

NCERT Solution For Class 10 Maths Chapter 7 Coordinate Geometry

Exercise 7.1

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1. Find the distance between the following pairs of points:

- (i) (2, 3), (4, 1)
 (ii) (-5, 7), (-1, 3)
 (iii) (a, b), (-a, -b)

Solution:

Distance formula to find the distance between two points (x_1, y_1) and (x_2, y_2) is, say d ,

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \quad \text{OR} \quad d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

(i) Distance between (2, 3), (4, 1)

$$d = \sqrt{(4 - 2)^2 + (1 - 3)^2} = \sqrt{(2)^2 + (-2)^2} = \sqrt{8} = 2\sqrt{2}$$

(ii) Distance between (-5, 7), (-1, 3)

$$d = \sqrt{(-1 + 5)^2 + (3 - 7)^2} = \sqrt{(4)^2 + (-4)^2} = \sqrt{32} = 4\sqrt{2}$$

(iii) Distance between (a, b), (-a, -b)

$$d = \sqrt{(-a - a)^2 + (-b - b)^2} = \sqrt{(-2a)^2 + (-2b)^2} = \sqrt{4a^2 + 4b^2} = 2\sqrt{a^2 + b^2}$$

2. Find the distance between the points (0, 0) and (36, 15). Can you now find the distance between the two towns A and B discussed in Section 7.2.

Solution: Let us consider, town A at point (0, 0). Therefore, town B will be at point (36, 15).

Distance between points (0, 0) and (36, 15)

$$d = \sqrt{(36 - 0)^2 + (15 - 0)^2} = \sqrt{(36)^2 + (15)^2} = \sqrt{1296 + 225} = \sqrt{1521} = 39$$

The distance between town A and B will be 39 km.

3. Determine if the points (1, 5), (2, 3) and (-2, -11) are collinear.

Solution: The sum of the lengths of any two line segments is equal to the length of the third line segment then all three points are collinear. Consider, A = (1, 5) B = (2, 3) and C = (-2, -11)

Find the distance between points; say AB, BC and CA

$$AB = \sqrt{(2 - 1)^2 + (3 - 5)^2} = \sqrt{(1)^2 + (-2)^2} = \sqrt{1 + 4} = \sqrt{5}$$

$$BC = \sqrt{(-2 - 2)^2 + (-11 - 3)^2} = \sqrt{(-4)^2 + (-14)^2} = \sqrt{16 + 196} = \sqrt{212}$$

$$CA = \sqrt{(-2 - 1)^2 + (-11 - 5)^2} = \sqrt{(-3)^2 + (-16)^2} = \sqrt{9 + 256} = \sqrt{265}$$

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Since $AB + BC \neq CA$

Therefore, the points (1, 5), (2, 3), and (-2, -11) are not collinear.

4. Check whether (5, -2), (6, 4) and (7, -2) are the vertices of an isosceles triangle.

Solution:

Since two sides of any isosceles triangle are equal. To check whether given points are vertices of an isosceles triangle, we will find the distance between all the points.

Let the points (5, -2), (6, 4), and (7, -2) are representing the vertices A, B, and C respectively.

$$AB = \sqrt{(6-5)^2 + (4+2)^2} = \sqrt{(-1)^2 + (6)^2} = \sqrt{37}$$

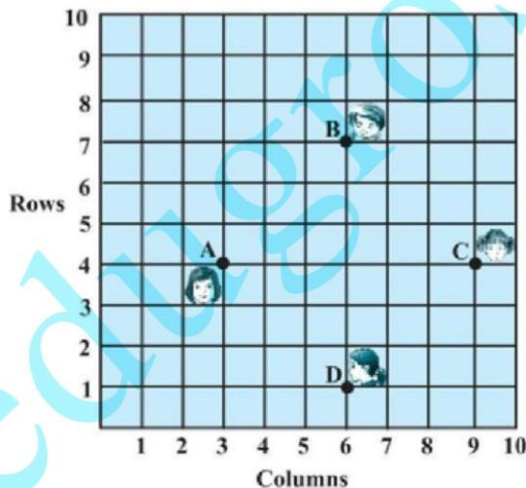
$$BC = \sqrt{(7-6)^2 + (-2-4)^2} = \sqrt{(-1)^2 + (6)^2} = \sqrt{37}$$

$$CA = \sqrt{(7-5)^2 + (-2+2)^2} = \sqrt{(-2)^2 + (0)^2} = 2$$

Here $AB = BC = \sqrt{37}$

This implies, whether given points are vertices of an isosceles triangle.

5. In a classroom, 4 friends are seated at the points A, B, C and D as shown in Fig. 7.8. Champa and Chameli walk into the class and after observing for a few minutes Champa asks Chameli, "Don't you think ABCD is a square?" Chameli disagrees. Using distance formula, find which of them is correct.



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Solution:

From figure, the coordinates of points A, B, C and D are (3, 4), (6, 7), (9, 4) and (6,1). Find distance between points using distance formula, we get

$$AB = \sqrt{(6-3)^2 + (7-4)^2} = \sqrt{9+9} = 3\sqrt{2}$$

$$BC = \sqrt{(9-6)^2 + (4-7)^2} = \sqrt{9+9} = 3\sqrt{2}$$

$$CD = \sqrt{(6-9)^2 + (1-4)^2} = \sqrt{9+9} = 3\sqrt{2}$$

$$DA = \sqrt{(6-3)^2 + (1-4)^2} = \sqrt{9+9} = 3\sqrt{2}$$

$$AB = BC = CD = DA = 3\sqrt{2}$$

All sides are of equal length. Therefore, ABCD is a square and hence, Champa was correct.

