 &= -63/2 \text{ unit}^2
 \end{aligned}$$

Since area cannot be negative area  $\triangle ACD = 63/2 \text{ unit}^2$

$$\begin{aligned}
 \text{Area (ABCD)} &= 29 + 63/2 \\
 &= 121/2 \text{ unit}^2
 \end{aligned}$$

**2. The base of an equilateral triangle with side  $2a$  lies along the y-axis such that the mid-point of the base is at the origin. Find vertices of the triangle. Solution:**



Let us consider ABC be the given equilateral triangle with side  $2a$ .

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Where,  $AB = BC = AC = 2a$

In the above figure, by assuming that the base BC lies on the x axis such that the midpoint of BC is at the origin i.e.  $BO = OC = a$ , where O is the origin. The co-ordinates of point C are  $(0, a)$  and that of B are  $(0, -a)$

Since the line joining a vertex of an equilateral  $\Delta$  with the mid-point of its opposite side is perpendicular.

So, vertex A lies on the y –axis

By applying Pythagoras theorem

$$(AC)^2 = OA^2 + OC^2$$

$$(2a)^2 = a^2 + OC^2$$

$$4a^2 - a^2 = OC^2$$

$$3a^2 = OC^2$$

$$OC = \sqrt{3}a$$

Co-ordinates of point C =  $\pm \sqrt{3}a, 0$

$\therefore$  The vertices of the given equilateral triangle are  $(0, a), (0, -a), (\sqrt{3}a, 0)$  Or  $(0, a), (0, -a)$  and  $(-\sqrt{3}a, 0)$

**3. Find the distance between P  $(x_1, y_1)$  and Q  $(x_2, y_2)$  when: (i) PQ is parallel to the y-axis, (ii) PQ is parallel to the x-axis.**

**Solution:**

Given:

Points P  $(x_1, y_1)$  and Q  $(x_2, y_2)$

(i) When PQ is parallel to y axis then  $x_1 =$

$$\begin{aligned} \text{So, the distance between P and Q is given by} &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ &= \sqrt{(y_2 - y_1)^2} \end{aligned}$$

$$= |y_2 - y_1|$$

(ii) When PQ is parallel to the x-axis then  $y_1 =$

$$\begin{aligned} \text{So, the distance between P and Q is given by} &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ &= \sqrt{(x_2 - x_1)^2} \end{aligned}$$

$$=$$

$$= |x_2 - x_1|$$

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- 4. Find a point on the x-axis, which is equidistant from the points (7, 6) and (3, 4). Solution:**

Let us consider (a, 0) be the point on the x-axis that is equidistant from the point (7, 6) and (3, 4).

So,

$$\sqrt{(7-a)^2 + (6-0)^2} = \sqrt{(3-a)^2 + (4-0)^2}$$

$$\sqrt{49 + a^2 - 14a + 36} = \sqrt{9 + a^2 - 6a + 16}$$

$$\sqrt{a^2 - 14a + 85} = \sqrt{a^2 - 6a + 25}$$

Now, let us square on both the sides we get,

$$a^2 - 14a + 85 = a^2 - 6a + 25$$

$$-8a = -60$$

$$a = 60/8$$

$$= 15/2$$

∴ The required point is (15/2, 0)

- 5. Find the slope of a line, which passes through the origin, and the mid-point of the line segment joining the points P (0, -4) and B (8, 0). Solution:**

The co-ordinates of mid-point of the line segment joining the points P (0, -4) and B (8, 0) are  $(0+8)/2, (-4+0)/2 = (4, -2)$

The slope 'm' of the line non-vertical line passing through the point  $(x_1, y_1)$  and  $(x_2, y_2)$  is given by  $m = (y_2 - y_1)/(x_2 - x_1)$  where,  $x \neq x_1$

The slope of the line passing through (0, 0) and (4, -2) is  $(-2-0)/(4-0) = -1/2$  ∴

The required slope is -1/2.

- 6. Without using the Pythagoras theorem, show that the points (4, 4), (3, 5) and (-1, -1) are the vertices of a right-angled triangle. Solution:**

The vertices of the given triangle are (4, 4), (3, 5) and (-1, -1).

The slope (m) of the line non-vertical line passing through the point  $(x_1, y_1)$  and  $(x_2, y_2)$  is given by  $m = (y_2 - y_1)/(x_2 - x_1)$  where,  $x \neq x_1$  So,

the slope of the line AB  $(m_1) = (5-4)/(3-4) = 1/-1 = -1$  the

slope of the line BC  $(m_2) = (-1-5)/(-1-3) = -6/-4 = 3/2$  the

slope of the line CA  $(m_3) = (4+1)/(4+1) = 5/5 = 1$

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It is observed that,  $m_1.m_3 = -1.1 = -1$

Hence, the lines AB and CA are perpendicular to each other

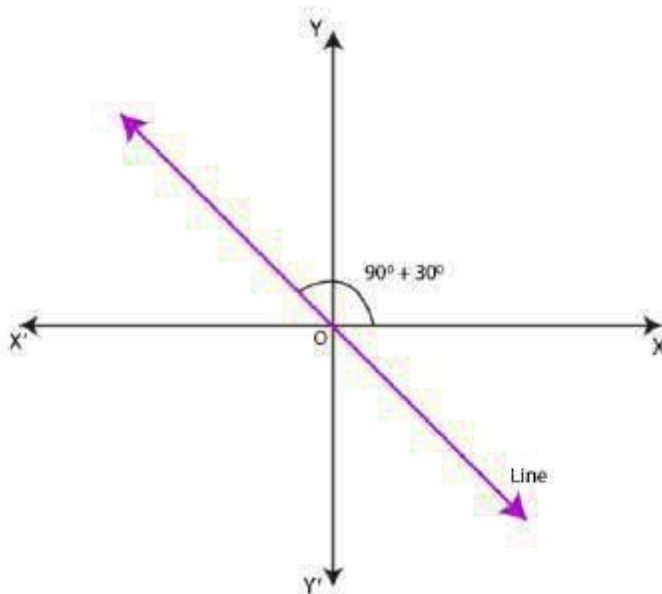
$\therefore$  given triangle is right-angled at A (4, 4)

And the vertices of the right-angled  $\Delta$  are (4, 4), (3, 5) and (-1, -1)

**7. Find the slope of the line, which makes an angle of  $30^\circ$  with the positive direction of y-axis measured anticlockwise.**

**Solution:**

We know that, if a line makes an angle of  $30^\circ$  with the positive direction of y-axis measured anti-clock-wise, then the angle made by the line with the positive direction of x- axis measure anti-clock-wise is  $90^\circ + 30^\circ = 120^\circ$



$\therefore$  The slope of the given line is  $\tan 120^\circ = \tan (180^\circ - 60^\circ)$   
 $= -\tan 60^\circ$   
 $= -\sqrt{3}$

**8. Find the value of x for which the points (x, -1), (2, 1) and (4, 5) are collinear.**

**Solution:**

If the points (x, -1), (2, 1) and (4, 5) are collinear, then Slope of AB = Slope of BC

Then,  $(1+1)/(2-x) = (5-1)/(4-2)$

$$2/(2-x) = 4/2$$

$$2/(2-x) = 2$$

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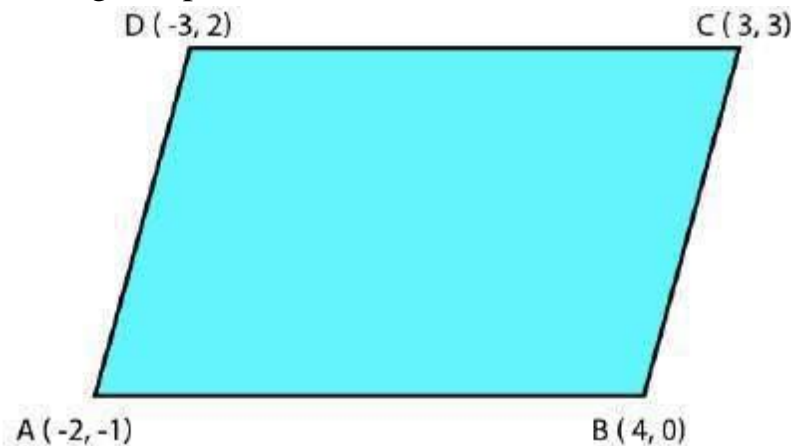
$$\begin{aligned}
 2 &= 2(2-x) \\
 2 &= 4 - 2x \\
 2x &= 4 - 2 \\
 2x &= 2 \quad \quad \quad x \\
 &= 2/2 \\
 &= 1
 \end{aligned}$$

$\therefore$  The required value of  $x$  is 1.

**9. Without using distance formula, show that points  $(-2, -1)$ ,  $(4, 0)$ ,  $(3, 3)$  and  $(-3, 2)$  are the vertices of a parallelogram.**

**Solution:**

Let the given point be  $A(-2, -1)$ ,  $B(4, 0)$ ,  $C(3, 3)$  and  $D(-3, 2)$



So now, The slope of  $AB = (0+1)/(4+2) = 1/6$

The slope of  $CD = (3-2)/(3+3) = 1/6$

Hence, slope of  $AB$  = Slope of  $CD$

$\therefore AB \parallel CD$

Now,

The slope of  $BC = (3-0)/(3-4) = 3/-1 = -3$

The slope of  $CD = (2+1)/(-3+2) = 3/-1 = -3$

Hence, slope of  $BC$  = Slope of  $CD$

$\therefore BC \parallel CD$

Thus the pair of opposite sides are quadrilateral are parallel, so we can say that  $ABCD$  is a parallelogram.

Hence the given vertices,  $A(-2, -1)$ ,  $B(4, 0)$ ,  $C(3, 3)$  and  $D(-3, 2)$  are vertices of a parallelogram.

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**10. Find the angle between the x-axis and the line joining the points (3, -1) and (4, -2).**

**Solution:**

The Slope of the line joining the points (3, -1) and (4, -2) is given by

$$m = (y_2 - y_1)/(x_2 - x_1) \text{ where, } x \neq x_1 \quad m = (-2 - (-1))/(4-3)$$

$$= (-2+1)/(4-3)$$

$$= -1/1$$

$$= -1$$

The angle of inclination of line joining the points (3, -1) and (4, -2) is given by

$$\tan \theta = -1 \quad \theta = (90^\circ + 45^\circ) = 135^\circ$$

$\therefore$  The angle between the x-axis and the line joining the points (3, -1) and (4, -2) is  $135^\circ$ .

**11. The slope of a line is double of the slope of another line. If tangent of the angle between them is  $1/3$ , find the slopes of the lines.**

**Solution:**

Let us consider ' $m_1$ ' and ' $m$ ' be the slope of the two given lines such that  $m_1 = 2m$

We know that if  $\theta$  is the angle between the lines  $l_1$  and  $l_2$  with slope  $m_1$  and  $m_2$ , then

$$\tan \theta = \left| \frac{(m_2 - m_1)}{(1 + m_1 m_2)} \right|$$

Given here that the tangent of the angle between the two lines is  $1/3$

So,

$$\frac{1}{3} = \left| \frac{m - 2m}{1 + 2m \times m} \right| = \left| \frac{-m}{1 + 2m^2} \right|$$

$$\frac{1}{3} = \frac{m}{1 + 2m^2}$$

Now, case 1:

$$\frac{1}{3} = \frac{-m}{1 + 2m^2}$$

$$1 + 2m^2 = -3m$$

$$2m^2 + 1 + 3m = 0$$

$$2m(m+1) + 1(m+1) = 0$$

$$(2m+1)(m+1) = 0 \quad m = -$$

$$1 \text{ or } -1/2$$

If  $m = -1$ , then the slope of the lines are -1 and -2

If  $m = -1/2$ , then the slope of the lines are -1/2 and -1

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Case 2:

$$\frac{1}{3} = \frac{-m}{1+2m^2}$$

$$2m^2 - 3m + 1 = 0$$

$$2m^2 - 2m - m + 1 = 0 \quad 2m$$

$$(m - 1) - 1(m - 1) = 0$$

$$m = 1 \text{ or } 1/2$$

If  $m = 1$ , then the slope of the lines are 1 and 2

If  $m = 1/2$ , then the slope of the lines are  $1/2$  and 1

$\therefore$  The slope of the lines are  $[-1 \text{ and } -2]$  or  $[-1/2 \text{ and } -1]$  or  $[1 \text{ and } 2]$  or  $[1/2 \text{ and } 1]$

**12. A line passes through  $(x_1, y_1)$  and  $(h, k)$ . If slope of the line is  $m$ , show that  $k - y_1 = m(h - x_1)$ .**

**Solution:**

Given: the slope of the line is 'm'

The slope of the line passing through  $(x_1, y_1)$  and  $(h, k)$  is  $(k - y_1)/(h - x_1)$

So,

$$(k - y_1)/(h - x_1) = m$$

$$(k - y_1) = m(h - x_1) \text{ Hence}$$

proved.

**13. If three points  $(h, 0)$ ,  $(a, b)$  and  $(0, k)$  lie on a line, show that  $a/h + b/k = 1$**

**Solution:**

Let us consider if the given points A  $(h, 0)$ , B  $(a, b)$  and C  $(0, k)$  lie on a line

Then, slope of AB = slope of BC

$$(b - 0)/(a - h) = (k - b)/(0 - a) \text{ let}$$

us simplify we get,  $-ab = (k - b)$

$$(a - h) - ab = ka - kh - ab + bh \quad ka$$

$$+bh = kh$$

Divide both the sides by  $kh$  we get,

$$ka/kh + bh/kh = kh/kh \quad a/h + b/k =$$

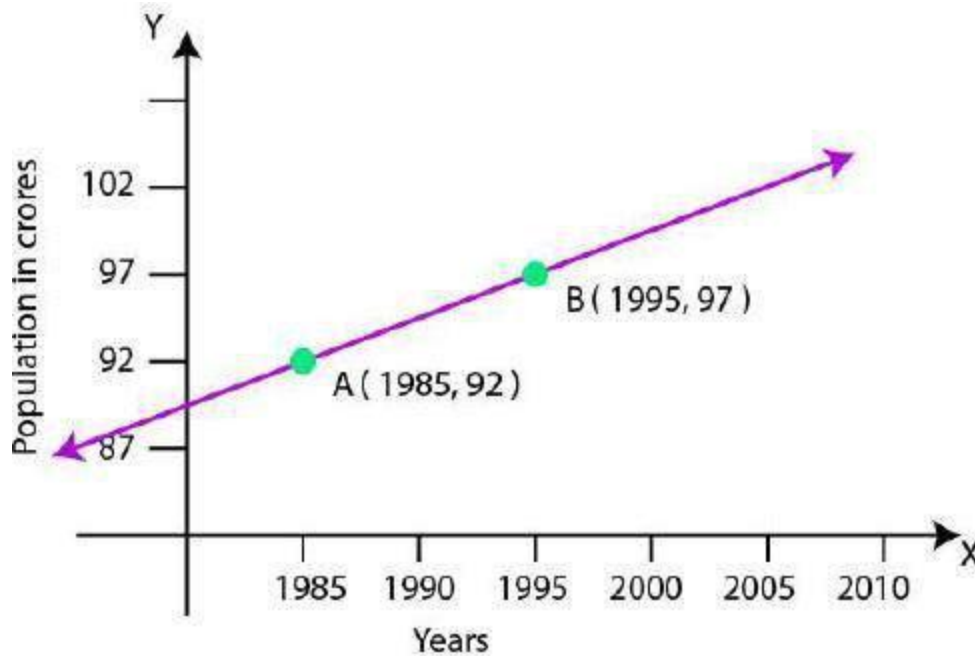
$$1$$

Hence proved.

**14. Consider the following population and year graph (Fig 10.10), find the slope of the line AB and using it, find what will be the population in the year 2010?**



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### Solution:

We know that, the line AB passes through points A (1985, 92) and B (1995, 97),  
Its slope will be  $(97 - 92)/(1995 - 1985) = 5/10 = 1/2$

Let 'y' be the population in the year 2010. Then, according to the given graph, AB must pass through point C (2010, y) So now, slope of AB = slope of BC

$$\frac{1}{2} = \frac{y - 97}{2010 - 1995}$$

$$15/2 = y - 97 \quad y = 7.5$$

$$+ 97 = 104.5$$

$\therefore$  The slope of the line AB is  $1/2$ , while in the year 2010 the population will be 104.5 crores.

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## EXERCISE 10.2

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In Exercises 1 to 8, find the equation of the line which satisfy the given conditions:

1. Write the equations for the x-and y-axes.

**Solution:**

The y-coordinate of every point on x-axis is 0.  $\therefore$

Equation of x-axis is  $y = 0$ .

The x-coordinate of every point on y-axis is 0.

$\therefore$  Equation of y-axis is  $x = 0$ .

2. Passing through the point  $(-4, 3)$  with slope  $1/2$

**Solution:**

Given:

Point  $(-4, 3)$  and slope,  $m = 1/2$

We know that the point  $(x, y)$  lies on the line with slope  $m$  through the fixed point  $(x_0, y_0)$ , if and only if, its coordinates satisfy the equation  $y - y_0 = m(x - x_0)$

So,  $y - 3 = 1/2(x - (-4))$

$y - 3 = 1/2(x + 4)$

$2(y - 3) = x + 4$

$2y - 6 = x + 4$

$x + 4 - (2y - 6) = 0$

$x + 4 - 2y + 6 = 0$

$x - 2y + 10 = 0$

$\therefore$  The equation of the line is  $x - 2y + 10 = 0$ .

3. Passing through  $(0, 0)$  with slope  $m$ .

**Solution:**

Given:

Point  $(0, 0)$  and slope,  $m = m$

We know that the point  $(x, y)$  lies on the line with slope  $m$  through the fixed point  $(x_0, y_0)$ , if and only if, its coordinates satisfy the equation  $y - y_0 = m(x - x_0)$

So,  $y - 0 = m(x - 0)$

$y = mx$

$y - mx = 0$

$\therefore$  The equation of the line is  $y - mx = 0$ .

**4. Passing through  $(2, 2\sqrt{3})$  and inclined with the x-axis at an angle of  $75^\circ$ . Solution:**

Given: point  $(2, 2\sqrt{3})$  and  $\theta = 75^\circ$  Equation

of line:  $(y - y_1) = m(x - x_1)$

where,  $m = \text{slope of line} = \tan \theta$  and  $(x_1, y_1)$  are the points through which line passes  $\therefore$

$m = \tan 75^\circ$

$75^\circ = 45^\circ + 30^\circ$  Applying

the formula:

$$\tan(A + B) = \frac{\tan A + \tan B}{1 - \tan A \cdot \tan B}$$

$$\tan(45^\circ + 30^\circ) = \frac{\tan 45^\circ + \tan 30^\circ}{1 - \tan 45^\circ \cdot \tan 30^\circ} = \frac{1 + \frac{1}{\sqrt{3}}}{1 - \frac{1}{\sqrt{3}}}$$

$$\tan 75^\circ = \frac{\sqrt{3} + 1}{\sqrt{3} - 1}$$

Let us rationalizing we get,

$$\tan 75^\circ = \frac{3 + 1 + 2\sqrt{3}}{3 - 1} = 2 + \sqrt{3}$$

We know that the point  $(x, y)$  lies on the line with slope  $m$  through the fixed point  $(x_1, y_1)$ , if and only if, its coordinates satisfy the equation  $y - y_1 = m(x - x_1)$  Then,  $y - 2\sqrt{3} = (2 + \sqrt{3})(x - 2)$   $y - 2\sqrt{3} = 2x - 4 + \sqrt{3}x - 2\sqrt{3}$   $y = 2x - 4 + \sqrt{3}x$

$$(2 + \sqrt{3})x - y - 4 = 0$$

$$(2 + \sqrt{3})x - y - 4 = 0$$

$\therefore$  The equation of the line is  $(2 + \sqrt{3})x - y - 4 = 0$ .

**5. Intersecting the x-axis at a distance of 3 units to the left of origin with slope -2. Solution:**

Given:

Slope,  $m = -2$

We know that if a line  $L$  with slope  $m$  makes x-intercept  $d$ , then equation of  $L$  is  $y = m(x - d)$ .

If the distance is 3 units to the left of origin then  $d = -3$

$$\text{So, } y = (-2)(x - (-3))$$

$$y = (-2)(x + 3) \quad y = -$$

$$2x - 6$$

$$2x + y + 6 = 0$$

$\therefore$  The equation of the line is  $2x + y + 6 = 0$ .

**6. Intersecting the y-axis at a distance of 2 units above the origin and making an angle of  $30^\circ$  with positive direction of the x-axis. Solution:**

Given:  $\theta = 30^\circ$

We know that slope,  $m = \tan \theta$

$$m = \tan 30^\circ = (1/\sqrt{3})$$

We know that the point  $(x, y)$  on the line with slope  $m$  and y-intercept  $c$  lies on the line if and only if  $y = mx + c$ .

If distance is 2 units above the origin,  $c = +2$

$$\text{So, } y = (1/\sqrt{3})x + 2 \quad y = (x + 2\sqrt{3}) / \sqrt{3} \quad \sqrt{3} y$$

$$= x + 2\sqrt{3} \quad x - \sqrt{3} y + 2\sqrt{3} = 0$$

$\therefore$  The equation of the line is  $x - \sqrt{3} y + 2\sqrt{3} = 0$ .

**7. Passing through the points  $(-1, 1)$  and  $(2, -4)$ .**

**Solution:**

Given:

Points  $(-1, 1)$  and  $(2, -4)$

We know that the equation of the line passing through the points  $(x_1, y_1)$  and  $(x_2, y_2)$  is given by

$$y - y_1 = \frac{y_2 - y_1}{x_2 - x_1} (x - x_1)$$

$$y - 1 = \frac{-4 - 1}{2 - (-1)} (x - (-1))$$

$$y - 1 = -5/3 (x + 1) \quad 3$$

$$(y - 1) = (-5) (x + 1)$$

$$3y - 3 = -5x - 5$$

$$3y - 3 + 5x + 5 = 0$$

$$5x + 3y + 2 = 0$$

$\therefore$  The equation of the line is  $5x + 3y + 2 = 0$ .

**8. Perpendicular distance from the origin is 5 units and the angle made by the perpendicular with the positive x-axis is  $30^\circ$ . Solution:**

Given:  $p = 5$  and  $\omega = 30^\circ$

We know that the equation of the line having normal distance  $p$  from the origin and angle  $\omega$  which the normal makes with the positive direction of x-axis is given by  $x \cos \omega + y \sin \omega = p$ .

Substituting the values in the equation, we get

$$x \cos 30^\circ + y \sin 30^\circ = 5 \quad x(\sqrt{3}/2) + y(1/2) = 5$$

$$\sqrt{3}x + y = 5(2) = 10 \quad \sqrt{3}x + y - 10 = 0$$

$$x + y - 10 = 0$$

$\therefore$  The equation of the line is  $\sqrt{3}x + y - 10 = 0$ .

**9. The vertices of  $\Delta PQR$  are  $P(2, 1)$ ,  $Q(-2, 3)$  and  $R(4, 5)$ . Find equation of the median through the vertex  $R$ .**

**Solution:** Given:

Vertices of  $\Delta PQR$  i.e.  $P(2, 1)$ ,  $Q(-2, 3)$  and  $R(4, 5)$

Let  $RL$  be the median of vertex  $R$ . So,  $L$  is a midpoint of  $PQ$ .

We know that the midpoint formula is given by  $\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$ .

$$\therefore L = \left(\frac{2-2}{2}, \frac{1+3}{2}\right) = (0, 2)$$

We know that the equation of the line passing through the points  $(x_1, y_1)$  and  $(x_2, y_2)$  is

$$\text{given by } y - y_1 = \frac{y_2 - y_1}{x_2 - x_1}(x - x_1)$$

$$\therefore y - 5 = \frac{2 - 5}{0 - 4}(x - 4)$$

$$y - 5 = -3/4 (x - 4) \quad (-4)$$

$$(y - 5) = (-3)(x - 4)$$

$$-4y + 20 = -3x + 12$$

$$-4y + 20 + 3x - 12 = 0$$

$$3x - 4y + 8 = 0$$

$\therefore$  The equation of median through the vertex  $R$  is  $3x - 4y + 8 = 0$ .

**10. Find the equation of the line passing through  $(-3, 5)$  and perpendicular to the line through the points  $(2, 5)$  and  $(-3, 6)$ .**

**Solution:**

Given:

Points are  $(2, 5)$  and  $(-3, 6)$ .

$$\begin{aligned}\text{We know that slope, } m &= (y_2 - y_1)/(x_2 - x_1) \\ &= (6 - 5)/(-3 - 2) \\ &= 1/-5 = -1/5\end{aligned}$$

We know that two non-vertical lines are perpendicular to each other if and only if their slopes are negative reciprocals of each other.

$$\begin{aligned}\text{Then, } m &= (-1/m) \\ &= -1/(-1/5) \\ &= 5\end{aligned}$$

We know that the point  $(x, y)$  lies on the line with slope  $m$  through the fixed point  $(x_0, y_0)$ , if and only if, its coordinates satisfy the equation  $y - y_0 = m(x - x_0)$

$$\begin{aligned}\text{Then, } y - 5 &= 5(x - (-3)) \\ y - 5 &= 5x + 15 \\ -y + 5 &= 0 \\ 5x - y + 20 &= 0 \\ \therefore \text{The equation of the line is } 5x - y + 20 &= 0\end{aligned}$$

**11. A line perpendicular to the line segment joining the points  $(1, 0)$  and  $(2, 3)$  divides it in the ratio  $1: n$ . Find the equation of the line.**

**Solution:**

We know that the coordinates of a point dividing the line segment joining the points  $(x_1, y_1)$  and  $(x_2, y_2)$  internally in the ratio  $m: n$  are

$$\left( \frac{mx_2 + nx_1}{m+n}, \frac{my_2 + ny_1}{m+n} \right) = \left( \frac{1(2) + n(1)}{1+n}, \frac{1(3) + n(0)}{1+n} \right) = \left( \frac{2+n}{1+n}, \frac{3}{1+n} \right)$$

$$\begin{aligned}\text{We know that slope, } m &= (y_2 - y_1)/(x_2 - x_1) \\ &= (3 - 0)/(2 - 1) \\ &= 3/1 \\ &= 3\end{aligned}$$

We know that two non-vertical lines are perpendicular to each other if and only if their slopes are negative reciprocals of each other.

Then,  $m = (-1/m) = -1/3$

We know that the point  $(x, y)$  lies on the line with slope  $m$  through the fixed point  $(x_0, y_0)$ , if and only if, its coordinates satisfy the equation  $y - y_0 = m(x - x_0)$ . Here, the point is

$$\left(\frac{2+n}{1+n}, \frac{3}{1+n}\right)$$

$$\left(y - \frac{3}{1+n}\right) = \frac{-1}{3} \left(x - \frac{2+n}{1+n}\right)$$

$$3((1+n)y - 3) = -(1+n)x + 2+n$$

$$3(1+n)y - 9 = -(1+n)x + 2+n$$

$$(1+n)x + 3(1+n)y - n - 9 - 2 = 0$$

$$(1+n)x + 3(1+n)y - n - 11 = 0$$

$\therefore$  The equation of the line is  $(1+n)x + 3(1+n)y - n - 11 = 0$ .

**12. Find the equation of a line that cuts off equal intercepts on the coordinate axes and passes through the point  $(2, 3)$ .**

**Solution:**

Given: the line cuts off equal intercepts on the coordinate axes i.e.  $a = b$ .

We know that equation of the line intercepts  $a$  and  $b$  on  $x$ - and  $y$ -axis, respectively, which is

$$x/a + y/b = 1 \quad \text{So,}$$

$$x/a + y/a = 1 \quad x +$$

$$y = a \quad \dots (1)$$

Given: point  $(2, 3)$

$$2 + 3 = a$$

$$= 5$$

Substitute value of ' $a$ ' in (1), we get

$$x + y = 5 \quad x + y - 5 = 0$$

$\therefore$  The equation of the line is  $x + y - 5 = 0$ .