6. Name the type of quadrilateral formed, if any, by the following points, and give reasons for your answer:

(i) (- 1, - 2), (1, 0), (- 1, 2), (- 3, 0)

(ii) (- 3, 5), (3, 1), (0, 3), (- 1, - 4)

(iii) (4, 5), (7, 6), (4, 3), (1, 2)

Solution:

- (i) Let the points (- 1, - 2), (1, 0), (- 1, 2), and (- 3, 0) be representing the vertices A, B, C, and D of the given quadrilateral respectively.

$$AB = \sqrt{(1+1)^2 + (0+2)^2} = \sqrt{4+4} = 2\sqrt{2}$$

$$BC = \sqrt{(-1-1)^2 + (2-0)^2} = \sqrt{4+4} = 2\sqrt{2}$$

$$CD = \sqrt{(-3+1)^2 + (0-2)^2} = \sqrt{4+4} = 2\sqrt{2}$$

$$DA = \sqrt{(-3+1)^2 + (0-2)^2} = \sqrt{4+4} = 2\sqrt{2}$$

$$AC = \sqrt{(-1+1)^2 + (2+2)^2} = \sqrt{0+16} = 4$$

$$BD = \sqrt{(-3-1)^2 + (0-0)^2} = \sqrt{16+0} = 4$$

Side length = AB = BC = CD = DA = $2\sqrt{2}$

Diagonal Measure = AC = BD = 4

Therefore, the given points are the vertices of a square.

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- (ii) Let the points $(-3, 5)$, $(3, 1)$, $(0, 3)$, and $(-1, -4)$ be representing the vertices A, B, C, and D of the given quadrilateral respectively.

$$AB = \sqrt{(-3-3)^2 + (1-5)^2} = \sqrt{36+16} = 2\sqrt{13}$$

$$BC = \sqrt{(0-3)^2 + (3-1)^2} = \sqrt{9+4} = \sqrt{13}$$

$$CD = \sqrt{(-1-0)^2 + (-4-3)^2} = \sqrt{1+49} = 5\sqrt{2}$$

$$AD = \sqrt{(-1+3)^2 + (-4-5)^2} = \sqrt{4+81} = \sqrt{85}$$

All sides of this quadrilateral are of different lengths. Therefore, it can be said that it is a general quadrilateral.

- (iii) Let the points $(4, 5)$, $(7, 6)$, $(4, 3)$, and $(1, 2)$ be representing the vertices A, B, C, and D of the given quadrilateral respectively.

$$AB = \sqrt{(7-4)^2 + (6-5)^2} = \sqrt{9+1} = \sqrt{10}$$

$$BC = \sqrt{(4-7)^2 + (3-6)^2} = \sqrt{9+9} = \sqrt{18}$$

$$CD = \sqrt{(1-4)^2 + (2-3)^2} = \sqrt{9+1} = \sqrt{10}$$

$$AD = \sqrt{(1-4)^2 + (2-5)^2} = \sqrt{9+9} = \sqrt{18}$$

$$AC \text{ (diagonal)} = \sqrt{(4-4)^2 + (3-5)^2} = \sqrt{0+4} = 2$$

$$BD \text{ (diagonal)} = \sqrt{(1-7)^2 + (2-6)^2} = \sqrt{36+16} = 2\sqrt{13}$$

Opposite sides of this quadrilateral are of the same length. However, the diagonals are of different lengths. Therefore, the given points are the vertices of a parallelogram.

7. Find the point on the x-axis which is equidistant from $(2, -5)$ and $(-2, 9)$.

Solution:

To find a point on x-axis. Therefore, its y-coordinate will be 0. Let the point on x-axis be $(x, 0)$. Consider $A = (x, 0)$; $B = (2, -5)$ and $C = (-2, 9)$.

$$AB = \sqrt{(2-x)^2 + (-5-0)^2} = \sqrt{(2-x)^2 + 25}$$

$$AC = \sqrt{(-2-x)^2 + (9-0)^2} = \sqrt{(-2-x)^2 + 81}$$

Since both the distance are equal in measure, so $AB = AC$

$$\sqrt{(2-x)^2 + 25} = \sqrt{(-2-x)^2 + 81}$$

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Simplify the above equation,
Remove square root by taking square both the sides, we get

$$\begin{aligned}(2-x)^2 + 25 &= (-2-x)^2 + 81 \\ x^2 + 4 - 4x + 25 &= x^2 + 4 + 4x + 81 \\ 8x &= 25 - 81 = -56 \quad x = -7\end{aligned}$$

Therefore, the point is $(-7, 0)$.

8. Find the values of y for which the distance between the points $P(2, -3)$ and $Q(10, y)$ is 10 units.

Solution:

Given: Distance between $(2, -3)$ and $(10, y)$ is 10.

Using distance formula,

$$PQ = \sqrt{(10-2)^2 + (y+3)^2} = \sqrt{(8)^2 + (y+3)^2}$$

Since $PQ = 10$

$$\sqrt{(8)^2 + (y+3)^2} = 10$$

Simplify the above equation and find the value of y .

Squaring both sides,

$$64 + (y+3)^2 = 100$$

$$(y+3)^2 = 36 \quad y+3 = \pm 6$$

$$y+3 = +6 \quad \text{or} \quad y+3 = -6$$

Therefore, $y = 3$ or -9 .

9. If $Q(0, 1)$ is equidistant from $P(5, -3)$ and $R(x, 6)$, find the values of x . Also find the distance QR and PR . Solution:

Given: $Q(0, 1)$ is equidistant from $P(5, -3)$ and $R(x, 6)$, which means $PQ = QR$ Step

1: Find the distance between PQ and QR using distance formula,

$$PQ = \sqrt{(5-0)^2 + (-3-1)^2} = \sqrt{(-5)^2 + (-4)^2} = \sqrt{25+16} = \sqrt{41}$$

$$QR = \sqrt{(0-x)^2 + (1-6)^2} = \sqrt{(-x)^2 + (-5)^2} = \sqrt{x^2+25}$$

Step 2: Use $PQ = QR$

Squaring both the sides, to omit square root

$$41 = x^2 + 25$$

$$x^2 = 16 \quad x =$$

$$\pm 4$$

$$x = 4 \quad \text{or} \quad x = -4$$

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Coordinates of Point R will be R (4, 6) OR R (-4, 6),

If R (4, 6), then QR

$$QR = \sqrt{(0-4)^2 + (1-6)^2} = \sqrt{(4)^2 + (-5)^2} = \sqrt{16+25} = \sqrt{41}$$

$$PR = \sqrt{(5-4)^2 + (-3-6)^2} = \sqrt{(1)^2 + (9)^2} = \sqrt{1+81} = \sqrt{82}$$

If R (-4, 6), then

$$QR = \sqrt{(0+4)^2 + (1-6)^2} = \sqrt{(4)^2 + (-5)^2} = \sqrt{16+25} = \sqrt{41}$$

$$PR = \sqrt{(5+4)^2 + (-3-6)^2} = \sqrt{(9)^2 + (9)^2} = \sqrt{81+81} = 9\sqrt{2}$$