**13. Find equation of the line passing through the point  $(2, 2)$  and cutting off intercepts on the axes whose sum is 9.**

**Solution:**



We know that equation of the line making intercepts  $a$  and  $b$  on  $x$ -and  $y$ -axis, respectively, is  $x/a + y/b = 1$  . ... (1) Given: sum of intercepts = 9  $a + b = 9$

$$b = 9 - a$$

Now, substitute value of  $b$  in the above equation, we get  $x/a$

$$+ y/(9 - a) = 1$$

Given: the line passes through the point  $(2, 2)$ ,

$$\text{So, } 2/a + 2/(9 - a) = 1$$

$$[2(9 - a) + 2a] / a(9 - a) = 1$$

$$[18 - 2a + 2a] / a(9 - a) = 1$$

$$18/a(9 - a) = 1$$

$$18 = a(9 - a)$$

$$18 = 9a - a^2$$

$$-9a + 18 = 0$$

Upon

factorizing, we

$$\text{get } a^2 - 9a + 18 = 0$$

$$a(a - 3) - 6(a - 3) =$$

$$0 \quad (a - 3)(a - 6) =$$

$$0 \quad a = 3 \text{ or } a =$$

$$6$$

Let us substitute in (1),

Case 1 ( $a = 3$ ): Then  $b$

$$= 9 - 3 = 6 \quad x/3 + y/6 =$$

$$1 \quad 2x + y = 6$$

$$2x + y - 6 = 0$$

Case 2 ( $a = 6$ ):

$$\text{Then } b = 9 - 6 = 3$$

$$x/6 + y/3 = 1 \quad x +$$

$$2y = 6$$

$$x + 2y - 6 = 0$$

$\therefore$  The equation of the line is  $2x + y - 6 = 0$  or  $x + 2y - 6 = 0$ .

**14. Find equation of the line through the point (0, 2) making an angle  $2\pi/3$  with the positive x-axis. Also, find the equation of line parallel to it and crossing the y-axis at a distance of 2 units below the origin.**

**Solution:** Given:

Point (0, 2) and  $\theta = 2\pi/3$  We

know that  $m = \tan \theta$

$$m = \tan (2\pi/3) = -\sqrt{3}$$

We know that the point (x, y) lies on the line with slope m through the fixed point  $(x_0, y_0)$ , if and only if, its coordinates satisfy the equation  $y - y_0 = m (x - x_0)$   
 $y - 2 = -\sqrt{3} (x - 0)$   
 $y - 2 = -\sqrt{3} x$   
 $\sqrt{3} x + y - 2 = 0$

Given, equation of line parallel to above obtained equation crosses the y-axis at a distance of 2 units below the origin.

So, the point = (0, -2) and  $m = -\sqrt{3}$

From point slope form equation,

$$y - (-2) = -\sqrt{3} (x - 0)$$

$$y + 2 = -\sqrt{3} x$$

$$y + 2 = 0$$

$\therefore$  The equation of line is  $\sqrt{3} x + y - 2 = 0$  and the line parallel to it is  $\sqrt{3} x + y + 2 = 0$ .

**15. The perpendicular from the origin to a line meets it at the point (-2, 9), find the equation of the line.**

**Solution:**

Given:

Points are origin (0, 0) and (-2, 9).

We know that slope,  $m = (y_2 - y_1)/(x_2 - x_1)$

$$= (9 - 0)/(-2 - 0)$$

$$= -9/2$$

We know that two non-vertical lines are perpendicular to each other if and only if their slopes are negative reciprocals of each other.  $m = (-1/m) = -1/(-9/2) = 2/9$

We know that the point  $(x, y)$  lies on the line with slope  $m$  through the fixed point  $(x_0, y_0)$ , if and only if, its coordinates satisfy the equation  $y - y_0 = m(x - x_0)$   
 $y - 9 = (2/9)(x - (-2))$

$$9(y - 9) = 2(x + 2)$$

$$9y - 81 = 2x + 4$$

$$2x + 4 - 9y + 81 = 0$$

$$2x - 9y + 85 = 0$$

$\therefore$  The equation of line is  $2x - 9y + 85 = 0$ .

**16. The length  $L$  (in centimetre) of a copper rod is a linear function of its Celsius temperature  $C$ . In an experiment, if  $L = 124.942$  when  $C = 20$  and  $L = 125.134$  when  $C = 110$ , express  $L$  in terms of  $C$ .**

**Solution:**

Let us assume ' $L$ ' along X-axis and ' $C$ ' along Y-axis, we have two points  $(124.942, 20)$  and  $(125.134, 110)$  in XY-plane.

We know that the equation of the line passing through the points  $(x_1, y_1)$  and  $(x_2, y_2)$  is given by

$$y - y_1 = \frac{y_2 - y_1}{x_2 - x_1}(x - x_1)$$

$$C - 20 = \frac{110 - 20}{125.134 - 124.942}(L - 124.942)$$

$$C - 20 = \frac{90}{0.192}(L - 124.942)$$

$$0.192(C - 20) = 90(L - 124.942)$$

$$L = \frac{0.192}{90}(C - 20) + 124.942$$

$\therefore$  The required relation is  $L = \frac{0.192}{90}(C - 20) + 124.942$

**17. The owner of a milk store finds that, he can sell 980 litres of milk each week at Rs. 14/litre and 1220 litres of milk each week at Rs. 16/litre. Assuming a linear relationship between selling price and demand, how many litres could he sell weekly at Rs. 17/litre?**

**Solution:**

Assuming the relationship between selling price and demand is linear.

Let us assume selling price per litre along X-axis and demand along Y-axis, we have two points  $(14, 980)$  and  $(16, 1220)$  in XY-plane.

We know that the equation of the line passing through the points  $(x_1, y_1)$  and  $(x_2, y_2)$  is given by

$$y - y_1 = \frac{y_2 - y_1}{x_2 - x_1} (x - x_1)$$

$$y - 980 = \frac{1220 - 980}{16 - 14} (x - 14)$$

$$y - 980 = \frac{240}{2} (x - 14)$$

$$y - 980 = 120 (x - 14)$$

$$y = 120 (x - 14) + 980$$

When  $x = \text{Rs } 17/\text{litre}$ ,  $y$

$$= 120 (17 - 14) + 980$$

$$= 120(3) + 980$$

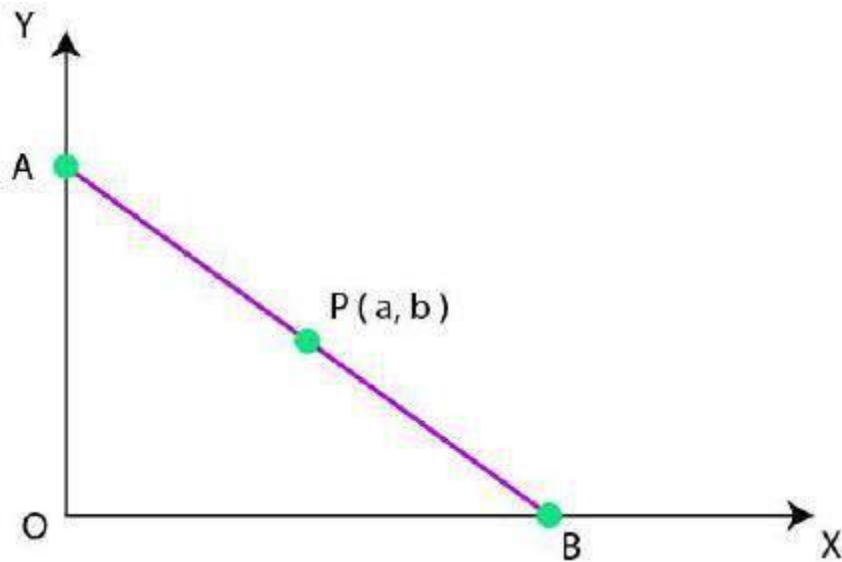
$$y = 360 + 980 = 1340$$

$\therefore$  The owner can sell 1340 litres weekly at Rs. 17/litre.

**18. P (a, b) is the mid-point of a line segment between axes. Show that equation of the line is  $x/a + y/b = 2$  Solution:**

Let AB be a line segment whose midpoint is P (a, b).

Let the coordinates of A and B be (0, y) and (x, 0) respectively.



We know that the midpoint is given by  $\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$

Since P is the midpoint of (a, b),

$$\left(\frac{0+x}{2}, \frac{y+0}{2}\right) = (a, b)$$

$$\left(\frac{x}{2}, \frac{y}{2}\right) = (a, b)$$

$$a = x/2 \text{ and } b = y/2$$

$$x = 2a \text{ and } y = 2b$$

$$A = (0, 2b) \text{ and } B = (2a, 0)$$

We know that the equation of the line passing through the points  $(x_1, y_1)$  and  $(x_2, y_2)$  is given by

$$y - y_1 = \frac{y_2 - y_1}{x_2 - x_1} (x - x_1)$$

$$y - 2b = \frac{0 - 2b}{2a - 0} (x - 0)$$

$$y - 2b = \frac{-2b}{2a} (x)$$

$$y - 2b = \frac{-b}{a} (x)$$

$$a(y - 2b) = -bx \quad ay - 2ab = -bx \quad bx + ay = 2ab$$

Divide both the sides with  $ab$ , then

$$\frac{bx}{ab} + \frac{ay}{ab} = \frac{2ab}{ab}$$

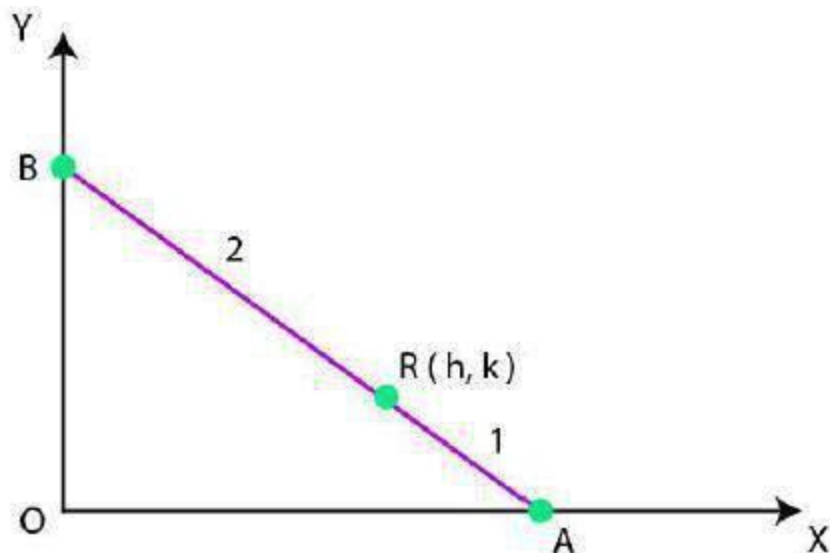
$$\frac{x}{a} + \frac{y}{b} = 2$$

Hence proved.

**19. Point R (h, k) divides a line segment between the axes in the ratio 1: 2. Find the equation of the line.**

**Solution:**

Let us consider, AB be the line segment such that r (h, k) divides it in the ratio 1: 2. So the coordinates of A and B be (0, y) and (x, 0) respectively.



We know that the coordinates of a point dividing the line segment joins the points  $(x_1, y_1)$  and  $(x_2, y_2)$  internally in the ratio  $m: n$  is

$$\left( \frac{mx_2 + nx_1}{m+n}, \frac{my_2 + ny_1}{m+n} \right)$$

$$\left( \frac{1(0) + 2(x)}{1+2}, \frac{1(y) + 2(0)}{1+2} \right) = (h, k)$$

$$\left( \frac{2x}{3}, \frac{y}{3} \right) = (h, k)$$

$$h = \frac{2x}{3} \text{ and } k = \frac{y}{3}$$

$$x = \frac{3h}{2} \text{ and } y = 3k$$

$$\therefore A = (0, 3k) \text{ and } B = \left( \frac{3h}{2}, 0 \right)$$

We know that the equation of the line passing through the points  $(x_1, y_1)$  and  $(x_2, y_2)$  is given by

$$y - y_1 = \frac{y_2 - y_1}{x_2 - x_1} (x - x_1)$$

$$y - 3k = \frac{0 - 3k}{\frac{3h}{2} - 0} (x - 0)$$

$$3h(y - 3k) = -6kx$$

$$3hy - 9hk = -6kx$$

$$6kx + 3hy = 9hk$$

Let us divide both the sides by  $9hk$ , we get,

$$2x/3h + y/3k = 1$$

$\therefore$  The equation of the line is given by  $2x/3h + y/3k = 1$

**20. By using the concept of equation of a line, prove that the three points (3, 0), (-2, -2) and (8, 2) are collinear.**

**Solution:**

According to the question,

If we have to prove that the given three points (3, 0), (-2, -2) and (8, 2) are collinear, then we have to also prove that the line passing through the points (3, 0) and (-2, -2) also passes through the point (8, 2).

By using the formula,

The equation of the line passing through the points  $(x_1, y_1)$  and  $(x_2, y_2)$  is given by

$$y - y_1 = \frac{y_2 - y_1}{x_2 - x_1} (x - x_1)$$

$$y - 0 = \frac{-2 - 0}{-2 - 3} (x - 3)$$

$$y = \frac{-2}{-5} (x - 3)$$

$$-5y = -2(x - 3)$$

$$-5y = -2x + 6$$

$$2x - 5y = 6$$

If  $2x - 5y = 6$  passes through (8, 2),

$$2x - 5y = 2(8) - 5(2)$$

$$= 16 - 10$$

$$= 6$$

$$= \text{RHS}$$

The line passing through the points (3, 0) and (-2, -2) also passes through the point (8, 2).

Hence proved. The given three points are collinear.

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### EXERCISE 10.3

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**1. Reduce the following equations into slope - intercept form and find their slopes and the y - intercepts. (i)  $x + 7y = 0$**

**(ii)  $6x + 3y - 5 = 0$**

**(iii)  $y = 0$**

**Solution: (i)**

$x + 7y = 0$

Given:

The equation is  $x + 7y = 0$

Slope – intercept form is represented in the form ' $y = mx + c$ ', where  $m$  is the slope and  $c$  is the y intercept

So, the above equation can be expressed as

$$y = -1/7x + 0$$

$\therefore$  The above equation is of the form  $y = mx + c$ , where  $m = -1/7$  and  $c = 0$ .

**(ii)  $6x + 3y - 5 = 0$**

Given:

The equation is  $6x + 3y - 5 = 0$

Slope – intercept form is represented in the form ' $y = mx + c$ ', where  $m$  is the slope and  $c$  is the y intercept

So, the above equation can be expressed as

$$3y = -6x + 5$$

$$y = -6/3x + 5/3$$

$$y = -2x + 5/3$$

$\therefore$  The above equation is of the form  $y = mx + c$ , where  $m = -2$  and  $c = 5/3$ .

**(iii)  $y = 0$**

Given:

Slope – intercept form is given by ' $y = mx + c$ ', where  $m$  is the slope and  $c$  is the y intercept  $y = 0 \times x + 0$

$\therefore$  The above equation is of the form  $y = mx + c$ , where  $m = 0$  and  $c = 0$ .

**2. Reduce the following equations into intercept form and find their intercepts on the axes.**

**(i)  $3x + 2y - 12 = 0$**

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(ii)  $4x - 3y = 6$  (iii)  $3y + 2 = 0$  Solution:

(i)  $3x + 2y - 12 = 0$

Given:

The equation is  $3x + 2y - 12 = 0$

Equation of line in intercept form is given by  $x/a + y/b = 1$ , where 'a' and 'b' are intercepts on x axis and y - axis respectively. So,  $3x + 2y = 12$

now let us divide both sides by 12, we get

$$3x/12 + 2y/12 = 12/12 \quad x/4$$

$$+ y/6 = 1$$

$\therefore$  The above equation is of the form  $x/a + y/b = 1$ , where  $a = 4$ ,  $b = 6$

Intercept on x - axis is 4

Intercept on y - axis is 6

(ii)  $4x - 3y = 6$

Given:

The equation is  $4x - 3y = 6$

Equation of line in intercept form is given by  $x/a + y/b = 1$ , where 'a' and 'b' are intercepts on x axis and y - axis respectively.

So,  $4x - 3y = 6$

Now let us divide both sides by 6, we get

$$4x/6 - 3y/6 = 6/6$$

$$2x/3 - y/2 = 1 \quad x/(3/2)$$

$$+ y/(-2) = 1$$

$\therefore$  The above equation is of the form  $x/a + y/b = 1$ , where  $a = 3/2$ ,  $b = -2$

Intercept on x - axis is  $3/2$

Intercept on y - axis is -2

(iii)  $3y + 2 = 0$  Given:

The equation is  $3y + 2 = 0$

Equation of line in intercept form is given by  $x/a + y/b = 1$ , where 'a' and 'b' are intercepts on x axis and y - axis respectively.

So,  $3y = -2$

Now, let us divide both sides by -2, we get

$$3y/-2 = -2/-2$$

$$3y/-2 = 1$$

$$y/(-2/3) = 1$$

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$\therefore$  The above equation is of the form  $x/a + y/b = 1$ , where  $a = 0$ ,  $b = -2/3$

Intercept on x – axis is 0

Intercept on y – axis is  $-2/3$

**3. Reduce the following equations into normal form. Find their perpendicular distances from the origin and angle between perpendicular and the positive x-axis.**

(i)  $x - \sqrt{3}y + 8 = 0$

(ii)  $y - 2 = 0$  (iii)

$x - y = 4$

**Solution:**

(i)  $x - \sqrt{3}y + 8 = 0$  Given:

The equation is  $x - \sqrt{3}y + 8 = 0$

Equation of line in normal form is given by  $x \cos \theta + y \sin \theta = p$  where ' $\theta$ ' is the angle between perpendicular and positive x axis and ' $p$ ' is perpendicular distance from origin. So now,  $x - \sqrt{3}y + 8 = 0$   $x - \sqrt{3}y = -8$

Divide both the sides by  $\sqrt{(1^2 + (\sqrt{3})^2)} = \sqrt{(1 + 3)} = \sqrt{4} = 2$

$x/2 - \sqrt{3}y/2 = -8/2$   $(-1/2)x + \sqrt{3}/2y = 4$

This is in the form of:  $x \cos 120^\circ + y \sin 120^\circ = 4$

$\therefore$  The above equation is of the form  $x \cos \theta + y \sin \theta = p$ , where  $\theta = 120^\circ$  and  $p = 4$ .

Perpendicular distance of line from origin = 4

Angle between perpendicular and positive x – axis =  $120^\circ$

(ii)  $y - 2 = 0$  Given:

The equation is  $y - 2 = 0$

Equation of line in normal form is given by  $x \cos \theta + y \sin \theta = p$  where ' $\theta$ ' is the angle between perpendicular and positive x axis and ' $p$ ' is perpendicular distance from origin.

So now,  $0 \times x + 1 \times y = 2$

Divide both sides by  $\sqrt{(0^2 + 1^2)} = \sqrt{1} = 1$

$0(x) + 1(y) = 2$

This is in the form of:  $x \cos 90^\circ + y \sin 90^\circ = 2$

$\therefore$  The above equation is of the form  $x \cos \theta + y \sin \theta = p$ , where  $\theta = 90^\circ$  and  $p = 2$ .

Perpendicular distance of line from origin = 2

Angle between perpendicular and positive x – axis =  $90^\circ$

(iii)  $x - y = 4$  Given:

The equation is  $x - y + 4 = 0$

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Equation of line in normal form is given by  $x \cos \theta + y \sin \theta = p$  where ' $\theta$ ' is the angle between perpendicular and positive x axis and ' $p$ ' is perpendicular distance from origin.

So now,  $x - y = 4$

Divide both the sides by  $\sqrt{(1^2 + 1^2)} = \sqrt{(1+1)} = \sqrt{2}$

$$x/\sqrt{2} - y/\sqrt{2} = 4/\sqrt{2} \quad 1/\sqrt{2}x + (-1/\sqrt{2})y = 2\sqrt{2}$$

This is in the form:  $x \cos 315^\circ + y \sin 315^\circ = 2\sqrt{2}$

$\therefore$  The above equation is of the form  $x \cos \theta + y \sin \theta = p$ , where  $\theta = 315^\circ$  and  $p = 2\sqrt{2}$ .

Perpendicular distance of line from origin =  $2\sqrt{2}$

Angle between perpendicular and positive x - axis =  $315^\circ$

**4. Find the distance of the point  $(-1, 1)$  from the line  $12(x + 6) = 5(y - 2)$ .**

**Solution:**

Given:

The equation of the line is  $12(x + 6) = 5(y - 2)$ .

$$12x + 72 = 5y - 10 \quad 12x$$

$$- 5y + 82 = 0 \quad \dots (1)$$

Now, compare equation (1) with general equation of line  $Ax + By + C = 0$ , where  $A = 12$ ,  $B = -5$ , and  $C = 82$

Perpendicular distance (d) of a line  $Ax + By + C = 0$  from a point  $(x_1, y_1)$  is given by

$$d = \frac{|Ax_1 + By_1 + C|}{\sqrt{A^2 + B^2}}$$

Given point  $(x_1, y_1) = (-1, 1)$

$\therefore$  Distance of point  $(-1, 1)$  from the given line is

$$d = \frac{|12 \times (-1) + (-5) \times 1 + 82|}{\sqrt{12^2 + (-5)^2}} = \frac{|-12 - 5 + 82|}{\sqrt{144 + 25}} = \frac{|65|}{\sqrt{169}} = \frac{65}{13} \text{ units}$$

$$= 5 \text{ units}$$

$\therefore$  The distance is 5units.

**5. Find the points on the x-axis, whose distances from the line  $x/3 + y/4 = 1$  are 4 units.**

**Solution:**

Given:

The equation of line is  $x/3 + y/4 = 1$

$$4x + 3y = 12$$

$$4x + 3y - 12 = 0 \quad \dots (1)$$

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Now, compare equation (1) with general equation of line  $Ax + By + C = 0$ , where  $A = 4$ ,  $B = 3$ , and  $C = -12$

Let  $(a, 0)$  be the point on the x-axis, whose distance from the given line is 4 units. So, the perpendicular distance (d) of a line  $Ax + By + C = 0$  from a point  $(x_1, y_1)$  is given by

$$d = \frac{|Ax_1 + By_1 + C|}{\sqrt{A^2 + B^2}}$$

$$4 = \frac{|4a + 3 \times 0 - 12|}{\sqrt{4^2 + 3^2}}$$

$$4 = \frac{|4a - 12|}{\sqrt{16 + 9}} = \frac{|4a - 12|}{5}$$

$$|4a - 12| = 4 \times 5$$

$$\pm (4a - 12) = 20$$

$$4a - 12 = 20 \text{ or } -(4a - 12) = 20$$

$$4a = 20 + 12 \text{ or } 4a = -20 + 12$$

$$a = 32/4 \text{ or } a = -8/4 \text{ } a = 8 \text{ or } a = -$$

$$2$$

$\therefore$  The required points on the x – axis are  $(-2, 0)$  and  $(8, 0)$

### 6. Find the distance between parallel lines

(i)  $15x + 8y - 34 = 0$  and  $15x + 8y + 31 = 0$  (ii)

$l(x + y) + p = 0$  and  $l(x + y) - r = 0$  Solution:

(i)  $15x + 8y - 34 = 0$  and  $15x + 8y + 31 = 0$

Given:

The parallel lines are  $15x + 8y - 34 = 0$  and  $15x + 8y + 31 = 0$ .

By using the formula,

The distance (d) between parallel lines  $Ax + By + C_1 = 0$  and  $Ax + By + C_2 = 0$  is given by

$$d = \frac{|C_1 - C_2|}{\sqrt{A^2 + B^2}}$$

Where,  $A = 15$ ,  $B = 8$ ,  $C_1 = -34$ ,  $C_2 = 31$

Distance between parallel lines is

$$d = \frac{|-34 - 31|}{\sqrt{15^2 + 8^2}}$$

$$= \frac{|-65|}{\sqrt{225 + 64}}$$

$$= 65/\sqrt{289}$$

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$$= 65/17$$

∴ The distance between parallel lines is 65/17

(ii)  $l(x + y) + p = 0$  and  $l(x + y) - r = 0$

Given:

The parallel lines are  $l(x + y) + p = 0$  and  $l(x + y) - r = 0$ .

$lx + ly + p = 0$  and  $lx + ly - r = 0$  by using the formula,

The distance (d) between parallel lines  $Ax + By + C_1 = 0$  and  $Ax + By + C_2 = 0$  is given by

$$d = \frac{|C_1 - C_2|}{\sqrt{A^2 + B^2}}$$

Where,  $A = l$ ,  $B = l$ ,  $C_1 = p$ ,  $C_2 = -r$

Distance between parallel lines is

$$\begin{aligned} d &= \frac{|p - (-r)|}{\sqrt{l^2 + l^2}} \\ &= \frac{|p + r|}{\sqrt{2}l} \\ &= \frac{|p+r|}{l\sqrt{2}} \end{aligned}$$

∴ The distance between parallel lines is  $|p+q|/l\sqrt{2}$

**7. Find equation of the line parallel to the line  $3x - 4y + 2 = 0$  and passing through the point  $(-2, 3)$ .**

**Solution:**

Given:

The line is  $3x - 4y + 2 = 0$

So,  $y = 3x/4 + 2/4$

$= 3x/4 + 1/2$

Which is of the form  $y = mx + c$ , where  $m$  is the slope of the given line.

The slope of the given line is  $3/4$

We know that parallel line have same slope. ∴

Slope of other line  $= m = 3/4$

Equation of line having slope  $m$  and passing through  $(x_1, y_1)$  is given by

$$y - y_1 = m(x - x_1)$$

∴ Equation of line having slope  $3/4$  and passing through  $(-2, 3)$  is

$$y - 3 = \frac{3}{4}(x - (-2)) \quad 4y - 3 \times 4 = 3x + 3 \times 2$$

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$$3x - 4y = 18$$

∴ The equation is  $3x - 4y = 18$

**8. Find equation of the line perpendicular to the line  $x - 7y + 5 = 0$  and having x intercept 3.**

**Solution:**

Given:

The equation of line is  $x - 7y + 5 = 0$

So,  $y = 1/7x + 5/7$  [which is of the form  $y = mx + c$ , where  $m$  is the slope of the given line.]

Slope of the given line is  $1/7$

Slope of the line perpendicular to the line having slope  $m$  is  $-1/m$

Slope of the line perpendicular to the line having a slope of  $1/7$  is  $-1/(1/7) = -7$

So, the equation of line with slope  $-7$  and x intercept 3 is given by  $y = m(x - d)$

$$y = -7(x - 3) \quad y = -7x + 21$$

$$7x + y = 21$$

∴ The equation is  $7x + y = 21$

**9. Find angles between the lines  $\sqrt{3}x + y = 1$  and  $x + \sqrt{3}y = 1$ . Solution:**

Given:

The lines are  $\sqrt{3}x + y = 1$  and  $x + \sqrt{3}y = 1$

So,  $y = -\sqrt{3}x + 1 \dots (1)$  and  $y = -1/\sqrt{3}x + 1/\sqrt{3} \dots (2)$

Slope of line (1) is  $m_1 = -\sqrt{3}$ , while the slope of line (2) is  $m_2 = -1/\sqrt{3}$

Let  $\theta$  be the angle between two lines So,

$$\begin{aligned} \tan \theta &= \left| \frac{m_1 - m_2}{1 + m_1 m_2} \right| \\ &= \left| \frac{-\sqrt{3} - \left(-\frac{1}{\sqrt{3}}\right)}{1 + (-\sqrt{3})\left(-\frac{1}{\sqrt{3}}\right)} \right| = \left| \frac{\frac{-3 + 1}{\sqrt{3}}}{1 + 1} \right| = \left| \frac{-2}{2 \times \sqrt{3}} \right| \\ &= 1/\sqrt{3} \end{aligned}$$

$$\theta = 30^\circ$$

∴ The angle between the given lines is either  $30^\circ$  or  $180^\circ - 30^\circ = 150^\circ$

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**10. The line through the points (h, 3) and (4, 1) intersects the line  $7x - 9y - 19 = 0$ . At right angle. Find the value of h.**

**Solution:**

Let the slope of the line passing through (h, 3) and (4, 1) be  $m_1$

$$\text{Then, } m_1 = (1-3)/(4-h) = -2/(4-h)$$

Let the slope of line  $7x - 9y - 19 = 0$  be  $m_2$

$$7x - 9y - 19 = 0 \text{ So,}$$

$$y = 7/9x - 19/9 \quad m_2$$

$$= 7/9$$

Since, the given lines are perpendicular

$$m_1 \times m_2 = -1 \quad -2/(4-h) \times 7/9 = -1$$

$$-14/(36-9h) = -1$$

$$-14 = -1 \times (36 - 9h)$$

$$36 - 9h = 14$$

$$9h = 36 - 14$$

$$= 22/9$$

$\therefore$  The value of h is  $22/9$

**11. Prove that the line through the point  $(x_1, y_1)$  and parallel to the line  $Ax + By + C = 0$  is  $A(x - x_1) + B(y - y_1) = 0$ .**

**Solution:**

Let the slope of line  $Ax + By + C = 0$  be m

$$Ax + By + C = 0 \text{ So,}$$

$$y = -A/Bx - C/B \quad m$$

$$= -A/B$$

By using the formula,

Equation of the line passing through point  $(x_1, y_1)$  and having slope  $m = -A/B$  is

$$y - y_1 = m(x - x_1)$$

$$= -A/B(x - x_1)$$

$$B(y - y_1) = -A(x - x_1)$$

$$\therefore A(x - x_1) + B(y - y_1) = 0$$

So, the line through point  $(x_1, y_1)$  and parallel to the line  $Ax + By + C = 0$  is  $A(x - x_1) +$

$$B(y - y_1) = 0 \text{ Hence}$$

proved.