10. Find a relation between x and y such that the point (x, y) is equidistant from the point (3, 6) and (-3, 4).

Solution:

Point (x, y) is equidistant from (3, 6) and (-3, 4).

$$\sqrt{(x-3)^2 + (y-6)^2} = \sqrt{(x-(-3))^2 + (y-4)^2}$$

$$\sqrt{(x-3)^2 + (y-6)^2} = \sqrt{(x+3)^2 + (y-4)^2}$$

Squaring both sides, $(x-3)^2 + (y-6)^2 = (x+3)^2 + (y-4)^2$

$$+9-6x+y^2+36-12y = x^2+9+6x+y^2+16-8y$$

$$36-16 = 6x+6x+12y-8y$$

$$20 = 12x+4y$$

$$3x+y = 5$$

$$3x+y-5 = 0$$

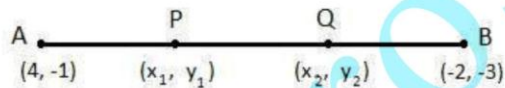
Exercise 7.2

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1. Find the coordinates of the point which divides the join of (-1, 7) and (4, -3) in the ratio 2:3.**Solution:**

Let P(x, y) be the required point. Using the section formula, we get x
 $= (2 \times 4 + 3 \times (-1)) / (2 + 3) = (8 - 3) / 5 = 1$
 $y = (2 \times (-3) + 3 \times 7) / (2 + 3) = (-6 + 21) / 5 = 3$

Therefore, the point is (1, 3).

2. Find the coordinates of the points of trisection of the line segment joining (4, -1) and (-2, -3).**Solution:**

Let P (x₁, y₁) and Q (x₂, y₂) are the points of trisection of the line segment joining the given points i.e., AP = PQ = QB

Therefore, point P divides AB internally in the ratio 1:2.

$$x_1 = (1 \times (-2) + 2 \times 4) / 3 = (-2 + 8) / 3 = 6 / 3 = 2$$

$$y_1 = (1 \times (-3) + 2 \times (-1)) / (1 + 2) = (-3 - 2) / 3 = -5 / 3$$

Therefore: P (x₁, y₁) = P(2, -5/3)

Point Q divides AB internally in the ratio 2:1.

$$x_2 = (2 \times (-2) + 1 \times 4) / (2 + 1) = (-4 + 4) / 3 = 0$$

$$y_2 = (2 \times (-3) + 1 \times (-1)) / (2 + 1) = (-6 - 1) / 3 = -7 / 3$$

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The coordinates of the point Q is $(0, -7/3)$

3. To conduct Sports

Day activities, in your rectangular shaped school ground ABCD, lines have been drawn with chalk powder at a distance of 1 m each. 100 flower pots have been placed at a distance of 1 m from each other along AD, as shown in the following figure. Niharika runs $1/4$ th the distance AD on the 2nd line and posts a green flag. Preet runs $1/5$ th the distance AD on the eighth line and posts a red flag. What is the distance between both the flags? If Rashmi has to post a blue flag exactly halfway between the line segment joining the two flags, where should she post her flag?

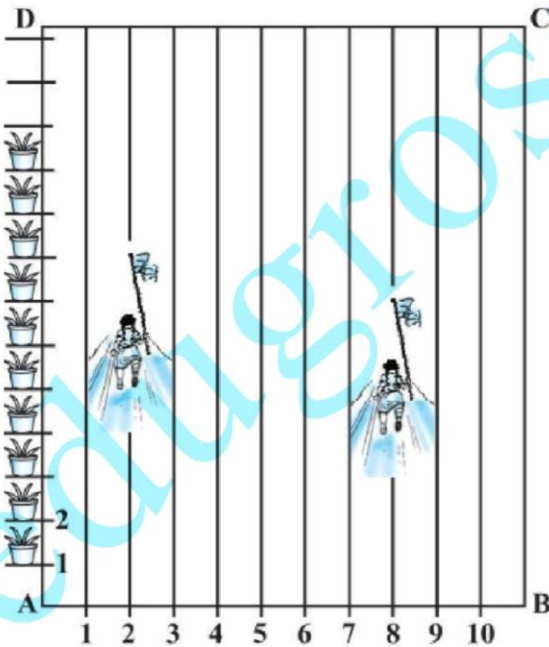


Fig. 7.12

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Solution:

From the given instruction, we observed that Niharika posted the green flag at $\frac{1}{4}$ th of the distance AD i.e., $(\frac{1}{4} \times 100)m = 25m$ from the starting point of 2nd line. Therefore, the coordinates of this point are (2, 25).

Similarly, Preet posted red flag at $\frac{1}{5}$ of the distance AD i.e., $(\frac{1}{5} \times 100) m = 20m$ from the starting point of 8th line. Therefore, the coordinates of this point are (8, 20).

Distance between these flags can be calculated by using distance formula,

The point at which Rashmi should post her blue flag is the mid- point of the line joining these points.

Let say this point be P(x, y). $x = \frac{(2+8)}{2} = \frac{10}{2} = 5$ and $y = \frac{(20+25)}{2} = \frac{45}{2}$

Hence, P(x, y) = (5, $\frac{45}{2}$)

Therefore, Rashmi should post her blue flag at $\frac{45}{2} = 22.5m$ on 5th line.

4. Find the ratio in which the line segment joining the points (-3, 10) and (6, -8) is divided by (-1, 6).**Solution:**

Consider the ratio in which the line segment joining (-3, 10) and (6, -8) is divided by point (-1, 6) be k : 1.

Therefore, $-1 = \frac{6k-3}{k+1}$

$$-k - 1 = 6k - 3$$

$$7k = 2$$

$$k = \frac{2}{7}$$

Therefore, the required ratio is 2:7.

5. Find the ratio in which the line segment joining A (1, -5) and B (-4, 5) is divided by the x-axis. Also find the coordinates of the point of division.**Solution:**

Let the ratio in which the line segment joining A (1, -5) and B (-4, 5) is divided by x-axis be k : 1.

Therefore, the coordinates of the point of division, say P(x, y) is $(\frac{-4k+1}{k+1}, \frac{5k-5}{k+1})$.

We know that y-coordinate of any point on x-axis is 0.

$$\text{Therefore, } \frac{5k-5}{k+1} = 0$$

$$5k = 5$$

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or $k = 1$

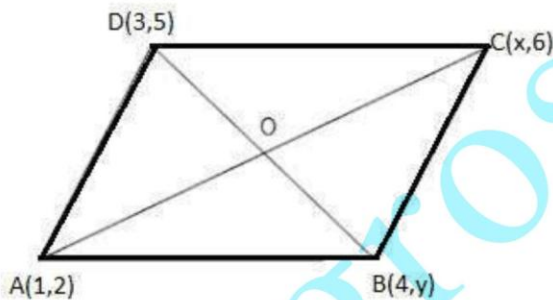
So, x-axis divides the line segment in the ratio 1:1. Now, find the coordinates of the point of division:

$$P(x, y) = \left(\frac{-4(1)+1}{(1+1)}, \frac{(5(1)-5)}{(1+1)} \right) = \left(-\frac{3}{2}, 0 \right)$$

6. If $(1, 2)$, $(4, y)$, $(x, 6)$ and $(3, 5)$ are the vertices of a parallelogram taken in order, find x and y .

Solution:

Let A, B, C and D be the points of a parallelogram : A(1,2), B(4,y), C(x,6) and D(3,5).



Since the diagonals of a parallelogram bisect each other, the midpoint is same. To find the value of x and y , solve for midpoint first.

$$\text{Midpoint of AC} = \left(\frac{(1+x)}{2}, \frac{(2+6)}{2} \right) = \left(\frac{(1+x)}{2}, 4 \right)$$

$$\text{Midpoint of BD} = \left(\frac{(4+3)}{2}, \frac{(5+y)}{2} \right) = \left(\frac{7}{2}, \frac{(5+y)}{2} \right)$$

Midpoint of AC and BD are same, this implies

$$\frac{(1+x)}{2} = \frac{7}{2} \text{ and } 4 = \frac{(5+y)}{2}$$

$$x + 1 = 7 \text{ and } 5 + y = 8$$

$$x = 6 \text{ and } y = 3. \text{ Answer!}$$

7. Find the coordinates of a point A, where AB is the diameter of circle whose centre is $(2, -3)$ and B is $(1,4)$.

Solution:

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Let the coordinates of point A be (x, y) .

Mid-point of AB is $(2, -3)$, which is the centre of the circle.

Coordinate of B = $(1, 4)$

$$(2, -3) = \left(\frac{x+1}{2}, \frac{y+4}{2}\right)$$

$$(x+1)/2 = 2 \text{ and } (y+4)/2 = -3$$

$$x + 1 = 4 \text{ and } y + 4 = -6$$

$$x = 3 \text{ and } y = -10$$

The coordinates of A are $(3, -10)$. Answer!

- 8. If A and B are $(-2, -2)$ and $(2, -4)$, respectively, find the coordinates of P such that $AP = \frac{3}{7} AB$ and P lies on the line segment AB.**

Solution: In the figure, it can be observed that points X, Y, Z are dividing the line segment in a ratio 1:3, 1:1, 3:1 respectively.



The coordinates of point A and B are $(-2, -2)$ and $(2, -4)$ respectively. Since $AP = \frac{3}{7} AB$

Therefore, $AP : PB = 3 : 4$

Point P divides the line segment AB in the ratio 3:4.

$$\text{Coordinate of P} = \left(\frac{3(2) + 4(-2)}{3+4}, \frac{3(-4) + 4(-2)}{3+4}\right) = \left(\frac{6-8}{7}, \frac{-12-8}{7}\right) = \left(-\frac{2}{7}, -\frac{20}{7}\right) \text{ which is required answer.}$$

- 9. Find the coordinates of the points which divide the line segment joining A $(-2, 2)$ and B $(2, 8)$ into four equal parts.**

Solution: Draw a figure, line dividing by 4 points.



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$$\text{Coordinates of X} = \left(\frac{1(2)+3(-2)}{1+3}, \frac{1(8)+3(2)}{1+3} \right) = (-1, 7/2)$$

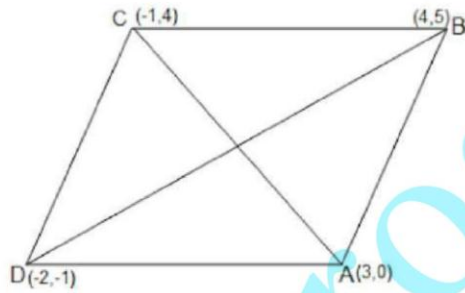
$$\text{Coordinates of Y} = \left(\frac{2(1)-2(1)}{1+1}, \frac{2(1)+8(1)}{1+1} \right) = (0, 0.5)$$

$$\text{Coordinates of Z} = \left(\frac{3(2)+1(-2)}{1+3}, \frac{3(8)+1(2)}{1+3} \right) = (1, 13/2)$$

10. Find the area of a rhombus if its vertices are (3, 0), (4, 5), (-1, 4) and (-2, -1) taken in order.
[Hint: Area of a rhombus = $1/2$ (product of its diagonals)]

Solution:

Let A(3, 0), B (4, 5), C (-1, 4) and D (-2, -1) are the vertices of a rhombus ABCD.



$$\text{Length of diagonal AC} = \sqrt{(3 - (-1))^2 + (0 - 4)^2} = \sqrt{16 + 16} = 4\sqrt{2}$$

$$\text{Length of diagonal BD} = \sqrt{(4 - (-2))^2 + (5 - (-1))^2} = \sqrt{36 + 36} = 6\sqrt{2}$$

$$\text{Therefore, area of rhombus ABCD} = \frac{1}{2} \times 4\sqrt{2} \times 6\sqrt{2} = 24 \text{ square units}$$

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GeometryExercise 7.3

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1. Find the area of the triangle whose vertices are:

- (i) (2, 3), (-1, 0), (2, -4)
(ii) (-5, -1), (3, -5), (5, 2)

Solution:

Area of a triangle formula = $\frac{1}{2} (x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$

(i) Here, $x_1 = 2$, $x_2 = -1$, $x_3 = 2$, $y_1 = 3$, $y_2 = 0$ and $y_3 = -4$

Substitute all the values in the above formula, we get

$$\begin{aligned} \text{Area of triangle} &= \frac{1}{2} [2 \{ 0 - (-4) \} + (-1) \{ (-4) - (3) \} + 2 \{ 3 - 0 \}] \\ &= \frac{1}{2} \{ 8 + 7 + 6 \} = \frac{21}{2} \end{aligned}$$

So area of triangle is $\frac{21}{2}$ square units.