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**12. Two lines passing through the point  $(2, 3)$  intersect each other at an angle of  $60^\circ$ . If slope of one line is 2, find equation of the other line.**

**Solution:**

Given:  $m_1 = 2$

Let the slope of the first line be  $m_1$

And let the slope of the other line be  $m_2$ .

Angle between the two lines is  $60^\circ$ .

So,

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$$\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1 m_2} \right|$$

$$\tan 60^\circ = \left| \frac{2 - m_2}{1 + 2m_2} \right|$$

$$\sqrt{3} = \pm \left( \frac{2 - m_2}{1 + 2m_2} \right)$$

i.e.,

$$\sqrt{3} = \frac{2 - m_2}{1 + 2m_2} \text{ or } \sqrt{3} = - \left( \frac{2 - m_2}{1 + 2m_2} \right)$$

$$\sqrt{3}(1 + 2m_2) = 2 - m_2 \text{ or } \sqrt{3}(1 + 2m_2) = -(2 - m_2)$$

$$\sqrt{3} + 2\sqrt{3}m_2 + m_2 = 2 \text{ or } \sqrt{3} + 2\sqrt{3}m_2 - m_2 = -2$$

$$m_2(2\sqrt{3} + 1) = 2 - \sqrt{3} \text{ or } m_2(2\sqrt{3} - 1) = -(2 + \sqrt{3})$$

$$m_2 = \frac{2 - \sqrt{3}}{(2\sqrt{3} + 1)} \text{ or } m_2 = \frac{-(2 + \sqrt{3})}{(2\sqrt{3} - 1)}$$

So now let us consider

Case 1: When

$$m_2 = \frac{2 - \sqrt{3}}{(2\sqrt{3} + 1)}$$

The equation of the line passing through point (2, 3) and having a slope  $m_2$  is

$$y - 3 = \left( \frac{2 - \sqrt{3}}{2\sqrt{3} + 1} \right) (x - 2)$$

$$(2\sqrt{3} + 1)y - 3(2\sqrt{3} + 1) = (2 - \sqrt{3})x - 2(2 - \sqrt{3})$$

$$(\sqrt{3} - 2)x + (2\sqrt{3} + 1)y = -4 + 2\sqrt{3} + 6\sqrt{3} + 3$$

$$(\sqrt{3} - 2)x + (2\sqrt{3} + 1)y = 8\sqrt{3} - 1$$

$$\therefore \text{Equation of the other line is } (\sqrt{3} - 2)x + (2\sqrt{3} + 1)y = 8\sqrt{3} - 1$$

Case 2: When

$$m_2 = \frac{-(2 + \sqrt{3})}{(2\sqrt{3} - 1)}$$

The equation of the line passing through point (2, 3) and having a slope  $m_2$  is

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$$y - 3 = \frac{-(2 + \sqrt{3})}{(2\sqrt{3} - 1)}(x - 2)$$

$$(2\sqrt{3} - 1)y - 3(2\sqrt{3} - 1) = -(2 + \sqrt{3})x + 2(2 + \sqrt{3})$$

$$(2\sqrt{3} - 1)y + (2 + \sqrt{3})x = 4 + 2\sqrt{3} + 6\sqrt{3} - 3$$

$$(2\sqrt{3} - 1)y + (2 + \sqrt{3})x = 8\sqrt{3} + 1$$

$$\therefore \text{Equation of the other line is } (2\sqrt{3} - 1)y + (2 + \sqrt{3})x = 8\sqrt{3} + 1$$

**13. Find the equation of the right bisector of the line segment joining the points (3, 4) and (-1, 2).**

**Solution:**

Given:

The right bisector of a line segment bisects the line segment at  $90^\circ$ .

End-points of the line segment AB are given as A (3, 4) and B (-1, 2).

Let mid-point of AB be (x, y)  $x = (3+4)/2$   $y = (-1+2)/2$  (x, y) = (7/2, 1/2)

Let the slope of line AB be  $m_1$

$$= (2 - 4)/(-1 - 3)$$

$$= -2/(-4)$$

$$= 1/2$$

And let the slope of the line perpendicular to AB be  $m_2$

$$= -1/(1/2)$$

$$= -2$$

The equation of the line passing through (1, 3) and having a slope of -2 is

$$(y - 3) = -2(x - 1)$$

$$y - 3 = -2x + 2$$

$$2x + y = 5$$

$\therefore$  The required equation of the line is  $2x + y = 5$

**14. Find the coordinates of the foot of perpendicular from the point (-1, 3) to the line  $3x - 4y - 16 = 0$ .**

**Solution:**

Let us consider the co-ordinates of the foot of the perpendicular from (-1, 3) to the line  $3x - 4y - 16 = 0$  be (a, b)

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So, let the slope of the line joining  $(-1, 3)$  and  $(a, b)$  be  $m_1$   
 $m_1 = (b-3)/(a+1)$

And let the slope of the line  $3x - 4y - 16 = 0$  be  $m_2$

$$y = \frac{3}{4}x - 4 \quad m_2 = \frac{3}{4}$$

Since these two lines are perpendicular,  $m_1 \times m_2 = -1$

$$(b-3)/(a+1) \times (3/4) = -1$$

$$(3b-9)/(4a+4) = -1$$

$$3b - 9 = -4a - 4 \quad 4a +$$

$$3b = 5 \dots\dots(1)$$

Point  $(a, b)$  lies on the line  $3x - 4y = 16$

$$3a - 4b = 16 \dots\dots(2)$$

Solving equations (1) and (2), we get a

$$= 68/25 \text{ and } b = -49/25$$

$\therefore$  The co-ordinates of the foot of perpendicular is  $(68/25, -49/25)$

**15. The perpendicular from the origin to the line  $y = mx + c$  meets it at the point  $(-1, 2)$ . Find the values of  $m$  and  $c$ .**

**Solution:**

Given:

The perpendicular from the origin meets the given line at  $(-1, 2)$ .

The equation of line is  $y = mx + c$

The line joining the points  $(0, 0)$  and  $(-1, 2)$  is perpendicular to the given line.

So, the slope of the line joining  $(0, 0)$  and  $(-1, 2) = 2/(-1) = -2$  Slope of the given line is  $m$ .  $m \times (-2) = -1$   $m = 1/2$

Since, point  $(-1, 2)$  lies on the given line,

$$y = mx + c \quad 2 = 1/2 \times (-1) + c \quad c = 2 + 1/2$$

$$= 5/2$$

$\therefore$  The values of  $m$  and  $c$  are  $1/2$  and  $5/2$  respectively.

**16. If  $p$  and  $q$  are the lengths of perpendiculars from the origin to the lines  $x \cos \theta - y \sin \theta = k \cos 2\theta$  and  $x \sec \theta + y \operatorname{cosec} \theta = k$ , respectively, prove that  $p^2 + 4q^2 = k^2$**

**Solution:**

Given:

The equations of given lines are

$$x \cos \theta - y \sin \theta = k \cos 2\theta \dots\dots\dots(1)$$

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$$x \sec \theta + y \operatorname{cosec} \theta = k \dots\dots\dots (2)$$

Perpendicular distance (d) of a line  $Ax + By + C = 0$  from a point  $(x_1, y_1)$  is given by

$$d = \frac{|Ax_1 + By_1 + C|}{\sqrt{A^2 + B^2}}$$

So now, compare equation (1) to the general equation of line i.e.,  $Ax + By + C = 0$ , we get

$$A = \cos \theta, B = -\sin \theta, \text{ and } C = -k \cos 2\theta$$

It is given that p is the length of the perpendicular from (0, 0) to line (1).

$$p = \frac{|A \times 0 + B \times 0 + C|}{\sqrt{A^2 + B^2}} = \frac{|C|}{\sqrt{A^2 + B^2}} = \frac{|-k \cos 2\theta|}{\sqrt{\cos^2 \theta + \sin^2 \theta}} = k \cos 2\theta$$

$$p = k \cos 2\theta$$

Let us square on both sides we get,

$$p^2 = k^2 \cos^2 2\theta \dots\dots\dots (3)$$

Now, compare equation (2) to the general equation of line i.e.,  $Ax + By + C = 0$ , we get

$$A = \sec \theta, B = \operatorname{cosec} \theta, \text{ and } C = -k$$

It is given that q is the length of the perpendicular from (0, 0) to line (2)

$$\begin{aligned} q &= \frac{|A \times 0 + B \times 0 + C|}{\sqrt{A^2 + B^2}} \\ &= \frac{|C|}{\sqrt{A^2 + B^2}} \\ &= \frac{|-k|}{\sqrt{\sec^2 \theta + \operatorname{cosec}^2 \theta}} \\ &= \frac{k}{\sqrt{\sec^2 \theta + \operatorname{cosec}^2 \theta}} \\ &= \frac{k}{\sqrt{\frac{1}{\cos^2 \theta} + \frac{1}{\sin^2 \theta}}} = \frac{k \cos \theta \sin \theta}{\sqrt{\cos^2 \theta + \sin^2 \theta}} = k \cos \theta \sin \theta \end{aligned}$$

$$q = k \cos \theta \sin \theta$$

Multiply both sides by 2, we get

$$2q = 2k \cos \theta \sin \theta = k \times 2 \sin \theta \cos \theta$$

$$2q = k \sin 2\theta$$

Squaring both sides, we get

$$4q^2 = k^2 \sin^2 2\theta \dots\dots\dots (4)$$

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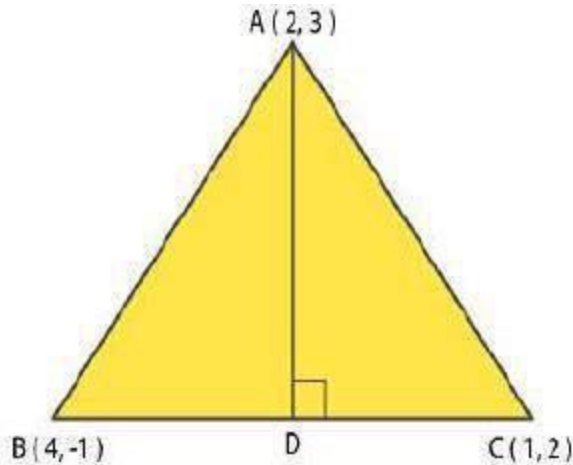
Now add (3) and (4) we get  $p^2 +$

$$4q^2 = k^2 \cos^2 2\theta + k^2 \sin^2 2\theta$$

$$p^2 + 4q^2 = k^2 (\cos^2 2\theta + \sin^2 2\theta) \text{ [Since, } \cos^2 2\theta + \sin^2 2\theta = 1]$$

$$\therefore p^2 + 4q^2 = k^2 \text{ Hence proved.}$$

**17. In the triangle ABC with vertices A (2, 3), B (4, -1) and C (1, 2), find the equation and length of altitude from the vertex A. Solution:**



Let AD be the altitude of triangle ABC from vertex

A. So, AD is perpendicular to BC Given:

Vertices A (2, 3), B (4, -1) and C (1, 2)

Let slope of line BC =  $m_1$

$$m_1 = \frac{-1 - 2}{4 - 1} \quad m_1 = -1$$

Let slope of line AD be  $m_2$

AD is perpendicular to BC

$$m_1 \times m_2 = -1 \quad -1 \times m_2 = -1$$

$$m_2 = 1$$

The equation of the line passing through point (2, 3) and having a slope of 1

$$\text{is } y - 3 = 1 \times (x - 2) \quad y - 3 = x - 2$$

$$y - x = 1$$

Equation of the altitude from vertex A =  $y - x = 1$

Length of AD = Length of the perpendicular from A (2, 3) to BC Equation of BC is

$$y + 1 = -1 \times (x - 4) \quad y$$

$$+ 1 = -x + 4$$

$$x + y - 3 = 0 \dots\dots\dots(1)$$

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Perpendicular distance (d) of a line  $Ax + By + C = 0$  from a point  $(x_1, y_1)$  is given by

$$d = \frac{|Ax_1 + By_1 + C|}{\sqrt{A^2 + B^2}}$$

Now compare equation (1) to the general equation of line i.e.,  $Ax + By + C = 0$ , we get

$$\text{Length of AD} = \frac{|1 \times 2 + 1 \times 3 - 3|}{\sqrt{1^2 + 1^2}} = \frac{|2|}{\sqrt{2}} = \sqrt{2} \text{ units}$$

[where,  $A = 1$ ,  $B = 1$  and  $C = -3$ ]

$\therefore$  The equation and the length of the altitude from vertex A are  $y - x = 1$  and  $\sqrt{2}$  units respectively.

**18. If p is the length of perpendicular from the origin to the line whose intercepts on the axes are a and b, then show that  $1/p^2 = 1/a^2 + 1/b^2$  Solution:**

Equation of a line whose intercepts on the axes are a and b is  $x/a + y/b = 1$  or

$$bx + ay = ab$$

$$bx + ay - ab = 0 \dots\dots\dots(1)$$

Perpendicular distance (d) of a line  $Ax + By + C = 0$  from a point  $(x_1, y_1)$  is given by

$$d = \frac{|Ax_1 + By_1 + C|}{\sqrt{A^2 + B^2}}$$

Now compare equation (1) to the general equation of line i.e.,  $Ax + By + C = 0$ , we get

$$A = b, B = a \text{ and } C = -ab$$

If p is the length of the perpendicular from point  $(x_1, y_1) = (0, 0)$  to line (1), we get

$$\begin{aligned} p &= \frac{|A \times 0 + B \times 0 - ab|}{\sqrt{a^2 + b^2}} \\ &= \frac{|-ab|}{\sqrt{a^2 + b^2}} \end{aligned}$$

Now square on both the sides we get

$$p^2 = \frac{(-ab)^2}{a^2 + b^2}$$

$$\frac{1}{p^2} = \frac{a^2 + b^2}{a^2 b^2}$$

$$\frac{1}{p^2} = \frac{a^2}{a^2 b^2} + \frac{b^2}{a^2 b^2}$$

$\therefore 1/p^2 = 1/a^2 + 1/b^2$  Hence proved.

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## MISCELLANEOUS EXERCISE

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1. Find the values of  $k$  for which the line  $(k - 3)x - (4 - k^2)y + k^2 - 7k + 6 = 0$  is (a) Parallel to the x-axis, (b) Parallel to the y-axis, (c) Passing through the origin.