(ii) Here, $x_1 = -5$, $x_2 = 3$, $x_3 = 5$, $y_1 = -1$, $y_2 = -5$ and $y_3 = 2$

$$\begin{aligned} \text{Area of the triangle} &= \frac{1}{2} [-5 \{ (-5) - (2) \} + 3 \{ 2 - (-1) \} + 5 \{ -1 - (-5) \}] \\ &= \frac{1}{2} \{ 35 + 9 + 20 \} = 32 \end{aligned}$$

Therefore, area of the triangle is 32 square units.

2. In each of the following find the value of 'k', for which the points are collinear.

- (i) (7, -2), (5, 1), (3, -k)
(ii) (8, 1), (k, -4), (2, -5)

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Solution:

- (i) For collinear points, area of triangle formed by them is always zero.

Let points (7, -2), (5, 1), and (3, k) are vertices of a triangle.

$$\text{Area of triangle} = \frac{1}{2} [7\{1-k\} + 5\{k-(-2)\} + 3\{(-2)-1\}] = 0$$

$$7 - 7k + 5k + 10 - 9 = 0$$

$$-2k + 8 = 0 \quad k = 4$$

- (ii) For collinear points, area of triangle formed by them is zero.

Therefore, for points (8, 1), (k, -4), and (2, -5), area = 0

$$\frac{1}{2} [8\{-4-(-5)\} + k\{(-5)-(-1)\} + 2\{1-(-4)\}] = 0$$

$$8 - 6k + 10 = 0 \quad 6k$$

$$= 18$$

$$k = 3$$

3. Find the area of the triangle formed by joining the mid-points of the sides of the triangle whose vertices are (0, -1), (2, 1) and (0, 3). Find the ratio of this area to the area of the given triangle.

Solution:

Let the vertices of the triangle be A (0, -1), B (2, 1), C (0, 3).

Let D, E, F be the mid-points of the sides of this triangle.

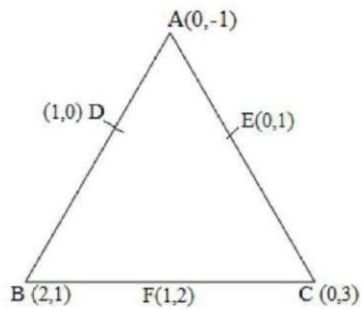
Coordinates of D, E, and F are given by

$$D = \left(\frac{0+2}{2}, \frac{-1+1}{2} \right) = (1, 0)$$

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$$E = \left(\frac{0+2}{2}, \frac{3+1}{2} \right) = (1, 2)$$

$$F = \left(\frac{0+2}{2}, \frac{3+1}{2} \right) = (1, 2)$$



$$\text{Area of a triangle} = \frac{1}{2} (x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$\text{Area of } \triangle DEF = \frac{1}{2} \{1(2-1) + 1(1-0) + 0(0-2)\} = \frac{1}{2} (1+1) = 1$$

Area of $\triangle DEF$ is 1 square units

$$\text{Area of } \triangle ABC = \frac{1}{2}$$

$$[0(1-3) + 2\{3-(-1)\} + 0(-1-1)] = \frac{1}{2} \{8\} = 4$$

Area of $\triangle ABC$ is 4 square units

Therefore, the required ratio is 1:4.

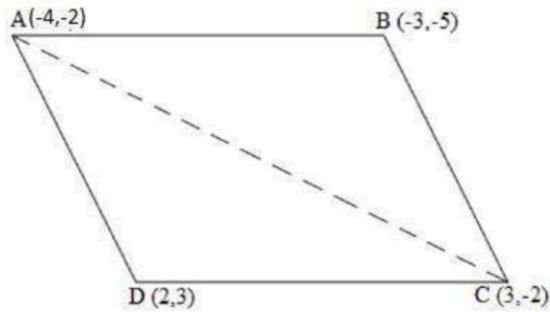
4. Find the area of the quadrilateral whose vertices, taken in order, are

(-4, -2), (-3, -5), (3, -2) and (2, 3).

Solution:

Let the vertices of the quadrilateral be A (-4, -2), B (-3, -5), C (3, -2), and D (2, 3). Join AC and divide quadrilateral into two triangles.

NCERT Solution For Class 10 Maths Chapter 7 Coordinate Geometry



We have two triangles ΔABC and ΔACD .

$$\text{Area of a triangle} = \frac{1}{2} (x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$\text{Area of } \Delta ABC = \frac{1}{2} [(-4) \{(-5) - (-2)\} + (-3) \{(-2) - (-2)\} + 3 \{(-2) - (-5)\}]$$

$$= \frac{1}{2} (12 + 0 + 9)$$

$$= \frac{21}{2} \text{ square units}$$

$$\text{Area of } \Delta ACD = \frac{1}{2} [(-4) \{(-2) - (3)\} + 3\{(3) - (-2)\} + 2 \{(-2) - (-2)\}]$$

$$= \frac{1}{2} (20 + 15 + 0)$$

$$= \frac{35}{2} \text{ square units}$$

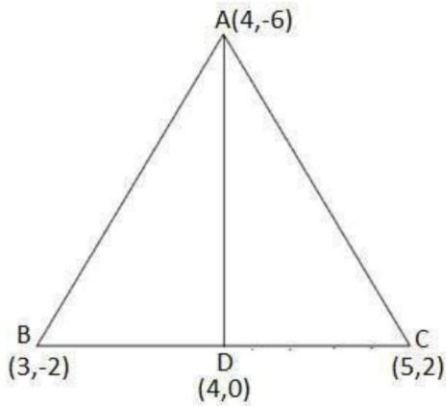
Area of quadrilateral ABCD = Area of ΔABC + Area of ΔACD

$$= (\frac{21}{2} + \frac{35}{2}) \text{ square units} = 28 \text{ square units}$$

5. You have studied in Class IX that a median of a triangle divides it into two triangles of equal areas. Verify this result for ΔABC whose vertices are A (4, -6), B (3, -2) and C (5, 2).

Solution: Let the vertices of the triangle be A (4, -6), B (3, -2), and C (5, 2).

NCERT Solution For Class 10 Maths Chapter 7 Coordinate Geometry



Let D be the mid-point of side BC of $\triangle ABC$. Therefore, AD is the median in $\triangle ABC$.

$$\text{Coordinates of point D} = \text{Midpoint of BC} = \left(\frac{3+5}{2}, \frac{-2+2}{2} \right) = (4, 0)$$

Formula, to find Area of a triangle = $\frac{1}{2} (x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$

$$\text{Now, Area of } \triangle ABD = \frac{1}{2} [(4) \{(-2) - (0)\} + 3\{(0) - (-6)\} + (4) \{(-6) - (-2)\}]$$

$$= \frac{1}{2} (-8 + 18 - 16)$$

$$= -3 \text{ square units}$$

However, area cannot be negative. Therefore, area of $\triangle ABD$ is 3 square units.

$$\text{Area of } \triangle ACD = \frac{1}{2} [(4) \{0 - (2)\} + 4\{(2) - (-6)\} + (5) \{(-6) - (0)\}]$$

$$= \frac{1}{2} (-8 + 32 - 30) = -3 \text{ square units}$$

However, area cannot be negative. Therefore, area of $\triangle ACD$ is 3 square units.

The area of both sides is same. Thus, median AD has divided $\triangle ABC$ in two triangles of equal areas.

NCERT Solution For Class 10 Maths Chapter 7 Coordinate Geometry

1. Determine the ratio in which the line $2x + y - 4 = 0$ divides the line segment joining the points A(2, -2) and B(3, 7).

Solution:

Consider line $2x + y - 4 = 0$ divides line AB joined by the two points A(2, -2) and B(3, 7) in $k : 1$ ratio. Coordinates of point of division can be given as follows:

$$x = \frac{2+3k}{k+1} \text{ and } y = \frac{-2+7k}{k+1}$$

Substituting the values of x and y given equation, i.e. $2x + y - 4 = 0$, we have

$$\frac{2+3k}{k+1} - 2 + 7k - 4 = 0$$

$$\frac{4+6k}{k+1} - 2 + 7k = 4$$

$$4 + 6k - 2 + 7k = 4(k+1)$$

$$-2 + 9k = 0$$

$$\text{Or } k = \frac{2}{9}$$

Hence, the ratio is 2:9.

2. Find the relation between x and y if the points (x, y) , $(1, 2)$ and $(7, 0)$ are collinear.

Solution:

If given points are collinear then area of triangle formed by them must be zero.

Let (x, y) , $(1, 2)$ and $(7, 0)$ are vertices of a triangle,

$$\text{Area of a triangle} = \frac{1}{2} (x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)) = 0$$

$$\frac{1}{2} [x(2 - 0) + 1(0 - y) + 7(y - 2)] = 0$$

$$\Rightarrow 2x - y + 7y - 14 = 0$$

$$\Rightarrow 2x + 6y - 14 = 0$$

$$\Rightarrow x + 3y - 7 = 0. \text{ Which is required result.}$$

NCERT Solution For Class 10 Maths Chapter 7 Coordinate Geometry

3. Find the centre of a circle passing through points (6, -6), (3, -7) and (3, 3).

Solution:

Let A = (6, -6), B = (3, -7), C = (3, 3) are the points on a circle.

If O is the centre, then OA = OB = OC (radii are equal) If

O = (x, y) then

$$OA = \sqrt{(x-6)^2 + (y+6)^2} = OB$$

$$= \sqrt{(x-3)^2 + (y+7)^2}$$

$$OC = \sqrt{(x-3)^2 + (y-3)^2}$$

Choose: OA = OB, we have

$$(x-6)^2 + (y-6)^2 = (x-3)^2 + (y-3)^2$$

$$x^2 + 36 - 12x + y^2 + 36 - 12y = x^2 + 9 - 6x + y^2 + 9 - 6y$$

After simplifying above, we get $-6x = 2y - 14$ (1)

Similarly: OB = OC

$$(x-3)^2 + (y+7)^2 = (x-3)^2 + (y-3)^2$$

$$(y+7)^2 = (y-3)^2$$

$$y^2 + 14y + 49 = y^2 - 6y + 9$$

$$20y = -40 \text{ or}$$

$$y = -2$$

Substituting the value of y in equation (1), we get;

$$-6x = 2y - 14 \quad -6x =$$

$$-4 - 14 = -18 \quad x = 3$$

Hence, centre of the circle located at point (3, -2).

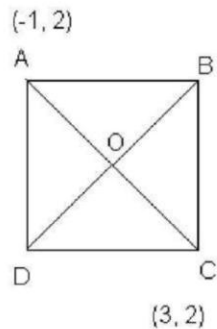
4. The two opposite vertices of a square are (-1, 2) and (3, 2). Find the coordinates of the other two vertices.

Solution:

Let ABCD is a square, where A(-1, 2) and B(3, 2). And Point O is the point of intersection of AC and BD To

Find: Coordinate of points C and D.

NCERT Solution For Class 10 Maths Chapter 7 Coordinate Geometry



Step 1: Find distance between A and C and coordinates of point O.

We know that, diagonals of a square are equal and bisect each other.

$$AC = \sqrt{(3 + 1)^2 + (2 - 2)^2} = 4$$

Coordinates of O can be calculated as follows:

$$x = (3-1)/2 = 1 \text{ and } y = (2+2)/2 = 2$$

So O(1,2)

Step 2: Find the side of the square using Pythagoras theorem

Let a be the side of square and $AC = 4$

From right triangle, ACD, $a = 2\sqrt{2}$

Hence, each side of square = $2\sqrt{2}$

Step 3: Find coordinates of point D

Equate length measure of AD and CD

Say, if coordinate of D are (x_1, y_1) , then

$$AD = \sqrt{(x_1 + 1)^2 + (y_1 - 2)^2}$$

Squaring both sides,

$$AD^2 = (x_1 + 1)^2 + (y_1 - 2)^2$$

$$\text{Similarly, } CD^2 = (x_1 - 3)^2 + (y_1 - 2)^2$$

Since all sides of a square are equal, which means $AD = CD$

$$(x_1 + 1)^2 + (y_1 - 2)^2 = (x_1 - 3)^2 + (y_1 - 2)^2$$

$$x_1^2 + 1 + 2x_1 = x_1^2 + 9 - 6x_1$$

$$8x_1 = 8$$

$$x_1 = 1$$

NCERT Solution For Class 10 Maths Chapter 7 Coordinate Geometry

Value of y_1 can be calculated as follows by using the value of x .