**Solution:**

It is given that

$$(k - 3)x - (4 - k^2)y + k^2 - 7k + 6 = 0 \dots (1)$$

- (a) Here if the line is parallel to the x-axis

Slope of the line = Slope of the x-axis

It can be written as

$$(4 - k^2)y = (k - 3)x + k^2 - 7k + 6 = 0$$

We get

$$y = \frac{(k - 3)}{(4 - k^2)}x + \frac{k^2 - 7k + 6}{(4 - k^2)}$$

Which is of the form  $y = mx + c$

Here the slope of the given line

$$= \frac{(k - 3)}{(4 - k^2)}$$

Consider the slope of x-axis = 0

$$\frac{(k - 3)}{(4 - k^2)} = 0$$

By further calculation

$$k - 3 = 0 \quad k = 3$$

Hence, if the given line is parallel to the x-axis, then the value of  $k$  is 3.

- (b) Here if the line is parallel to the y-axis, it is vertical and the slope will be undefined.  
So the slope of the given line

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$$= \frac{(k-3)}{(4-k^2)}$$

Here,

$$\frac{(k-3)}{(4-k^2)} \text{ is undefined at } k^2 = 4$$

$$k^2 = 4$$

$$k = \pm 2$$

Hence, if the given line is parallel to the y-axis, then the value of k is  $\pm 2$ . (c)

Here if the line is passing through (0, 0) which is the origin satisfies the given equation of line.

$$(k-3)(0) - (4-k^2)(0) + k^2 - 7k + 6 = 0$$

By further calculation

$$k^2 - 7k + 6 = 0$$

Separating the terms

$$k^2 - 6k - k + 6 = 0 \text{ We}$$

get

$$(k-6)(k-1) = 0$$

$$= 1 \text{ or } 6$$

Hence, if the given line is passing through the origin, then the value of k is either 1 or 6.

**2. Find the values of  $\theta$  and p, if the equation  $x \cos \theta + y \sin \theta = p$  is the normal form of the line  $\sqrt{3}x + y + 2 = 0$ . Solution:**

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It is given that

$$\sqrt{3}x + y + 2 = 0$$

It can be reduced as

$$\sqrt{3}x + y + 2 = 0$$

$$-\sqrt{3}x - y = 2$$

By dividing both sides by  $\sqrt{(-\sqrt{3})^2 + (-1)^2} = 2$ , we get

$$-\frac{\sqrt{3}}{2}x - \frac{1}{2}y = \frac{2}{2}$$

It can be written as

$$\left(-\frac{\sqrt{3}}{2}\right)x + \left(-\frac{1}{2}\right)y = 1 \quad \dots(1)$$

By comparing equation (1) to  $x \cos \theta + y \sin \theta = p$ , we get

$$\cos \theta = -\frac{\sqrt{3}}{2}, \sin \theta = -\frac{1}{2}, \text{ and } p = 1$$

Here the values of  $\sin \theta$  and  $\cos \theta$  are negative

$$\theta = \pi + \frac{\pi}{6} = \frac{7\pi}{6}$$

Hence, the respective values of  $\theta$  and  $p$  are  $7\pi/6$  and 1.

**3. Find the equations of the lines, which cut-off intercepts on the axes whose sum and product are 1 and -6, respectively.**

**Solution:**

Consider the intercepts cut by the given lines on a and b axes.

$$a + b = 1 \quad \dots\dots (1) \quad ab$$

$$= -6 \quad \dots\dots (2)$$

By solving both the equations we get a

$$= 3 \text{ and } b = -2 \text{ or } a = -2 \text{ and } b = 3$$

We know that the equation of the line whose intercepts on a and b axes is

$$\frac{x}{a} + \frac{y}{b} = 1 \text{ or } bx + ay - ab = 0$$

Case I –  $a = 3$  and  $b = -2$

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So the equation of the line is  $-2x + 3y + 6 = 0$ , i.e.  $2x - 3y = 6$ .

Case II –  $a = -2$  and  $b = 3$

So the equation of the line is  $3x - 2y + 6 = 0$ , i.e.  $-3x + 2y = 6$

Hence, the required equation of the lines are  $2x - 3y = 6$  and  $-3x + 2y = 6$ .

#### 4. What are the points on the y-axis whose distance from the line $x/3 + y/4 = 1$ is 4 units. Solution:

Consider  $(0, b)$  as the point on the y-axis whose distance from line  $x/3 + y/4 = 1$  is 4 units.

It can be written as  $4x + 3y - 12 = 0$  ..... (1)

By comparing equation (1) to the general equation of line  $Ax + By + C = 0$ , we get  $A = 4$ ,  $B = 3$  and  $C = -12$

We know that the perpendicular distance ( $d$ ) of a line  $Ax + By + C = 0$  from  $(x_1, y_1)$  is written as

$$d = \frac{|Ax_1 + By_1 + C|}{\sqrt{A^2 + B^2}}$$

If  $(0, b)$  is the point on the y-axis whose distance from line  $x/3 + y/4 = 1$  is 4 units, then

$$4 = \frac{|4(0) + 3(b) - 12|}{\sqrt{4^2 + 3^2}}$$

By further calculation

$$4 = \frac{|3b - 12|}{5}$$

By cross multiplication

$$20 = |3b - 12|$$

We get

$$20 = \pm (3b - 12)$$

$$\text{Here } 20 = (3b - 12) \text{ or } 20 = -(3b - 12)$$

It can be written as

$$3b = 20 + 12 \text{ or } 3b = -20 + 12$$

So we get

$$b = 32/3 \text{ or } b = -8/3$$

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Hence, the required points are  $(0, 32/3)$  and  $(0, -8/3)$ .

**5. Find the perpendicular distance from the origin to the line joining the points  $(\cos \theta, \sin \theta)$  and  $(\cos \phi, \sin \phi)$ .**

**Solution:**

Here the equation of the line joining the points  $(\cos \theta, \sin \theta)$  and  $(\cos \phi, \sin \phi)$  is written as

$$y - \sin \theta = \frac{\sin \phi - \sin \theta}{\cos \phi - \cos \theta} (x - \cos \theta)$$

By cross multiplication

$$y(\cos \phi - \cos \theta) - \sin \theta(\cos \phi - \cos \theta) = x(\sin \phi - \sin \theta) - \cos \theta(\sin \phi - \sin \theta)$$

By multiplying the terms we get

$$x(\sin \theta - \sin \phi) + y(\cos \phi - \cos \theta) + \cos \theta \sin \phi - \cos \theta \sin \theta - \sin \theta \cos \phi + \sin \theta \cos \theta = 0$$

On further simplification

$$x(\sin \theta - \sin \phi) + y(\cos \phi - \cos \theta) + \sin(\phi - \theta) = 0$$

So we get

$$Ax + By + C = 0, \text{ where } A = \sin \theta - \sin \phi, B = \cos \phi - \cos \theta, \text{ and } C = \sin(\phi - \theta)$$

We know that the perpendicular distance (d) of a line  $Ax + By + C = 0$  from  $(x_1, y_1)$  is written as

$$d = \frac{|Ax_1 + By_1 + C|}{\sqrt{A^2 + B^2}}$$

So the perpendicular distance (d) of the given line from  $(x_1, y_1) = (0, 0)$  is

$$d = \frac{|(\sin \theta - \sin \phi)(0) + (\cos \phi - \cos \theta)(0) + \sin(\phi - \theta)|}{\sqrt{(\sin \theta - \sin \phi)^2 + (\cos \phi - \cos \theta)^2}}$$

By expanding using formula

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$$= \frac{|\sin(\phi - \theta)|}{\sqrt{\sin^2 \theta + \sin^2 \phi - 2 \sin \theta \sin \phi + \cos^2 \phi + \cos^2 \theta - 2 \cos \phi \cos \theta}}$$

Grouping of terms

$$= \frac{|\sin(\phi - \theta)|}{\sqrt{(\sin^2 \theta + \cos^2 \theta) + (\sin^2 \phi + \cos^2 \phi) - 2(\sin \theta \sin \phi + \cos \theta \cos \phi)}}$$

By further simplification

$$= \frac{|\sin(\phi - \theta)|}{\sqrt{1 + 1 - 2(\cos(\phi - \theta))}}$$

Taking out 2 as common

$$= \frac{|\sin(\phi - \theta)|}{\sqrt{2(1 - \cos(\phi - \theta))}}$$

Using the formula

$$= \frac{|\sin(\phi - \theta)|}{\sqrt{2 \left( 2 \sin^2 \left( \frac{\phi - \theta}{2} \right) \right)}}$$

We get

$$= \frac{|\sin(\phi - \theta)|}{2 \sin \left( \frac{\phi - \theta}{2} \right)}$$

**6. Find the equation of the line parallel to y-axis and drawn through the point of intersection of the lines  $x - 7y + 5 = 0$  and  $3x + y = 0$ .**

**Solution:**

Here the equation of any line parallel to the y-axis is of the form

$x = a$  ..... (1) Two given lines are  $x - 7y + 5 = 0$  ..... (2)  $3x + y = 0$  ..... (3)

By solving equations (2) and (3) we get x

$= -5/22$  and  $y = 15/22$

$(-5/22, 15/22)$  is the point of intersection of lines (2) and (3)

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If the line  $x = a$  passes through point  $(-5/22, 15/22)$  we get  $a = -5/22$

Hence, the required equation of the line is  $x = -5/22$ .

**7. Find the equation of a line drawn perpendicular to the line  $x/4 + y/6 = 1$  through the point, where it meets the y-axis.**

**Solution:**

It is given that

$$x/4 + y/6 = 1$$

We

can write it as

$$3x + 2y - 12 = 0$$

So

we get

$$y = -3/2 x + 6, \text{ which is of the form } y = mx + c$$

Here the slope of the given line  $= -3/2$

So the slope of line perpendicular to the given line  $= -1/(-3/2) = 2/3$

Consider the given line intersect the y-axis at  $(0, y)$  By substituting  $x$  as zero in the equation of the given line

$$y/6 = 1 \quad y = 6$$

Hence, the given line intersects the y-axis at  $(0, 6)$

We know that the equation of the line that has a slope of  $2/3$  and passes through point  $(0, 6)$  is

$$(y - 6) = 2/3 (x - 0)$$

By further calculation

$$3y - 18 = 2x$$

So we get

$$2x - 3y + 18 = 0$$

Hence, the required equation of the line is  $2x - 3y + 18 = 0$ .

**8. Find the area of the triangle formed by the lines  $y - x = 0$ ,  $x + y = 0$  and  $x - k = 0$ .**

**Solution:**



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It is given that  $y -$

$$x = 0 \dots\dots (1) \quad x +$$

$$y = 0 \dots\dots (2) \quad x -$$

$$k = 0 \dots\dots (3)$$

Here the point of intersection of

Lines (1) and (2) is

$$x = 0 \text{ and } y = 0$$

Lines (2) and (3) is

$$x = k \text{ and } y = -k$$

Lines (3) and (1) is

$$x = k \text{ and } y = k$$

So the vertices of the triangle formed by the three given lines are  $(0, 0)$ ,  $(k, -k)$  and  $(k, k)$

Here the area of triangle whose vertices are  $(x_1, y_1)$ ,  $(x_2, y_2)$  and  $(x_3, y_3)$  is

$$\frac{1}{2} |x_1 (y_2 - y_3) + x_2 (y_3 - y_1) + x_3 (y_1 - y_2)|$$

So the area of triangle formed by the three given lines

$$= \frac{1}{2} |0 (-k - k) + k (k - 0) + k (0 + k)| \text{ square units}$$

By further calculation

$$= \frac{1}{2} |k^2 + k^2| \text{ square units}$$

So we get

$$= \frac{1}{2} |2k^2|$$

$$= k^2 \text{ square units}$$

**9. Find the value of  $p$  so that the three lines  $3x + y - 2 = 0$ ,  $px + 2y - 3 = 0$  and  $2x - y - 3 = 0$  may intersect at one point.**

**Solution:**

It is given that  $3x + y -$

$$2 = 0 \dots\dots (1) \quad px + 2y$$

$$- 3 = 0 \dots\dots (2)$$

$$2x - y - 3 = 0 \dots\dots (3)$$

By solving equations (1) and (3) we get  $x$

$$= 1 \text{ and } y = -1$$

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Here the three lines intersect at one point and the point of intersection of lines (1) and (3) will also satisfy line (2)  $p(1) + 2(-1) - 3 = 0$  By further calculation  $p - 2 - 3 = 0$  So we get

$$p = 5$$

Hence, the required value of  $p$  is 5.