From step 2: each side of square = $2\sqrt{2}$

$$CD^2 = (x_1 - 3)^2 + (y_1 - 2)^2$$

$$8 = (1 - 3)^2 + (y_1 - 2)^2$$

$$y_1 - 2 = 2$$

$$y_1 = 4$$

Hence, $D = (1, 4)$

Step 4: Find coordinates of point B

From line segment, BOD

Coordinates of B can be calculated using coordinates of O; as follows:

Earlier, we had calculated $O = (1, 2)$

Say $B = (x_2, y_2)$ For

BD;

$$x_2 + 1$$

$$1 =$$

$$2$$

$$x_2 = 1$$

$$y_2 + 4$$

$$\text{And } 2 =$$

$$2$$

$$\Rightarrow y_2 = 0$$

Therefore, the coordinates of required points are $B = (1, 0)$ and $D = (1, 4)$

5. The class X students of a secondary school in Krishinagar have been allotted a rectangular plot of land for their gardening activity. Saplings of Gulmohar are planted on the boundary at a distance of 1 m from each other. There is a triangular lawn in the plot as shown in the fig. 7.14. The students are to sow the seeds of flowering plants on the remaining area of the plot.

(i) Taking A as origin, find the coordinates of the vertices of the triangle.

(ii) What will be the coordinates of the vertices of triangle PQR if C is the origin?

Also calculate the areas of the triangles in these cases. What do you observe?

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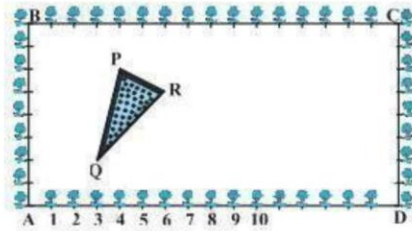


Fig. 7.14

Solution:

(i) Taking A as origin, coordinates of the vertices P, Q and R are,

From figure: P = (4, 6), Q = (3, 2), R (6, 5)

Here AD is the x-axis and AB is the y-axis.

(ii) Taking C as origin,

Coordinates of vertices P, Q and R are (12, 2), (13, 6) and (10, 3) respectively. Here CB is the x-axis and CD is the y-axis.

Find the area of triangles:

Area of triangle PQR in case of origin A:

$$\begin{aligned} \text{Using formula: Area of a triangle} &= \frac{1}{2}(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)) \\ &= \frac{1}{2}[4(2 - 5) + 3(5 - 6) + 6(6 - 2)] \\ &= \frac{1}{2}(-12 - 3 + 24) \\ &= \frac{9}{2} \text{ sq unit} \end{aligned}$$

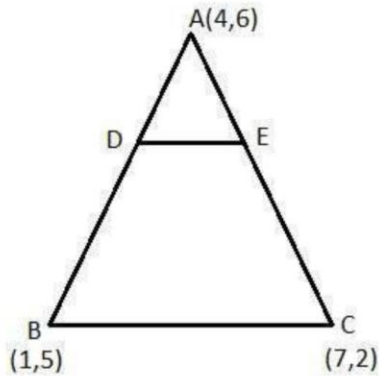
(ii) Area of triangle PQR in case of origin C:

$$\begin{aligned} \text{Area of a triangle} &= \frac{1}{2}(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)) \\ &= \frac{1}{2}[12(6 - 3) + 13(3 - 2) + 10(2 - 6)] \\ &= \frac{1}{2}(36 + 13 - 40) \\ &= \frac{9}{2} \text{ sq unit} \end{aligned}$$

This implies, Area of triangle PQR at origin A = Area of triangle PQR at origin C

Area is same in both case because triangle remains the same no matter which point is considered as origin.

NCERT Solution For Class 10 Maths Chapter 7 Coordinate Geometry



6. The vertices of a ΔABC are A (4, 6), B (1, 5) and C (7, 2). A line is drawn to intersect sides AB and AC at D and E respectively, such that $\frac{AD}{AB} = \frac{AE}{AC} = \frac{1}{4}$. Calculate the area of the ΔADE and compare it with area of ΔABC . (Recall Theorem 6.2 and Theorem 6.6)

$$\frac{AD}{AB} = \frac{AE}{AC} = \frac{1}{4}$$

E respectively, such that $\frac{AD}{AB} = \frac{AE}{AC} = \frac{1}{4}$. Calculate the area of the ΔADE and compare it with area of ΔABC . (Recall Theorem 6.2 and Theorem 6.6)

$$\frac{AD}{AB} = \frac{AE}{AC} = \frac{1}{4}$$

ABC. (Recall Theorem 6.2 and Theorem 6.6)

Solution:

Given: The vertices of a ΔABC are A (4, 6), B (1, 5) and C (7, 2)

$$\frac{AD}{AB} = \frac{AE}{AC} = \frac{1}{4}$$

Point D and Point E divide AB and AC respectively in ratio 1 : 3.

Coordinates of D can be calculated as follows:

$$\frac{AD}{AB} = \frac{AE}{AC} = \frac{1}{4}$$

$$\frac{AD}{AB} = \frac{AE}{AC} = \frac{1}{4}$$

$$\frac{m_1 x_2 + m_2 x_1}{m_1 + m_2} = \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2} = x \text{ and } y =$$

Here $m_1 = 1$ and $m_2 = 3$

Consider line segment AB which is divided by the point D at the ration 1:3.

$$x = \frac{3(4)+1(1)}{4} = \frac{13}{4}$$

$$y = \frac{3(6)+1(5)}{4} = \frac{23}{4}$$

Similarly, Coordinates of E can be calculated as follows:

$$x = \frac{1(7)+3(4)}{4} = \frac{19}{4}$$

$$y = \frac{1(2)+3(6)}{4} = \frac{20}{4} = 5$$

Find Area of triangle:

$$\text{Using formula: Area of a triangle} = \frac{1}{2}(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

Area of triangle ΔABC can be calculated as follows:

NCERT Solution For Class 10 Maths Chapter 7 Coordinate Geometry

$$= \frac{1}{2} [4(5 - 2) + 1(2 - 6) + 7(6 - 5)]$$

$$= \frac{1}{2} (12 - 4 + 7) = 15/2 \text{ sq unit}$$

Area of ΔADE can be calculated as follows:

$$= \frac{1}{2} [4(23/4 - 5) + 13/4(5 - 6) + 19/4(6 - 23/4)]$$

$$= \frac{1}{2} (3 - 13/4 + 19/16)$$

$$= \frac{1}{2} (15/16) = 15/32 \text{ sq unit}$$

Hence, ratio of area of triangle ADE to area of triangle ABC = 1 : 16.

7. Let A (4, 2), B (6, 5) and C (1, 4) be the vertices of ΔABC .

(i) The median from A meets BC at D. Find the coordinates of point D.

(ii) Find the coordinates of the point P on AD such that AP : PD = 2 : 1.

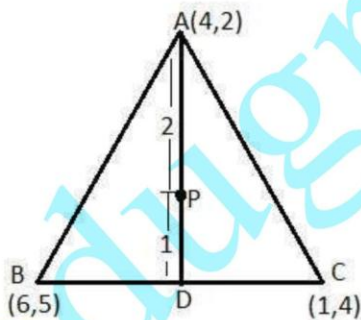
(iii) Find the coordinates of point Q and R on medians BE and CF respectively such that BQ : QE = 2:1 and CR : RF = 2 : 1.

(iv) What do you observe?

[Note : The point which is common to all the three medians is called the centroid and this point divides each median in the ratio 2 : 1.]

(v) If A (x_1, y_1), B (x_2, y_2) and C (x_3, y_3) are the vertices of triangle ABC, find the coordinates of the centroid of the triangle.

Solution:



(i) Coordinates of D can be calculated as follows:

$$\text{Coordinates of D} = \left(\frac{6+1}{2}, \frac{5+4}{2} \right) = \left(\frac{7}{2}, \frac{9}{2} \right)$$

$$D \left(\frac{7}{2}, \frac{9}{2} \right)$$

NCERT Solution For Class 10 Maths Chapter 7 Coordinate Geometry

(ii) Coordinates of P can be calculated as follows:

$$\text{Coordinates of P} = \frac{2\left(\frac{7}{2}\right)+1(4)}{2+1} \quad \frac{2\left(\frac{9}{2}\right)+1(2)}{2+1} \quad \frac{11}{3} \quad \frac{11}{3} \quad \left(\quad , \quad \right) = (,)$$

$$P\left(\frac{11}{3}, \frac{11}{3}\right)$$

(iii) Coordinates of E can be calculated as follows:

$$\text{Coordinates of E} = \left(\quad , \quad \right) = (,) = (5/2, 3)$$

$$E(5/2, 3)$$

Point Q and P would be coincident because medians of a triangle intersect each other at a common point called centroid. Coordinate of Q can be given as follows:

$$\text{Coordinates of Q} = \frac{2(\quad)+1(6)}{2+1} \quad (,) = (,)$$

F is the mid-point of the side AB

$$\text{Coordinates of F} = \left(\quad , \quad \right) = (5,)$$

Point R divides the side CF in ratio 2:1

$$\text{Coordinates of R} = \frac{2\left(\frac{7}{2}\right)+1(4)}{2+1} \quad (,) = (,)$$

(iv) Coordinates of P, Q and R are same which shows that medians intersect each other at a common point, i.e. centroid of the triangle.

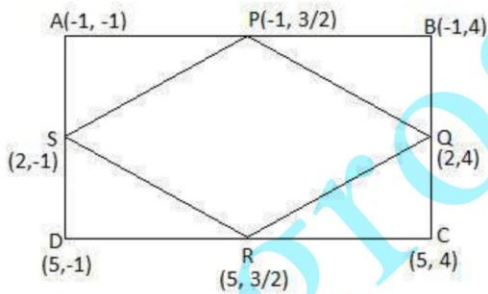
NCERT Solution For Class 10 Maths Chapter 7 Coordinate Geometry

(v) If A (x_1, y_1), B (x_2, y_2) and C (x_3, y_3) are the vertices of triangle ABC, the coordinates of centroid can be given as follows:

$$x = \frac{x_1 + x_2 + x_3}{3} \text{ and } y = \frac{y_1 + y_2 + y_3}{3}$$

8. ABCD is a rectangle formed by the points A (-1, -1), B (-1, 4), C (5, 4) and D (5, -1). P, Q, R and S are the midpoints of AB, BC, CD and DA respectively. Is the quadrilateral PQRS a square? a rectangle? or a rhombus? Justify your answer.

Solution:



P is the mid-point of side AB,

$$\text{Coordinate of P} = \left(\frac{-1-1}{2}, \frac{-1+4}{2} \right) = \left(-1, \frac{3}{2} \right)$$

Similarly, Q, R and S are (As Q is mid-point of BC, R is mid-point of CD and S is midpoint of AD)

$$\text{Coordinate of Q} = (2, 4)$$

$$\text{Coordinate of R} = \left(5, \frac{3}{2} \right)$$

$$\text{Coordinate of S} = (2, -1)$$

Now,

$$\text{Length of PQ} = \sqrt{(-1-2)^2 + \left(\frac{3}{2}-4\right)^2} = \sqrt{\frac{61}{4}} = \frac{\sqrt{61}}{2}$$

**NCERT Solution For Class 10 Maths Chapter 7 Coordinate
Geometry**

$$\text{Length of SP} = \sqrt{(2+1)^2 + \left(-1 - \frac{3}{2}\right)^2} = \sqrt{\frac{61}{4}} = \frac{\sqrt{61}}{2}$$

$$\text{Length of QR} = \sqrt{(2-5)^2 + \left(4 - \frac{3}{2}\right)^2} = \sqrt{\frac{61}{4}} = \frac{\sqrt{61}}{2}$$

$$\text{Length of RS} = \sqrt{(5-2)^2 + \left(\frac{3}{2} + 1\right)^2} = \sqrt{\frac{61}{4}} = \frac{\sqrt{61}}{2}$$

$$\text{Length of PR (diagonal)} = \sqrt{(-1-5)^2 + \left(\frac{3}{2} - \frac{3}{2}\right)^2} = 6$$

$$\text{Length of QS (diagonal)} = \sqrt{(2-2)^2 + (4+1)^2} = 5$$

The above values show that, $PQ = SP = QR = RS = \frac{\sqrt{61}}{2}$, i.e. all sides are equal.

But $PR \neq QS$ i.e. diagonals are not of equal measure.

Hence, the given figure is a rhombus.