**10. If three lines whose equations are  $y = m_1x + c_1$ ,  $y = m_2x + c_2$  and  $y = m_3x + c_3$  are concurrent, then show that  $m_1(c_2 - c_3) + m_2(c_3 - c_1) + m_3(c_1 - c_2) = 0$ . Solution:**

It is given that  $y =$

$$m_1x + c_1 \dots (1) \quad y =$$

$$m_2x + c_2 \dots (2) \quad y =$$

$$m_3x + c_3 \dots (3)$$

By subtracting equation (1) from (2) we get

$$0 = (m_2 - m_1)x + (c_2 - c_1)$$

$$(m_1 - m_2)x = c_2 - c_1$$

So we get

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### Straight Lines

$$x = \frac{c_2 - c_1}{m_1 - m_2}$$

By substituting this value in equation (1) we get

$$y = m_1 \left( \frac{c_2 - c_1}{m_1 - m_2} \right) + c_1$$

By multiplying the terms

$$y = \frac{m_1 c_2 - m_1 c_1}{m_1 - m_2} + c_1$$

Taking LCM

$$y = \frac{m_1 c_2 - m_1 c_1 + m_1 c_1 - m_2 c_1}{m_1 - m_2}$$

On further simplification

$$y = \frac{m_1 c_2 - m_2 c_1}{m_1 - m_2}$$

Here

$$\left( \frac{c_2 - c_1}{m_1 - m_2}, \frac{m_1 c_2 - m_2 c_1}{m_1 - m_2} \right) \text{ is the point of intersection of lines (1) and (2)}$$

Lines (1), (2) and (3) are concurrent. So the point of intersection of lines (1) and (2) will satisfy equation (3)

$$\frac{m_1 c_2 - m_2 c_1}{m_1 - m_2} = m_3 \left( \frac{c_2 - c_1}{m_1 - m_2} \right) + c_3$$

By multiplying the terms and taking LCM

$$\frac{m_1 c_2 - m_2 c_1}{m_1 - m_2} = \frac{m_3 c_2 - m_3 c_1 + c_3 m_1 - c_3 m_2}{m_1 - m_2}$$

By cross multiplication

$$m_1 c_2 - m_2 c_1 - m_3 c_2 + m_3 c_1 - c_3 m_1 + c_3 m_2 = 0$$

Taking out the common terms

$$m_1 (c_2 - c_3) + m_2 (c_3 - c_1) + m_3 (c_1 - c_2) = 0$$

$$\text{Therefore, } m_1 (c_2 - c_3) + m_2 (c_3 - c_1) + m_3 (c_1 - c_2) = 0.$$

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**11. Find the equation of the lines through the point (3, 2) which make an angle of  $45^\circ$  with the line  $x - 2y = 3$ .**

**Solution:**

Consider  $m_1$  as the slope of the required line. It can be written as

$y = \frac{1}{2}x - \frac{3}{2}$  which is of the form  $y = mx + c$

So the slope of the given line  $m_2 = \frac{1}{2}$

We know that the angle between the required line and line  $x - 2y = 3$  is  $45^\circ$

If  $\theta$  is the acute angle between lines  $l_1$  and  $l_2$  with slopes  $m_1$  and  $m_2$

$$\tan \theta = \left| \frac{m_2 - m_1}{1 + m_1 m_2} \right|$$

We get

$$\tan 45^\circ = \left| \frac{m_1 - m_2}{1 + m_1 m_2} \right|$$

Substituting the values

$$1 = \left| \frac{\frac{1}{2} - m_1}{1 + \frac{m_1}{2}} \right|$$

By taking LCM

$$1 = \left| \frac{\left( \frac{1 - 2m_1}{2} \right)}{\frac{2 + m_1}{2}} \right|$$

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On further calculation

$$1 = \left| \frac{1 - 2m_1}{2 + m_1} \right|$$

We get

$$1 = \pm \left( \frac{1 - 2m_1}{2 + m_1} \right)$$

Here

$$1 = \frac{1 - 2m_1}{2 + m_1} \text{ or } 1 = - \left( \frac{1 - 2m_1}{2 + m_1} \right)$$

It can be written as

$$2 + m_1 = 1 - 2m_1 \text{ or } 2 + m_1 = -1 + 2m_1$$

$$m_1 = -1/3 \text{ or } m_1 = 3$$

Case I –  $m_1 = 3$

Here the equation of the line passing through (3, 2) and having a slope 3 is

$$y - 2 = 3(x - 3) \text{ By further calculation}$$

$$y - 2 = 3x - 9$$

So we get

$$3x - y = 7$$

Case II –  $m_1 = -1/3$

Here the equation of the line passing through (3, 2) and having a slope -1/3 is

$$y - 2 = -1/3(x - 3) \text{ By further calculation}$$

$$3y - 6 = -x + 3 \text{ So}$$

we get

$$x + 3y = 9$$

Hence, the equations of the lines are  $3x - y = 7$  and  $x + 3y = 9$ .

**12. Find the equation of the line passing through the point of intersection of the lines  $4x + 7y - 3 = 0$  and  $2x - 3y + 1 = 0$  that has equal intercepts on the axes. Solution:**

Consider the equation of the line having equal intercepts on the axes as

$$x/a + y/a = 1 \text{ It can be written as } x + y = a \dots (1)$$

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By solving equations  $4x + 7y - 3 = 0$  and  $2x - 3y + 1 = 0$  we get  $x = 1/13$  and  $y = 5/13$

$(1/13, 5/13)$  is the point of intersection of two given lines

We know that equation (1) passes through point  $(1/13, 5/13)$

$$1/13 + 5/13 = a$$

$$= 6/13$$

So the equation (1) passes through  $(1/13, 5/13)$

$$1/13 + 5/13 = a$$

We get  $a =$

$$6/13$$

Here the equation (1) becomes

$$x + y = 6/13 \quad 13x + 13y = 6$$

Hence, the required equation of the line is  $13x + 13y = 6$ .

**13. Show that the equation of the line passing through the origin and making an**

**angle  $\theta$  with the line  $y = mx + c$  is  $\frac{y}{x} = \frac{m \pm \tan \theta}{1 \mp m \tan \theta}$ .**

**Solution:**

Consider  $y = m_1x$  as the equation of the line passing through the origin

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It is given that the line makes an angle  $\theta$  with line  $y = mx + c$ , then angle  $\theta$  is written as

$$\tan \theta = \left| \frac{m_1 - m}{1 + m_1 m} \right|$$

By substituting the values

$$\tan \theta = \left| \frac{\frac{y}{x} - m}{1 + \frac{y}{x} m} \right|$$

We get

$$\tan \theta = \pm \left( \frac{\frac{y}{x} - m}{1 + \frac{y}{x} m} \right)$$

Here

$$\tan \theta = \frac{\frac{y}{x} - m}{1 + \frac{y}{x} m} \text{ or } \tan \theta = - \left( \frac{\frac{y}{x} - m}{1 + \frac{y}{x} m} \right)$$

Case I –

$$\tan \theta = \frac{\frac{y}{x} - m}{1 + \frac{y}{x} m}$$

We can write it as

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$$\tan \theta + \frac{y}{x} m \tan \theta = \frac{y}{x} - m$$

By further simplification

$$m + \tan \theta = \frac{y}{x} (1 - m \tan \theta)$$

So we get

$$\frac{y}{x} = \frac{m + \tan \theta}{1 - m \tan \theta}$$

Case II –

$$\tan \theta = - \left( \frac{\frac{y}{x} - m}{1 + \frac{y}{x} m} \right)$$

We can write it as

$$\tan \theta + \frac{y}{x} m \tan \theta = - \frac{y}{x} + m$$

By further simplification

$$\frac{y}{x} (1 + m \tan \theta) = m - \tan \theta$$

So we get

$$\frac{y}{x} = \frac{m - \tan \theta}{1 + m \tan \theta}$$

Hence, the required line is given by

$$\frac{y}{x} = \frac{m \pm \tan \theta}{1 \mp m \tan \theta}$$

**14. In what ratio, the line joining  $(-1, 1)$  and  $(5, 7)$  is divided by the line  $x + y = 4$ ?**

**Solution:**



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We know that the equation of the line joining the points  $(-1, 1)$  and  $(5, 7)$  is given by

$$y - 1 = \frac{7-1}{5+1}(x+1)$$

By further calculation

$$y - 1 = \frac{6}{6}(x+1)$$

So we get

$$x - y + 2 = 0 \dots\dots (1)$$

So the equation of the given line is

$$x + y - 4 = 0 \dots\dots (2)$$

Here the point of intersection of lines (1) and (2) is given by

$$x = 1 \text{ and } y = 3$$

Consider  $(1, 3)$  divide the line segment joining  $(-1, 1)$  and  $(5, 7)$  in the ratio  $1: k$ .

Using the section formula

$$(1, 3) = \left( \frac{k(-1) + 1(5)}{1+k}, \frac{k(1) + 1(7)}{1+k} \right)$$

By further calculation

$$(1, 3) = \left( \frac{-k+5}{1+k}, \frac{k+7}{1+k} \right)$$

So we get

$$\frac{-k+5}{1+k} = 1, \frac{k+7}{1+k} = 3$$

We can write it as

$$\frac{-k+5}{1+k} = 1$$

By cross multiplication

$$-k + 5 = 1 + k$$

We get  $2k$

$$= 4$$

$$k = 2$$

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Hence, the line joining the points  $(-1, 1)$  and  $(5, 7)$  is divided by the line  $x + y = 4$  in the ratio  $1: 2$ .

**15. Find the distance of the line  $4x + 7y + 5 = 0$  from the point  $(1, 2)$  along the line  $2x - y = 0$ .**

**Solution:**

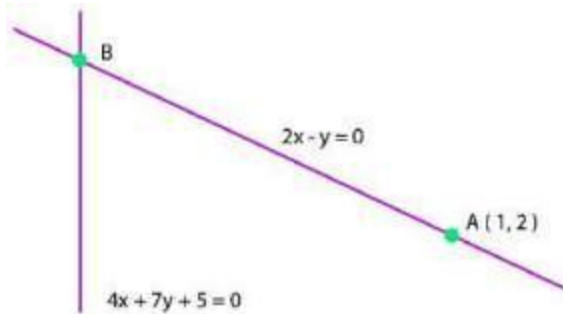
It is given that  $2x - y =$

$$0 \dots\dots (1) \quad 4x + 7y + 5 =$$

$$0 \dots\dots (2)$$

Here  $A(1, 2)$  is a point on the line (1)

Consider B as the point of intersection of lines (1) and (2)



By solving equations (1) and (2) we get  $x = -5/18$  and  $y = -5/9$

So the coordinates of point B are  $(-5/18, -5/9)$

From distance formula the distance between A and B

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$$AB = \sqrt{\left(1 + \frac{5}{18}\right)^2 + \left(2 + \frac{5}{9}\right)^2} \text{ units}$$

By taking LCM

$$= \sqrt{\left(\frac{23}{18}\right)^2 + \left(\frac{23}{9}\right)^2} \text{ units}$$

It can be written as

$$= \sqrt{\left(\frac{23}{2 \times 9}\right)^2 + \left(\frac{23}{9}\right)^2} \text{ units}$$

So we get

$$= \sqrt{\left(\frac{23}{9}\right)^2 \left(\frac{1}{2}\right)^2 + \left(\frac{23}{9}\right)^2} \text{ units}$$

By taking the common terms out

$$= \sqrt{\left(\frac{23}{9}\right)^2 \left(\frac{1}{4} + 1\right)} \text{ units}$$

We get

$$= \frac{23}{9} \sqrt{\frac{5}{4}} \text{ units}$$

$$= \frac{23}{9} \times \frac{\sqrt{5}}{2} \text{ units}$$

So we get

$$= \frac{23\sqrt{5}}{18} \text{ units}$$

Hence, the required distance is  $\frac{23\sqrt{5}}{18}$  units.

**16. Find the direction in which a straight line must be drawn through the point  $(-1, 2)$  so that its point of intersection with the line  $x + y = 4$  may be at a distance of 3 units from this point.**

**Solution:**

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Consider  $y = mx + c$  as the line passing through the point  $(-1, 2)$  So we get

$$2 = m(-1) + c$$

By further calculation

$$2 = -m + c$$

$$c = m + 2$$

Substituting the value of  $c$

$$y = mx + m + 2 \dots\dots (1)$$

So the given line is  $x$

$$+ y = 4 \dots\dots (2)$$

By solving both the equations we get

$$x = \frac{2-m}{m+1} \text{ and } y = \frac{5m+2}{m+1}$$

$$\left( \frac{2-m}{m+1}, \frac{5m+2}{m+1} \right) \text{ is the point of intersection of lines (1) and (2)}$$

Here the point is at a distance of 3 units from  $(-1, 2)$

From distance formula

$$\sqrt{\left( \frac{2-m}{m+1} + 1 \right)^2 + \left( \frac{5m+2}{m+1} - 2 \right)^2} = 3$$

Squaring on both sides

$$\left( \frac{2-m+m+1}{m+1} \right)^2 + \left( \frac{5m+2-2m-2}{m+1} \right)^2 = 3^2$$

By further calculation

$$\frac{9}{(m+1)^2} + \frac{9m^2}{(m+1)^2} = 9$$

Dividing the equation by 9

$$\frac{1+m^2}{(m+1)^2} = 1$$

By cross multiplication

$$1 + m^2 = m^2 + 1 + 2m$$

So we get  $2m$

$$= 0$$

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$$m = 0$$

Hence, the slope of the required line must be zero i.e. the line must be parallel to the x-axis.

**17. The hypotenuse of a right angled triangle has its ends at the points (1, 3) and (-4, 1). Find the equation of the legs (perpendicular sides) of the triangle. Solution:**

Consider ABC as the right angles triangle where  $\angle C = 90^\circ$

Here infinity such lines are present. m is the slope of AC

So the slope of BC =  $-1/m$

Equation of AC -  $y - 3$

=  $m(x - 1)$  By cross  
multiplication

$$x - 1 = 1/m(y - 3)$$

Equation of BC -  $y - 1$

=  $-1/m(x + 4)$  By cross  
multiplication

$$x + 4 = -m(y - 1)$$

By considering values of m we get

If  $m = 0$ ,

So we get

$$y - 3 = 0, x + 4 = 0$$

If  $m = \infty$ , So

we get

$$x - 1 = 0, y - 1 = 0 \text{ we get } x = 1, y = 1$$

**18. Find the image of the point (3, 8) with respect to the line  $x + 3y = 7$  assuming the line to be a plane mirror.**

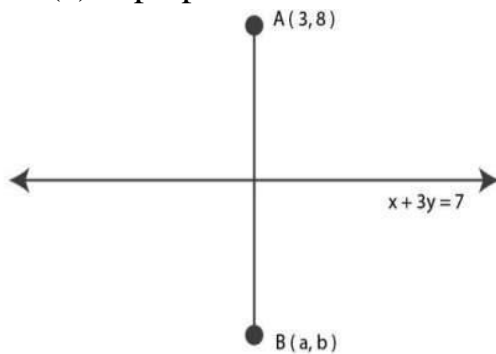
**Solution:**

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It is given that  $x +$

$$3y = 7 \dots\dots (1)$$

Consider B (a, b) as the image of point A (3, 8) So  
line (1) is perpendicular bisector of AB.



Here

$$\text{Slope of AB} = \frac{b-8}{a-3}$$

$$\text{slope of line (1)} = -\frac{1}{3}$$

Line (1) is perpendicular to AB

$$\left(\frac{b-8}{a-3}\right) \times \left(-\frac{1}{3}\right) = -1$$

By further calculation

$$\frac{b-8}{3a-9} = 1$$

By cross multiplication

$$b - 8 = 3a - 9$$

$$3a - b = 1 \dots\dots (2)$$

We know that

$$\text{Mid-point of AB} = \left(\frac{a+3}{2}, \frac{b+8}{2}\right)$$

So the mid-point of line segment AB will satisfy line (1)

From equation (1)

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$$\left(\frac{a+3}{2}\right) + 3\left(\frac{b+8}{2}\right) = 7$$

By further calculation

$$a + 3 + 3b + 24 = 14$$

On further simplification

$$a + 3b = -13 \dots\dots (3)$$

By solving equations (2) and (3) we get

$$a = -1 \text{ and } b = -4$$

Hence, the image of the given point with respect to the given line is  $(-1, -4)$ .

**19. If the lines  $y = 3x + 1$  and  $2y = x + 3$  are equally inclined to the line  $y = mx + 4$ , find the value of  $m$ .**

**Solution:**

It is given that

$$y = 3x + 1 \dots\dots (1)$$

$$2y = x + 3 \dots\dots (2)$$

$$y = mx + 4 \dots\dots (3)$$

Here the slopes of

$$\text{Line (1), } m_1 = 3$$

$$\text{Line (2), } m_2 = \frac{1}{2}$$

$$\text{Line (3), } m_3 = m$$

We know that the lines (1) and (2) are equally inclined to line (3) which means that the angle between lines (1) and (3) equals the angle between lines (2) and (3).

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$$\left| \frac{m_1 - m_3}{1 + m_1 m_3} \right| = \left| \frac{m_2 - m_3}{1 + m_2 m_3} \right|$$

Substituting the values we get

$$\left| \frac{3 - m}{1 + 3m} \right| = \left| \frac{\frac{1}{2} - m}{1 + \frac{1}{2}m} \right|$$

By taking LCM

$$\left| \frac{3 - m}{1 + 3m} \right| = \left| \frac{1 - 2m}{m + 2} \right|$$

It can be written as

$$\frac{3 - m}{1 + 3m} = \pm \left( \frac{1 - 2m}{m + 2} \right)$$

Here

$$\frac{3 - m}{1 + 3m} = \frac{1 - 2m}{m + 2} \text{ or } \frac{3 - m}{1 + 3m} = - \left( \frac{1 - 2m}{m + 2} \right)$$

If

$$\frac{3 - m}{1 + 3m} = \frac{1 - 2m}{m + 2}$$

By cross multiplication

$$(3 - m)(m + 2) = (1 - 2m)(1 + 3m)$$

On further calculation

$$-m^2 + m + 6 = 1 + m - 6m^2$$

So we get

$5m^2 + 5 = 0$  Dividing the equation by 5  $m^2 + 1 = 0$   $m = \sqrt{-1}$ , which is not real. Therefore, this case is not possible.

If



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$$\frac{3-m}{1+3m} = -\left(\frac{1-2m}{m+2}\right)$$

By cross multiplication

$$(3-m)(m+2) = -(1-2m)(1+3m)$$

On further calculation

$$-m^2 + m + 6 = -(1 + m - 6m^2)$$

So we get

$$7m^2 - 2m - 7 = 0$$

Here we get

$$m = \frac{2 \pm \sqrt{4 - 4(7)(-7)}}{2(7)}$$

By further simplification

$$m = \frac{2 \pm 2\sqrt{1+49}}{14}$$

We can write it as

$$m = \frac{1 \pm 5\sqrt{2}}{7}$$

Hence, the required value of m is

$$\frac{1 \pm 5\sqrt{2}}{7}$$

**20. If sum of the perpendicular distances of a variable point P (x, y) from the lines  $x + y - 5 = 0$  and  $3x - 2y + 7 = 0$  is always 10. Show that P must move on a line.**

**Solution:**

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It is given that

$$x + y - 5 = 0 \dots (1)$$

$$3x - 2y + 7 = 0 \dots (2)$$

Here the perpendicular distances of P (x, y) from lines (1) and (2) are written as

$$d_1 = \frac{|x + y - 5|}{\sqrt{(1)^2 + (1)^2}} \text{ and } d_2 = \frac{|3x - 2y + 7|}{\sqrt{(3)^2 + (-2)^2}}$$

So we get

$$d_1 = \frac{|x + y - 5|}{\sqrt{2}} \text{ and } d_2 = \frac{|3x - 2y + 7|}{\sqrt{13}}$$

We know that  $d_1 + d_2 = 10$

Substituting the values

$$\frac{|x + y - 5|}{\sqrt{2}} + \frac{|3x - 2y + 7|}{\sqrt{13}} = 10$$

By further calculation

$$\sqrt{13}|x + y - 5| + \sqrt{2}|3x - 2y + 7| - 10\sqrt{26} = 0$$

It can be written as

$$\sqrt{13}(x + y - 5) + \sqrt{2}(3x - 2y + 7) - 10\sqrt{26} = 0$$

Now by assuming  $(x + y - 5)$  and  $(3x - 2y + 7)$  are positive

$$\sqrt{13}x + \sqrt{13}y - 5\sqrt{13} + 3\sqrt{2}x - 2\sqrt{2}y + 7\sqrt{2} - 10\sqrt{26} = 0$$

Taking out the common terms

$$x(\sqrt{13} + 3\sqrt{2}) + y(\sqrt{13} - 2\sqrt{2}) + (7\sqrt{2} - 5\sqrt{13} - 10\sqrt{26}) = 0, \text{ which is the equation of a line.}$$

In the same way we can find the equation of line for any signs of  $(x + y - 5)$  and  $(3x - 2y + 7)$

Hence, point P must move on a line.

**21. Find equation of the line which is equidistant from parallel lines  $9x + 6y - 7 = 0$  and  $3x + 2y + 6 = 0$ .**

**Solution:**

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It is given that

$$9x + 6y - 7 = 0 \dots\dots (1)$$

$$3x + 2y + 6 = 0 \dots\dots (2)$$

Consider P (h, k) be the arbitrary point that is equidistant from lines (1) and (2)

Here the perpendicular distance of P (h, k) from line (1) is written as

$$d_1 = \frac{|9h + 6k - 7|}{(9)^2 + (6)^2} = \frac{|9h + 6k - 7|}{\sqrt{117}} = \frac{|9h + 6k - 7|}{3\sqrt{13}}$$

Similarly the perpendicular distance of P (h, k) from line (2) is written as

$$d_2 = \frac{|3h + 2k + 6|}{\sqrt{(3)^2 + (2)^2}} = \frac{|3h + 2k + 6|}{\sqrt{13}}$$

We know that P (h, k) is equidistant from lines (1) and (2)  $d_1 = d_2$

Substituting the values

$$\frac{|9h + 6k - 7|}{3\sqrt{13}} = \frac{|3h + 2k + 6|}{\sqrt{13}}$$

By further calculation

$$|9h + 6k - 7| = 3|3h + 2k + 6|$$

It can be written as

$$|9h + 6k - 7| = \pm 3(3h + 2k + 6)$$

Here

$$9h + 6k - 7 = 3(3h + 2k + 6) \text{ or } 9h + 6k - 7 = -3(3h + 2k + 6)$$

$$9h + 6k - 7 = 3(3h + 2k + 6) \text{ is not possible as}$$

$$9h + 6k - 7 = 3(3h + 2k + 6)$$

By further calculation

$$-7 = 18$$

We know that

$$9h + 6k - 7 = -3(3h + 2k + 6)$$

By multiplication  $9h + 6k$

$$-7 = -9h - 6k - 18$$

We get

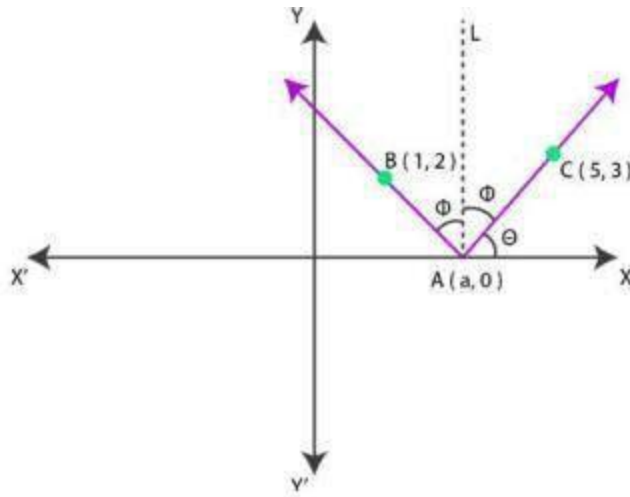
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$$18h + 12k + 11 = 0$$

Hence, the required equation of the line is  $18x + 12y + 11 = 0$ .

**22. A ray of light passing through the point (1, 2) reflects on the x-axis at point A and the reflected ray passes through the point (5, 3). Find the coordinates of A.**

**Solution:**



Consider the coordinates of point A as  $(a, 0)$

Construct a line (AL) which is perpendicular to the x-axis

Here the angle of incidence is equal to angle of reflection

$$\angle BAL = \angle CAL = \phi$$

$$\angle CAX = \theta$$

It can be written as

$$\angle OAB = 180^\circ - (\theta + 2\phi) = 180^\circ - [\theta + 2(90^\circ - \theta)]$$

On further calculation

$$= 180^\circ - \theta - 180^\circ + 2\theta$$

$$= \theta$$

So we get

$$\angle BAX = 180^\circ - \theta$$

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$$\text{slope of line AC} = \frac{3-0}{5-a}$$

$$\tan \theta = \frac{3}{5-a} \quad \dots(1)$$

$$\text{Slope of line AB} = \frac{2-0}{1-a}$$

We get

$$\tan(180^\circ - \theta) = \frac{2}{1-a}$$

By further calculation

$$-\tan \theta = \frac{2}{1-a}$$

$$\tan \theta = \frac{2}{a-1} \quad \dots(2)$$

From equations (1) and (2) we get

$$\frac{3}{5-a} = \frac{2}{a-1}$$

By cross multiplication

$$3a - 3 = 10 - 2a$$

We

$$\text{get}$$

$a = 13/5$   
Hence, the coordinates of point A are  $(13/5, 0)$ .

**23. Prove that the product of the lengths of the perpendiculars drawn from the points  $(\sqrt{a^2 - b^2}, 0)$  and  $(-\sqrt{a^2 - b^2}, 0)$  to the line  $\frac{x}{a} \cos \theta + \frac{y}{b} \sin \theta = 1$  is  $b^2$ .**

**Solution:**

It is given that

$$\frac{x}{a} \cos \theta + \frac{y}{b} \sin \theta = 1$$

We can write it as

$$bx \cos \theta + ay \sin \theta - ab = 0 \quad \dots (1)$$

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Here the length of the perpendicular from point  $(\sqrt{a^2 - b^2}, 0)$  to line (1)

$$p_1 = \frac{|b \cos \theta (\sqrt{a^2 - b^2}) + a \sin \theta (0) - ab|}{\sqrt{b^2 \cos^2 \theta + a^2 \sin^2 \theta}} = \frac{|b \cos \theta \sqrt{a^2 - b^2} - ab|}{\sqrt{b^2 \cos^2 \theta + a^2 \sin^2 \theta}} \quad \dots(2)$$

Similarly the length of the perpendicular from point  $(-\sqrt{a^2 - b^2}, 0)$  to line (2)

$$p_2 = \frac{|b \cos \theta (-\sqrt{a^2 - b^2}) + a \sin \theta (0) - ab|}{\sqrt{b^2 \cos^2 \theta + a^2 \sin^2 \theta}} = \frac{|b \cos \theta \sqrt{a^2 - b^2} + ab|}{\sqrt{b^2 \cos^2 \theta + a^2 \sin^2 \theta}} \quad \dots(3)$$

By multiplying equations (2) and (3) we get

$$p_1 p_2 = \frac{|b \cos \theta \sqrt{a^2 - b^2} - ab| |b \cos \theta \sqrt{a^2 - b^2} + ab|}{(\sqrt{b^2 \cos^2 \theta + a^2 \sin^2 \theta})^2}$$

We get

$$= \frac{|(b \cos \theta \sqrt{a^2 - b^2} - ab)(b \cos \theta \sqrt{a^2 - b^2} + ab)|}{(b^2 \cos^2 \theta + a^2 \sin^2 \theta)}$$

From the formula

$$= \frac{|(b \cos \theta \sqrt{a^2 - b^2})^2 - (ab)^2|}{(b^2 \cos^2 \theta + a^2 \sin^2 \theta)}$$

By squaring the numerator we get

$$= \frac{|b^2 \cos^2 \theta (a^2 - b^2) - a^2 b^2|}{(b^2 \cos^2 \theta + a^2 \sin^2 \theta)}$$

By expanding using formula

$$= \frac{|a^2 b^2 \cos^2 \theta - b^4 \cos^2 \theta - a^2 b^2|}{b^2 \cos^2 \theta + a^2 \sin^2 \theta}$$

Taking out the common terms

$$= \frac{b^2 |a^2 \cos^2 \theta - b^2 \cos^2 \theta - a^2|}{b^2 \cos^2 \theta + a^2 \sin^2 \theta}$$

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We get

$$= \frac{b^2 |a^2 \cos^2 \theta - b^2 \cos^2 \theta - a^2 \sin^2 \theta - a^2 \cos^2 \theta|}{b^2 \cos^2 \theta + a^2 \sin^2 \theta}$$

Here  $\sin^2 \theta + \cos^2 \theta = 1$

$$= \frac{b^2 |-(b^2 \cos^2 \theta + a^2 \sin^2 \theta)|}{b^2 \cos^2 \theta + a^2 \sin^2 \theta}$$

So we get

$$= \frac{b^2 (b^2 \cos^2 \theta + a^2 \sin^2 \theta)}{(b^2 \cos^2 \theta + a^2 \sin^2 \theta)}$$

$$= b^2$$

Therefore, it is proved.

**24. A person standing at the junction (crossing) of two straight paths represented by the equations  $2x - 3y + 4 = 0$  and  $3x + 4y - 5 = 0$  wants to reach the path whose equation is  $6x - 7y + 8 = 0$  in the least time. Find equation of the path that he should follow. Solution:**

It is given that

$$2x - 3y + 4 = 0 \dots\dots (1)$$

$$3x + 4y - 5 = 0 \dots\dots (2)$$

$$6x - 7y + 8 = 0 \dots\dots (3)$$

Here the person is standing at the junction of the paths represented by lines (1) and (2).

By solving equations (1) and (2) we get  $x = -1/17$  and  $y = 22/17$

Hence, the person is standing at point  $(-1/17, 22/17)$ .

We know that the person can reach path (3) in the least time if he walks along the perpendicular line to (3) from point  $(-1/17, 22/17)$

Here the slope of the line (3) =  $6/7$

We get the slope of the line perpendicular to line (3) =  $-1/(6/7) = -7/6$

So the equation of line passing through  $(-1/17, 22/17)$  and having a slope of  $-7/6$  is written as

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$$\left(y - \frac{22}{17}\right) = -\frac{7}{6}\left(x + \frac{1}{17}\right)$$

By further calculation

$$6(17y - 22) = -7(17x + 1)$$

By multiplication

$$102y - 132 = -119x - 7$$

We get

$$119x + 102y = 125$$

Therefore, the path that the person should follow is  $119x + 102y = 125$ .